

**PERFORMANCE- AND YIELD-DRIVEN  
OPTIMIZATION OF MICROWAVE CIRCUITS  
USING DIRECT EM SIMULATION**

J.W. Bandler

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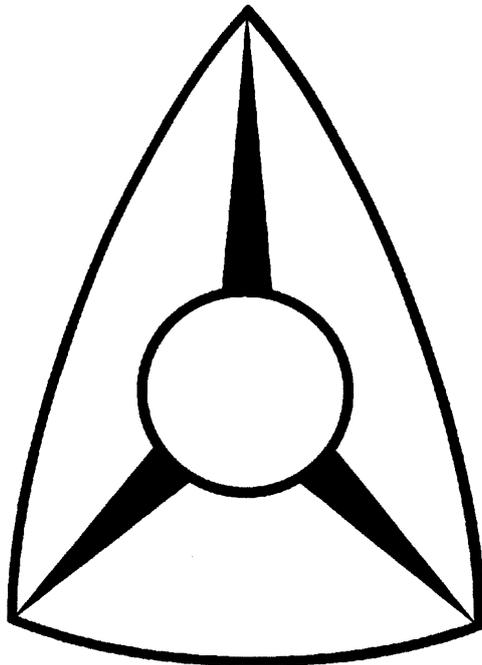
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**Optimization Systems Associates Inc.**

PIONEERS IN

yield and tolerance optimization

circuit performance optimization

parametric design centering

statistical device modeling

robust parameter extraction

harmonic balance simulation

physics based design

EM based design

large-scale optimization

benchmark CAD technology

software architecture for ICs



## **Areas of Expertise**

RF/microwave circuit simulation, design and optimization

harmonic balance simulation techniques

robust and statistical modeling of active and passive devices

automated processing of DC, RF and spectrum data

device modeling, statistical estimation of production yield

powerful performance and yield optimization algorithms

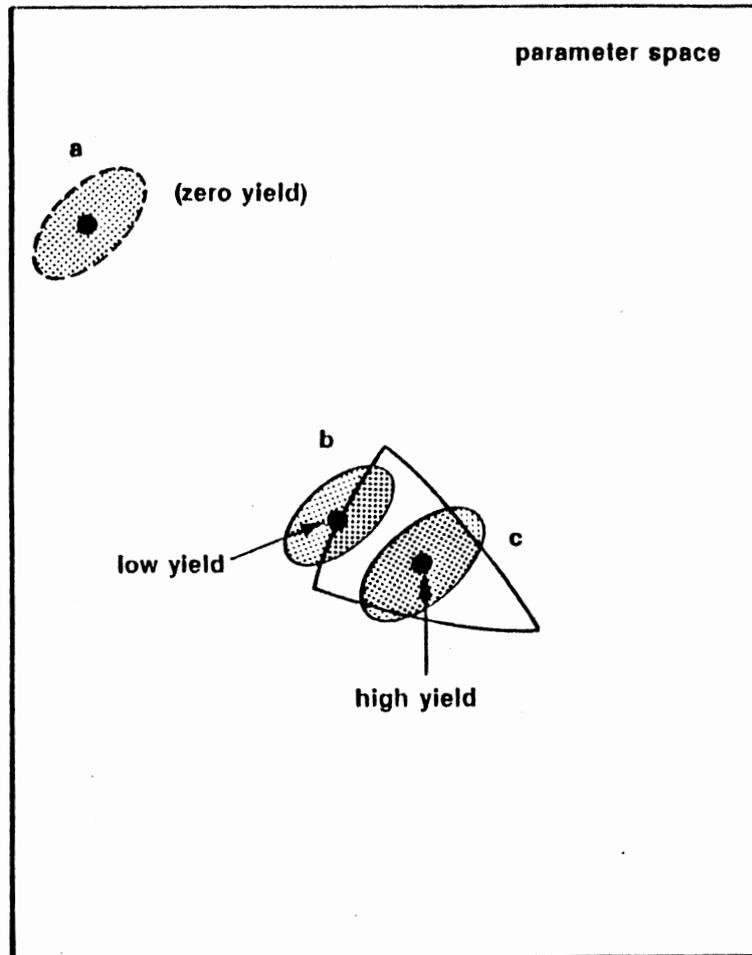
manufacturing tolerance assignment and cost minimization

customized optimizers for large-scale problems

computer optimization of linear and nonlinear networks

algorithms for automated production alignment and tuning

software architectures for integrated approach to design



Yield interpretation in the parameter space



## **Milestones I**

computerized Smith chart plots (1966)

performance-driven optimization (1968)

adjoint sensitivities (1970)

cost-driven worst-case design with optimized tolerances (1972)

centering, tolerance assignment integrated with tuning at the design stage (1974)

integrated approach to microwave design with tolerances and uncertainties (1975)

yield-driven optimization for general statistical distributions (1976)

new results for cascaded circuits (1978)



## **Milestones II**

optimal tuning and alignment at the production stage (1980)

fault diagnosis and parameter extraction (1980)

world's fastest multiplexer optimizer (1984)

introduction of powerful minimax optimizers into commercial CAD/CAE products (1985)

large-scale microwave optimization (1986)

foundation of multi-circuit  $\ell_1$  modeling (1986)

world's first yield-driven design for Super-Compact® (1987)

computational enhancements of commercial CAD/CAE products (1988)

parameter extraction using novel large-scale concepts (1988)



### **Milestones III**

nonlinear adjoint (harmonic balance) exact sensitivities (1988)

RoMPE™, world's first commercial product for FET parameter extraction featuring S-parameters and/or DC data (1988)

yield-driven design of nonlinear microwave circuits (1989)

FAST™, novel technique for high-speed nonlinear sensitivities (1989)

efficient large-signal FET parameter extraction using harmonics (1989)

HarPE™, world's first commercial product for harmonic balance driven FET parameter extraction (1989)

combined discrete/normal statistical modeling of active devices (1989)



## **Milestones IV**

efficient quadratic approximation for statistical design (1989)

nonlinear circuit optimization with dynamically integrated physical device models (1990)

analytically unified DC/small-signal/large-signal circuit design (1990)

OSA90™, world's first friendly optimization engine for performance- and yield-driven design (1990)

Datapipe™ Technology, OSA90's interprocess communication system (1990)

OSA90/hope™, the microwave and RF harmonic optimization system (1991)

design optimization with external simulators, circuit-theoretic and field-theoretic (1991)



## **Milestones V**

statistical modeling of GaAs MESFETs (1991)

gradient quadratic approximation for yield optimization (1991)

physics-based design and yield optimization of MMICs (1991)

Spicepipe™ connection of OSA90/hope™ with Zuberek's SPICE-PAC simulator (1992)

Empipe™ connection of OSA90/hope™ with Sonnet's *em*™ field simulator (1992)

predictable yield-driven circuit optimization (1992)

integrated physics-oriented statistical modeling, simulation and optimization (1992)

