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John W. Bandler

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Presented at the 1993 MTT-S Workshop "Critical Issues in Experimental Validation" Atlanta, GA, June 14, 1993

#### Introduction

questions (Rautio, 1992)

design of experiments error analysis sensitivity analysis experimental significance experimental objective

our aim

to find answers in microwave CAD technology to find answers in analog fault diagnosis to suggest software solutions now available to suggest some open areas for investigation



**Background** (Rautio, 1991)

no sensitivity evaluation

no error analysis

measurements made at a difficult frequency (data with large scatter)

too many "confounding" variables

the experimenter has a desired outcome in mind

incorrect objective

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#### **Our Points of View**

we could take the view that the feature being measured is a "fault" to be diagnosed

or we could take the view that the feature being measured is obscured by elements which may be uncertain or "faulty"

in validation a fluctuation or uncertainty is often under investigation; the experiment must be designed so that the effect is not obscured

examine <u>common denominators</u> of experimental validation, device characterization, parameter extraction and network testing such as approach, objectives, accuracy, uniqueness

soft (faults) deviations

the (faulty) element deviates from its nominal value without reaching its extreme bounds

result from manufacturing tolerances, aging, parasitic effects



#### **Relevant Approaches from Fault Analysis**

fault dictionary approach

dictionary construction selecting an optimal set of measurements dealing with ambiguity sets fault isolation techniques efficient methods of fault simulation

parameter identification techniques

DC or time-domain testing of nonlinear networks multifrequency testing of linear networks select test frequencies to optimize a measure of the solvability of the diagnosis equations? how solvable are the equations given an optimal choice of test frequencies? linear techniques for element value determination

fault verification techniques