Datapipe™ connection of OSA90/hope™ with Hoefler's TLM electromagnetic field simulators (1993)



## **Milestones VI**

Datapipe™ connection of OSA90/hope™ with Nakhla/Zhang VLSI interconnect simulators (1993)

microstrip filter design using direct EM field simulation (1993)

yield-driven direct electromagnetic optimization (1993)

robustizing modeling and design using Huber functions (1993)



## **OSA90/hope™ Version 2.5**

general nonlinear circuit simulation and optimization  
analytically unified

large-signal harmonic balance analysis

small-signal AC analysis

nonlinear DC analysis

statistical analysis and yield optimization

interconnects external simulators

Empipe™ merges *em*™

Spicepipe™ merges SPICE-PAC

user's simulators

customization oriented optimization shell

## **HarPE™ Version 1.7**

parameter extraction and device characterization

single-device circuit simulation and optimization

statistical modeling

Monte Carlo analysis

**OSA90™ (OSA90/hope™ Engine)**



## **OSA90/hope™ Optimization**

state-of-the-art gradient-based optimizers with a proven track record in electrical circuit and system optimization

L1

least squares (L2)

Huber

minimax

quasi-Newton

conjugate gradient

simplex

random

yield (one-sided L1) for statistical centering

exact or approximate gradient

specification and goal definition

quadratic modeling of functions and gradients

sensitivity displays help the user to select the most crucial variables for optimization



## **OSA90/hope™ Circuit Features**

general nonlinear circuit simulation and optimization  
physics-based yield optimization

analytically unified simulation:  
DC/small-signal/large-signal harmonic balance

arbitrary topology  
multitone, multisource excitations  
nonlinear sources controlled by arbitrary voltages

symbolic subcircuit definition: linear and nonlinear  
voltage and current labels (probes)

comprehensive device library  
empirical microstrip models  
*em*™ parameterized microstrip models  
user-definable models



## **OSA90/hope™ Math Features**

variable definition

expressions including conditional *if else* structures

extensive math library

vector and matrix operations

- multiplication

- transposition

- inverse

- LU factorization

- solving linear equations

vector and matrix elements fully optimizable

built-in transformations, including DFT, splines

operation control block



**OSA90/hope™ Graphics**

continuous, point, bar plots

parametric and multiple plots

histograms and run charts

sensitivity displays

waveforms

Smith chart and polar plots

user-defined legends, colors, views

graphics zoom

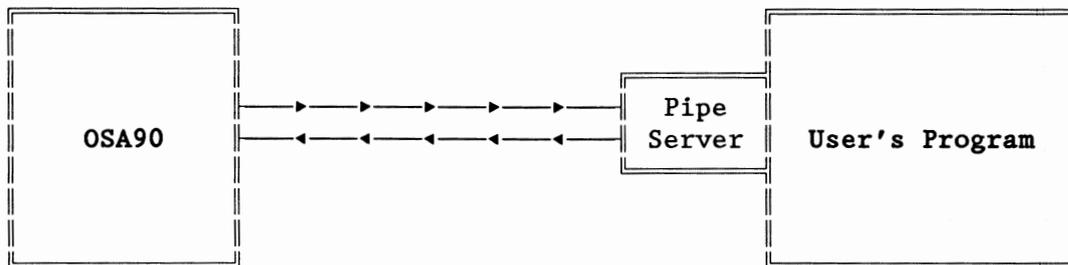
graphics hardcopies (HPGL files)



## **OSA90/hope™ Datapipe™**

**Datapipe™**: predefined protocols for UNIX pipes

ready-to-use to facilitate high-speed data connections to and from the user's software; over networks



typical READ and WRITE statements are used to receive and send data

a small pipe server (about 350 lines) establishes the protocols; OSA provides the source code of the pipe server

maintains complete security of user's software: OSA does not need access to the user's source code



**OSA90/hope™ Connections**

**Empipe™ merges *em*™**

from Sonnet Software, Inc.

for direct field-level optimizable microstrip designs  
under circuit-level linear/nonlinear analysis

**Spicepipe™ merges SPICE-PAC**

for time-domain simulation, noise analysis, etc.  
nominal optimization  
yield optimization

**OSA90™ can call OSA90™**



## **HarPE™ Version 1.7**

characterize devices

extract parameters

- simulation-driven
- data-driven

build equivalent circuit models

build physics models

simulate and optimize

- single device circuits at DC, small-signal and large-signal harmonic balance

statistically model devices

estimate Monte Carlo yield



## Minimax Design Optimization

$$\underset{\phi}{\text{minimize}} \{ \max_j (e_j(\phi)) \}$$

where

$\phi$             the vector of optimization variables

$R_j(\phi)$       $j=1,2,..$  - the circuit responses ( $S$  parameters, return loss, insertion loss, etc.)

$S_{uj}, S_{lj}$     upper/lower specification on  $R_j(\phi)$

the individual errors  $e_j(\phi)$  are of the form

$$e_j(\phi) = R_j(\phi) - S_{uj}$$

or

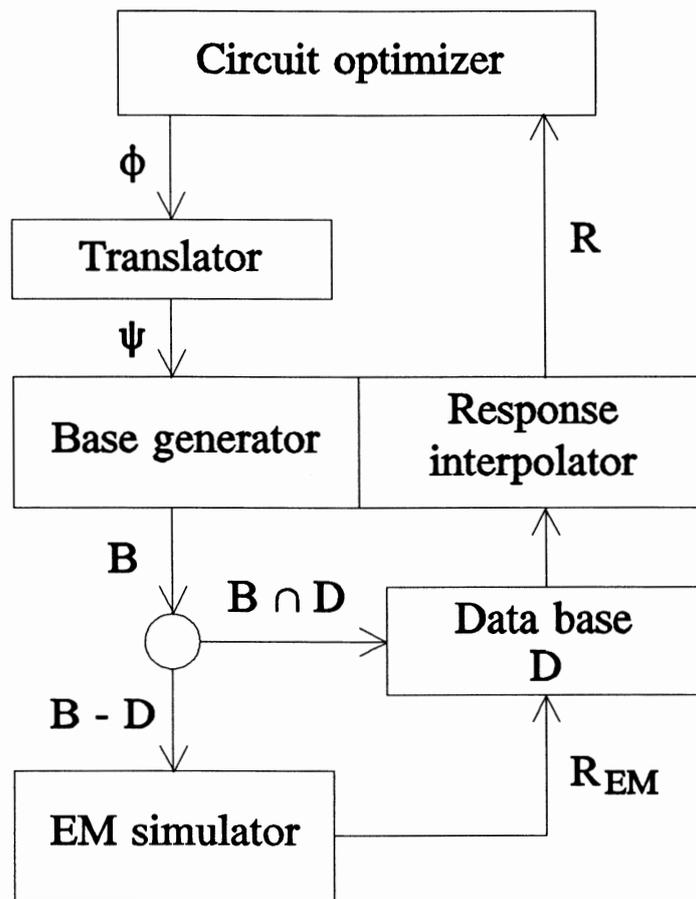
$$e_j(\phi) = S_{lj} - R_j(\phi)$$

negative/positive error value indicates that the corresponding specification is satisfied/violated

effective minimax optimization requires a dedicated optimizer and accurate gradients of individual errors w.r.t. the optimization variables  $\phi$

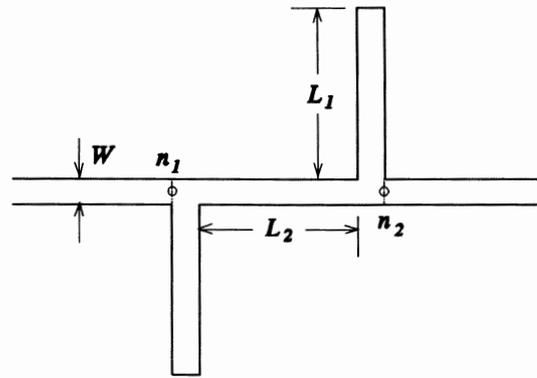


## Interconnection Between a Circuit Optimizer and a Numerical EM Simulator



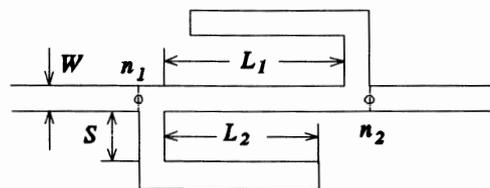


## Conventional Double Stub Microstrip Structure



for band-stop filter applications

## Double Folded Stub Microstrip Structure (Rautio, 1992)



substantially reduces the filter area while achieving the same goal as the conventional double stub structure

can be described by 4 parameters: width, spacing and two lengths  $W$ ,  $S$ ,  $L_1$  and  $L_2$



## **Design of the Double Folded Microstrip Structure**

minimax optimization to move the center frequency of the stop band from 15 GHz to 13 GHz

$W$  fixed at 4.8 mils

$L_1, L_2$  and  $S$  - variables (designable parameters)

design specifications

$$|S_{21}| > -3 \text{ dB} \quad \text{for } f < 9.5 \text{ GHz and } f > 16.5 \text{ GHz}$$

$$|S_{21}| < -30 \text{ dB} \quad \text{for } 12 \text{ GHz} < f < 14 \text{ GHz}$$

substrate thickness - 5 mils

relative dielectric constant - 9.9

*em*<sup>TM</sup> driven by the minimax gradient optimizer of OSA90/hope<sup>TM</sup> through Empipe<sup>TM</sup>

optimization was carried out in two steps

(1)  $\Delta x = \Delta y = 2.4$  mils

(2) the grid size was reduced to  $\Delta x = \Delta y = 1.6$  mils for fine resolution



## **Minimax Optimization of the Double Folded Microstrip Structure**

PARAMETER VALUES FOR THE DOUBLE FOLDED STUB  
BEFORE AND AFTER OPTIMIZATION

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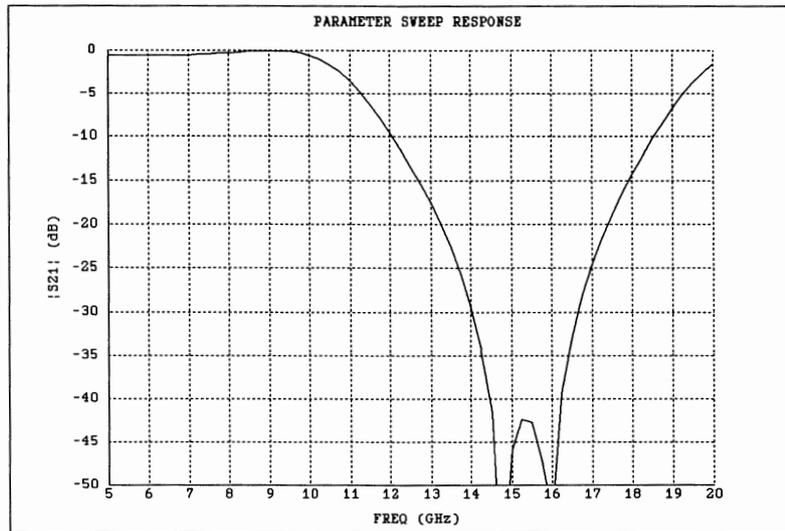
Parameter	Before optimization (mils)	After optimization (mils)
$L_1$	74.0	91.82
$L_2$	62.0	84.71
$S$	13.0	4.80

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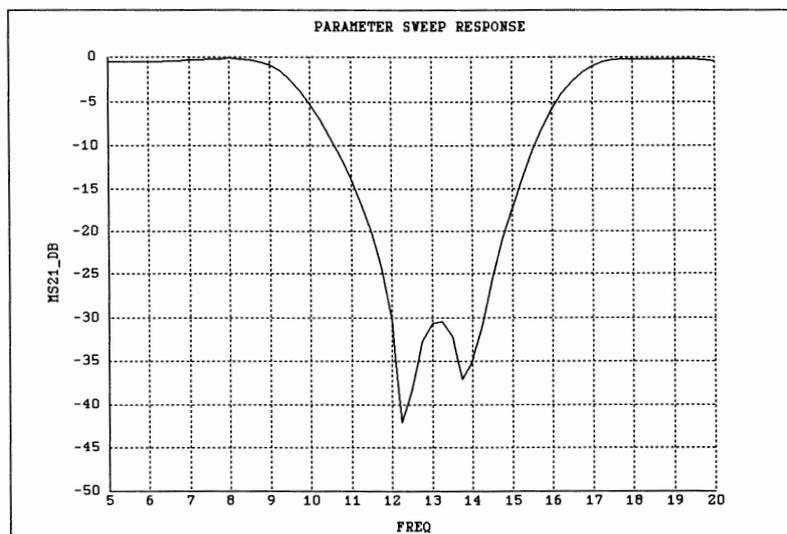


## Results for the Double Folded Microstrip Structure

*Before Optimization*

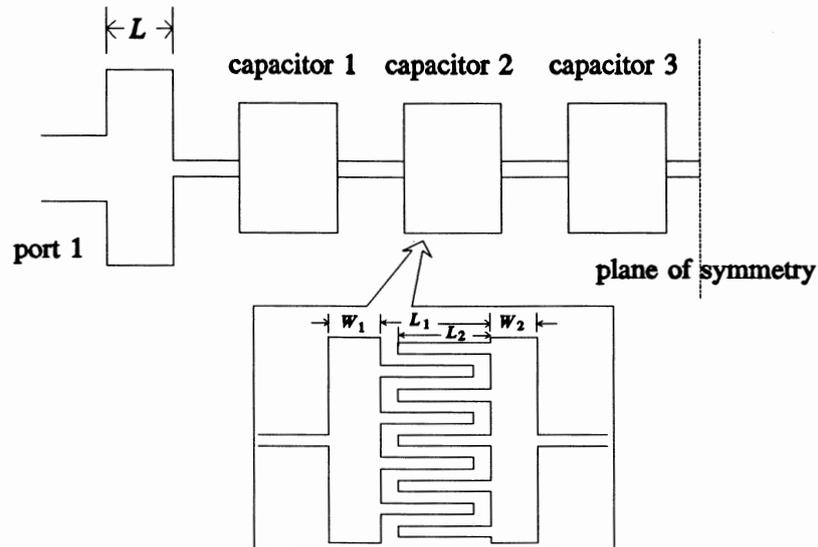


*After Optimization*





## 26-40 GHz Interdigital Microstrip Bandpass Filter



utilizes thin microstrip lines and interdigital capacitors to realize inductances and capacitances of a synthesized lumped ladder circuit

the original microstrip design was determined by matching the lumped prototype at the center frequency using  $em^{TM}$

when the filter was simulated by  $em^{TM}$  in the whole frequency range the results exhibited significant discrepancies w.r.t. the prototype

it necessitated manual adjustment and made a satisfactory design very difficult to achieve



## **Design of the 26-40 GHz Interdigital Microstrip Filter**

a total of 13 designable parameters including the distance between the patches  $L_1$ , the finger length  $L_2$  and two patch widths  $W_1$  and  $W_2$  for each of the three interdigital capacitors, and the length  $L$  of the end capacitor

the second half of the circuit, to the right of the plane of symmetry, is assumed identical to the first half, so it contains no additional variables

the transmission lines between the capacitors were fixed at the originally designed values

design specifications

$$|S_{11}| < -20 \text{ dB} \quad \text{and} \quad |S_{21}| > -0.04 \text{ dB}$$

$$\text{for } 26 \text{ GHz} < f < 40 \text{ GHz}$$

substrate thickness - 10 mils

dielectric constant - 2.25

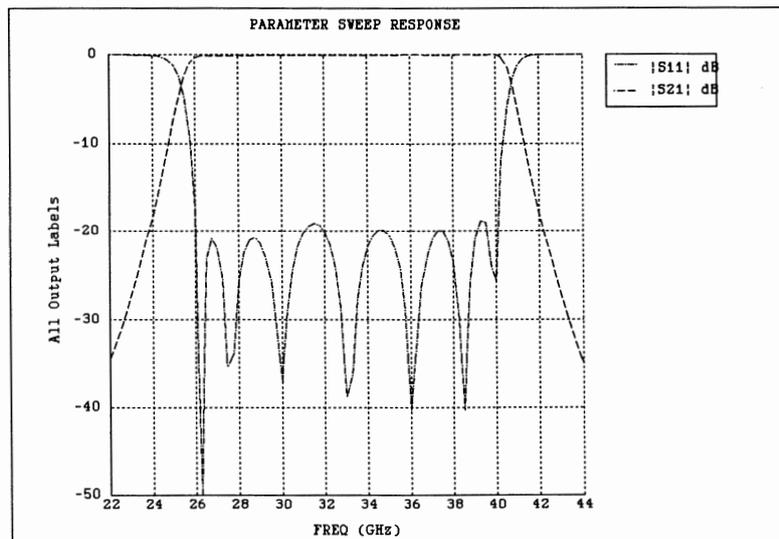
shielding height - 120 mils

*em*<sup>TM</sup> driven by the minimax gradient optimizer of OSA90/hope<sup>TM</sup> through Empipe<sup>TM</sup>



## **Simulation of the 26-40 GHz Interdigital Capacitor Filter After Optimization**

filter response after optimization



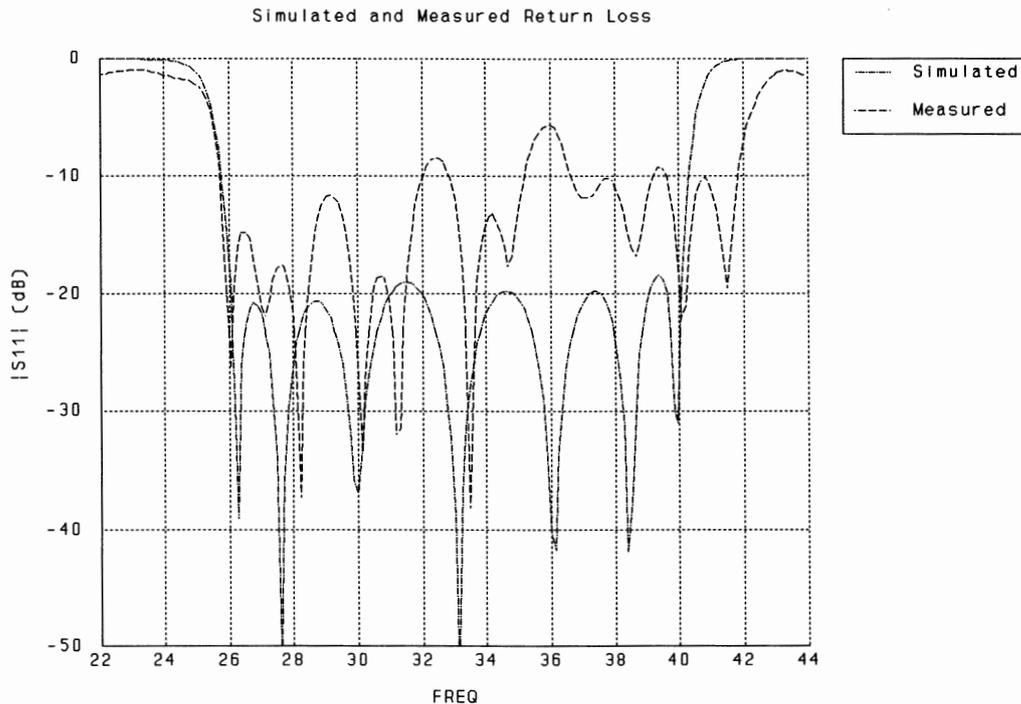
a typical minimax equal-ripple response of the filter was achieved after a series of consecutive optimizations with different subsets of optimization variables and frequency points

the resulting geometrical dimensions were finally rounded to 0.1 mil resolution



## Measurements of the 26-40 GHz Interdigital Capacitor Filter - Return Loss After Optimization

measured and simulated  $|S_{11}|$  of the filter after manufacturing

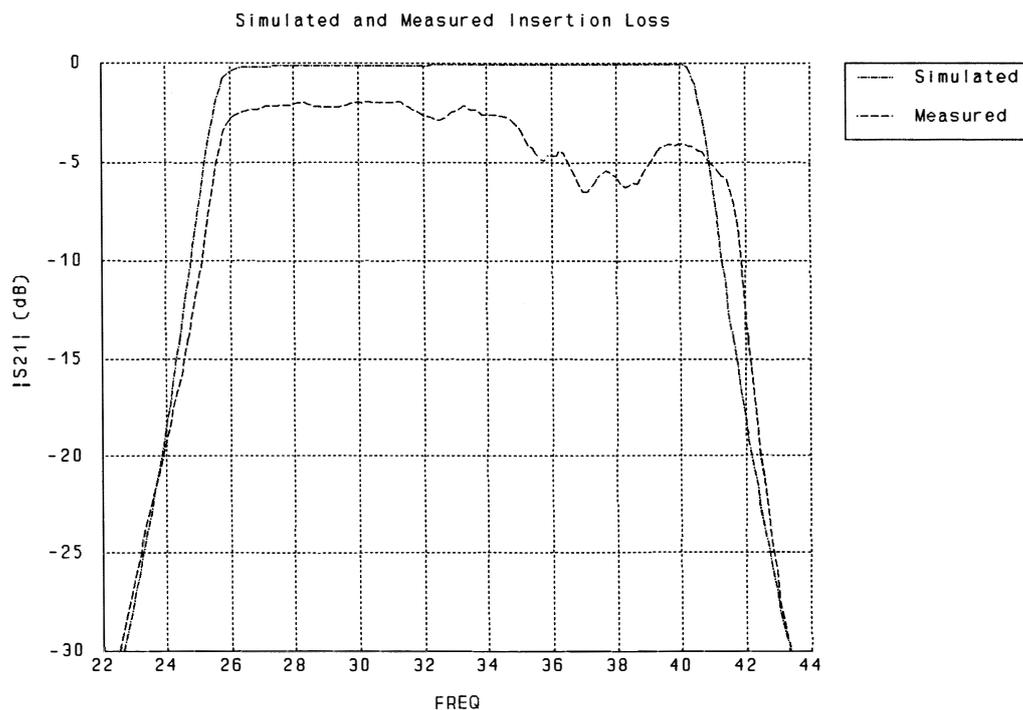


recent improvements in the field solver analysis of interdigital capacitors will improve the accuracy of the bandwidth prediction



## Measurements of the 26-40 GHz Interdigital Capacitor Filter - Insertion Loss After Optimization

measured and simulated  $|S_{21}|$  of the filter after manufacturing



the insertion loss flatness will clearly improve after return loss has been tuned



## Yield Optimization

the problem of yield optimization can be formulated as

$$\underset{\phi^0}{\text{maximize}} \left\{ Y(\phi^0) = \int_{R^n} I_a(\phi) f_\phi(\phi^0, \phi) d\phi \right\}$$

where

$\phi^0$             nominal circuit parameters  
 $\phi$              actual circuit outcome parameters  
 $Y(\phi^0)$        design yield  
 $f_\phi(\phi^0, \phi)$  probability density function of  $\phi$  around  $\phi^0$

$$I_a(\phi) = \begin{cases} 1 & \text{if } \phi \in A \\ 0 & \text{if } \phi \notin A \end{cases}$$

$A$              acceptability region

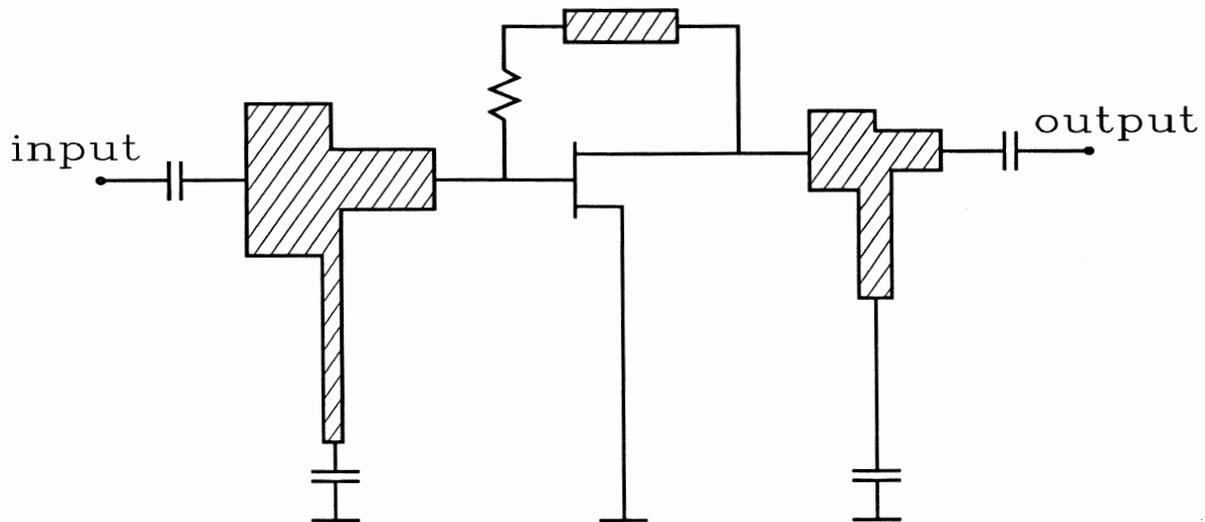
in practice, the integral is approximated using  $K$  Monte Carlo circuit outcomes  $\phi^i$  and yield is estimated by

$$Y(\phi^0) \approx \frac{1}{K} \left( \sum_{i=1}^K I_a(\phi^i) \right)$$

the outcomes  $\phi^i$  are generated by a random number generator according to  $f_\phi(\phi^0, \phi)$



## Optimization of a Small-Signal Amplifier



the specifications for yield optimization of the amplifier are

$$7 \text{ dB} \leq |S_{21}| \leq 8 \text{ dB} \quad \text{for} \quad 6 \text{ GHz} < f < 18 \text{ GHz}$$

the gate and drain circuit microstrip T-junctions and the feedback microstrip line are built on a 10 mil thick substrate with relative dielectric constant 9.9

the microstrip components of the amplifier are simulated using component level Q-models built from EM simulations

we used *em*<sup>TM</sup> from *Sonnet Software* for EM simulations

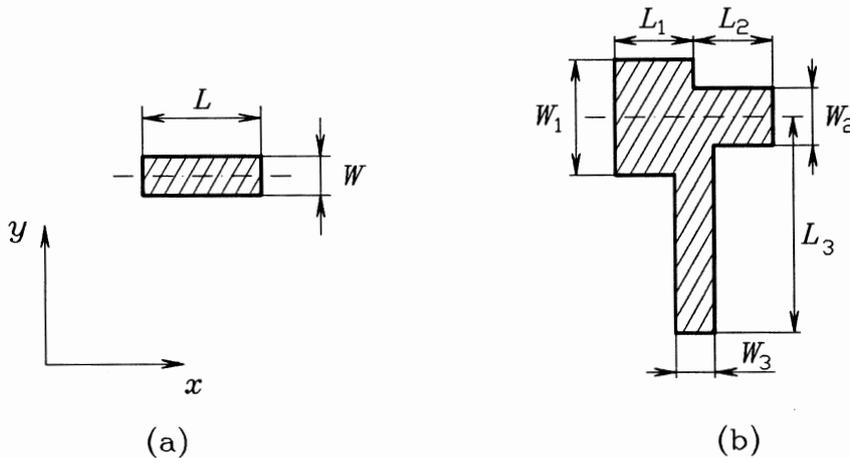


## Optimization Variables

$W_{g1}, L_{g1}, W_{g2}, L_{g2}$  of the gate circuit T-junction and  $W_{d1}, L_{d1}, W_{d2}, L_{d2}$  of the drain circuit T-junction are the optimization variables

$W_{g3}, L_{g3}, W_{d3}$  and  $L_{d3}$  of the T-junctions,  $W$  and  $L$  of the feedback microstrip line, as well as the FET parameters are not optimized

parameters of the microstrip line (a) and the T-junctions (b)



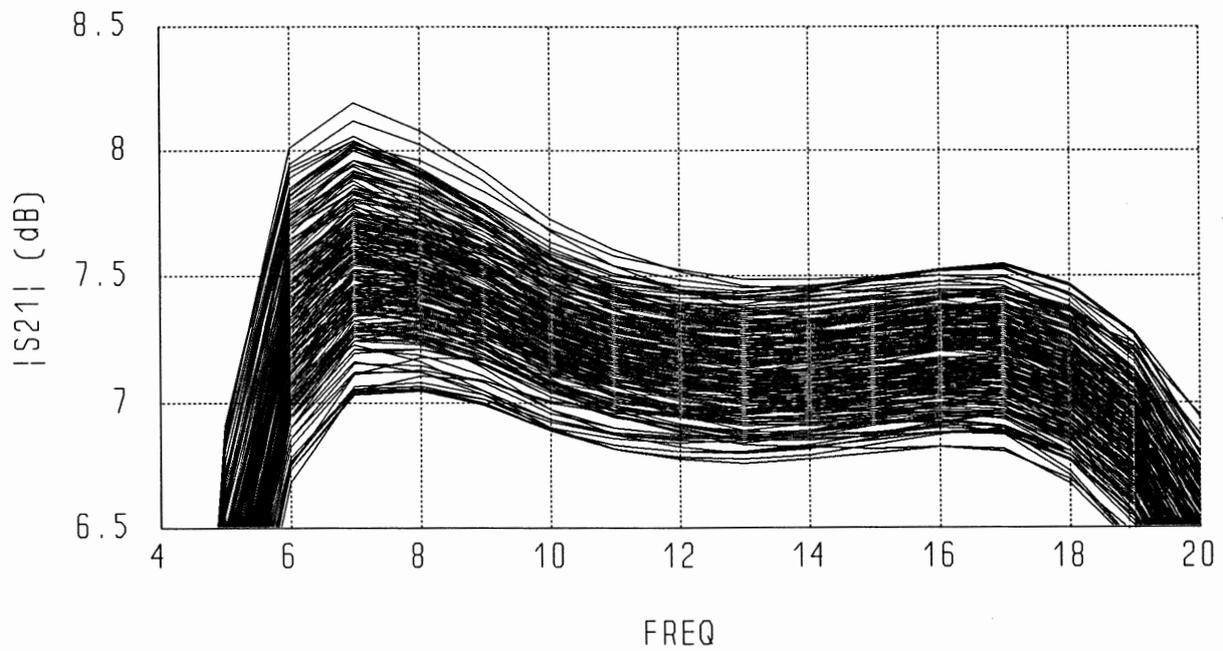
we assumed 0.5 mil tolerance and uniform distribution for all geometrical parameters of the microstrip components

the statistics of the small-signal FET model were extracted from measurement data



## **Small-Signal Amplifier Yield Before Optimization**

the starting point for yield optimization was obtained by nominal minimax optimization using analytical/empirical microstrip component models



**Monte Carlo simulation**

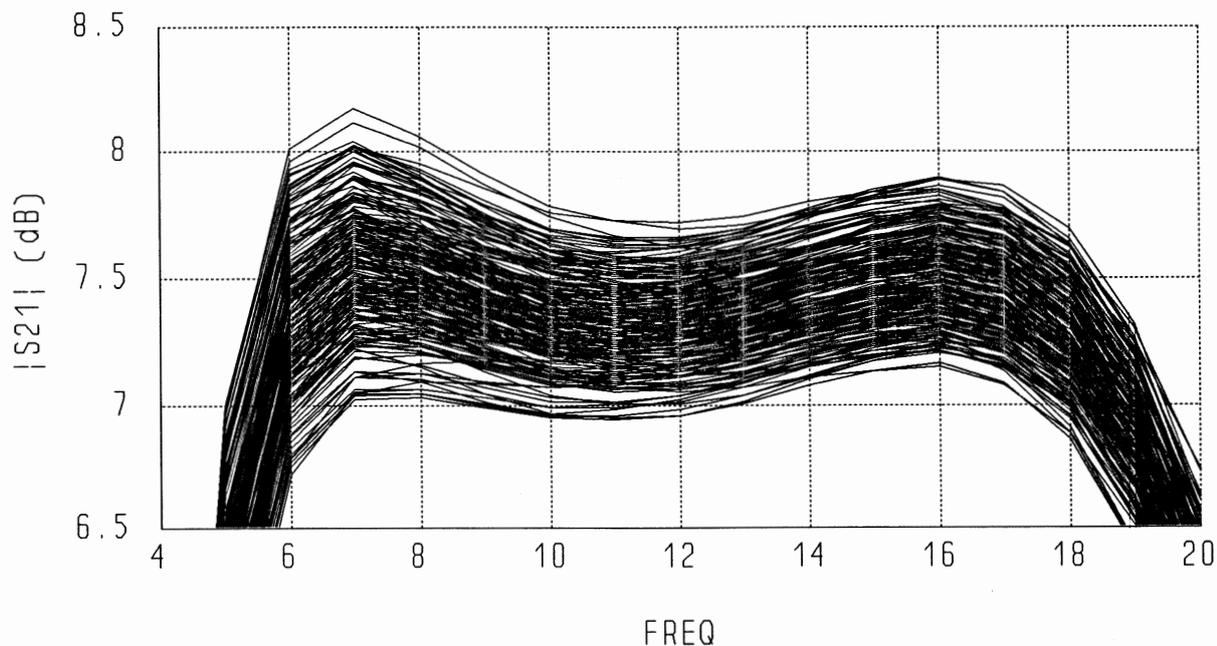
**250 outcomes**

**55% yield**



## Small-Signal Amplifier Yield After Optimization

the component level Q-models were used in yield optimization



yield estimated by 250 Monte Carlo simulations increased to 82%

optimization was performed by OSA90/hope<sup>TM</sup> with Empipe<sup>TM</sup> driving *em*<sup>TM</sup>



## Optimization Results

### MICROSTRIP PARAMETERS OF THE AMPLIFIER

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Parameters	Nominal design	Centered design
$W_{g1}$	17.45	19.0
$L_{g1}$	35.54	34.53
$W_{g2}$	9.01	8.611
$L_{g2}$	30.97	32.0
$W_{g3}$	3.0*	3.0*
$L_{g3}$	107.0*	107.0*
$W_{d1}$	8.562	7.0
$L_{d1}$	4.668	6.0
$W_{d2}$	3.926	3.628
$L_{d2}$	9.902	11.0
$W_{d3}$	3.5*	3.5*
$L_{d3}$	50.0*	50.0*
$W$	2.0*	2.0*
$L$	10.0*	10.0*

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Yield (250 outcomes)	55%	82%
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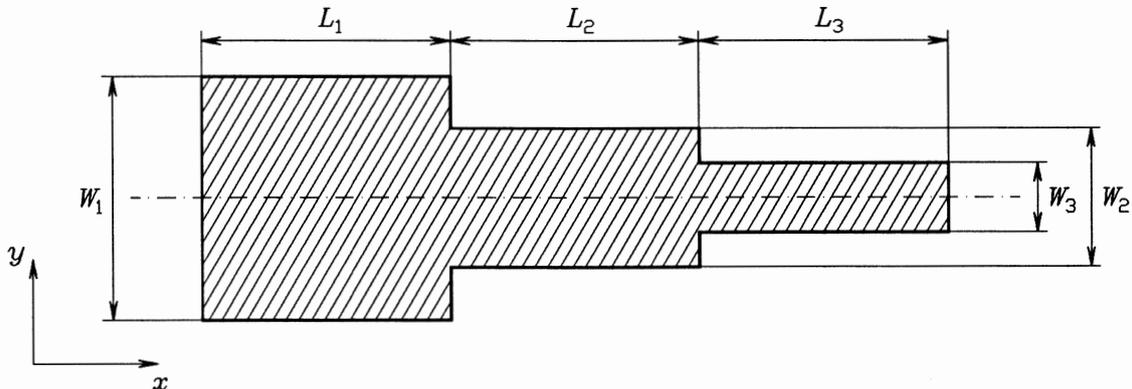
\* Parameters not optimized.

Dimensions of the parameters are in mils. 50 outcomes were used for yield optimization. 0.5 mil tolerance and uniform distribution were assumed for all the parameters.

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### Three-Section 3:1 Microstrip Impedance Transformer



designed on a 0.635 mm thick substrate with relative dielectric constant of 9.7

the source and load impedances are 50 and 150 ohms

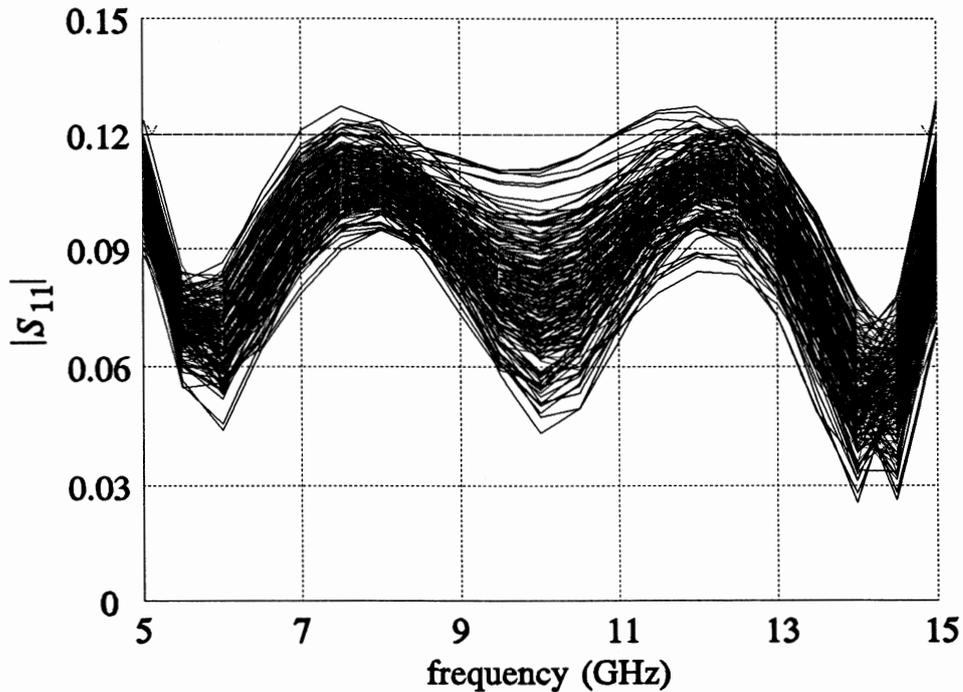
design specification set for the input reflection coefficient

$$|S_{11}| \leq 0.12, \text{ from 5 GHz to 15 GHz}$$

normal distributions with 2% standard deviations assumed for  $W_1$ ,  $W_2$  and  $W_3$  and 1% standard deviations assumed for  $L_1$ ,  $L_2$  and  $L_3$



## Three-Section Microstrip Transformer After Yield Optimization



modulus of the reflection coefficient vs. frequency

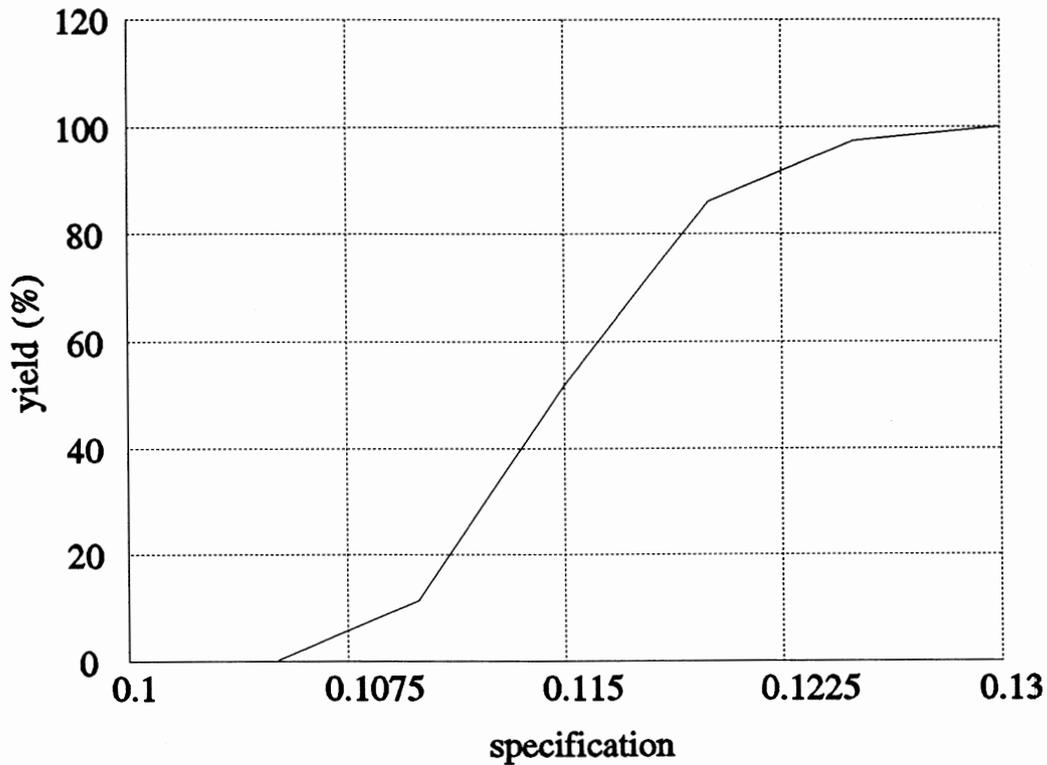
optimization using single-level (component) Q-models

100 statistical outcomes used for yield optimization

yield is increased to 86%



## Yield Sensitivity of the Microstrip Transformer



yield vs. specification on  $|S_{11}|$

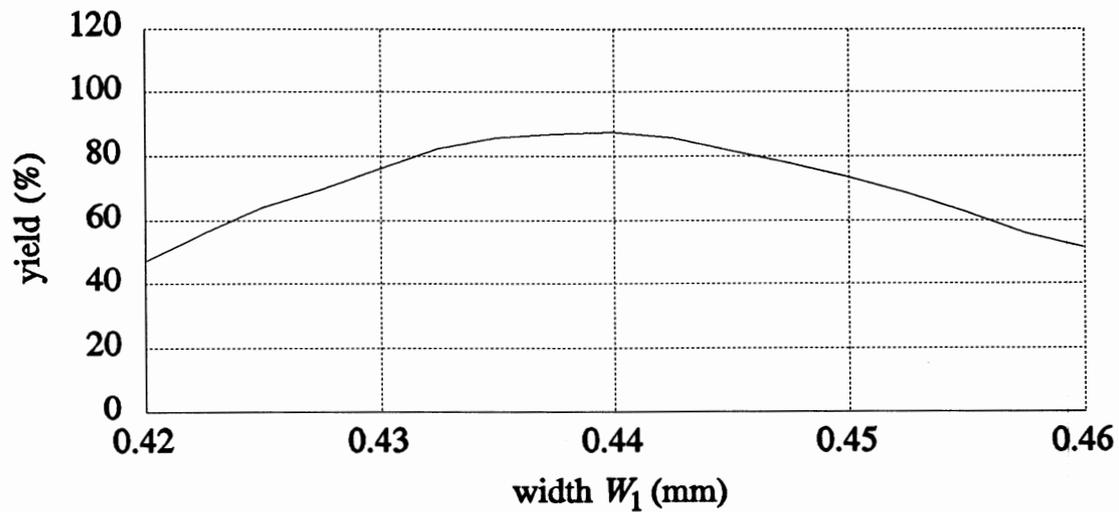
high sensitivity of yield w.r.t. the specification

yield varies from 0% to 100% over a very small range of the specification

yield estimated with 250 Monte Carlo outcomes



## Yield Sensitivity of the Microstrip Transformer



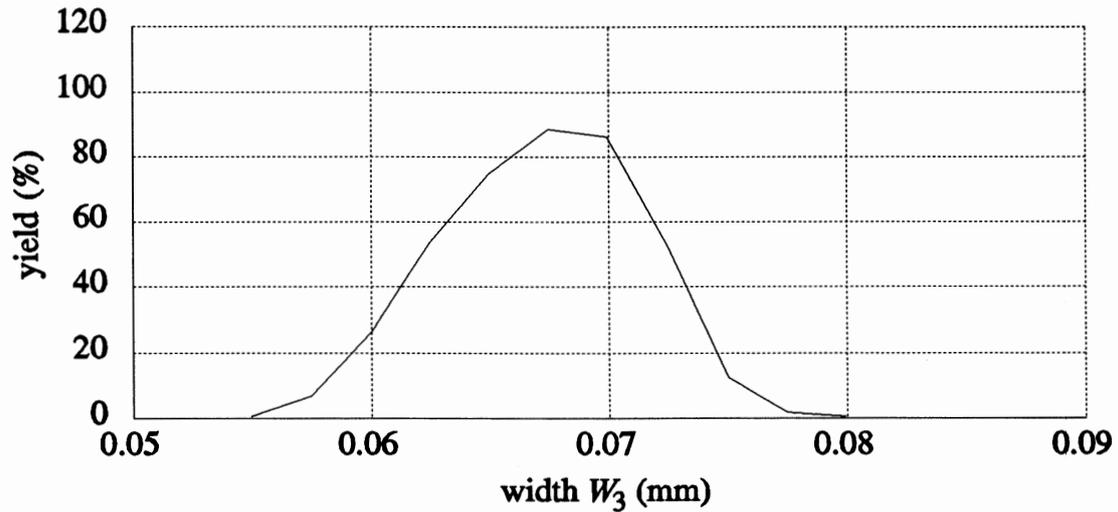
yield vs.  $W_1$

relatively high sensitivity of yield w.r.t.  $W_1$

yield estimated with 250 Monte Carlo outcomes



## Yield Sensitivity of the Microstrip Transformer



yield vs.  $W_3$

high sensitivity of yield w.r.t.  $W_3$

yield estimated with 250 Monte Carlo outcomes



## **Empipe™ (1992)**

smart connection of OSA90/hope™ with Sonnet's *em*™ field simulator for interprocessing circuit/field/measurement data

a significant step towards the required integrated approach offering

simulation, modeling, parameter extraction  
optimization, sensitivity analysis, statistical analysis  
error analysis (probability of satisfying error specs)  
automated processing of circuit/field/measurement data  
fixed or optimizable geometries simulated by *em*™

recent applications include

EM microstrip filter design  
yield-driven direct EM optimization  
EM statistical sensitivity analyses

more relevant experimental validation applications to come!



**Parameterized (Optimizable)  
Microstrip Library of Empipe™**

bend

cross junction

double patch capacitors

interdigital capacitors

line

mitered bend

open stub

overlay double patch capacitors

rectangular structure

spiral inductors

step junction

symmetrical and asymmetrical folded double stubs

symmetrical and asymmetrical gaps

symmetrical and asymmetrical double stubs

T junction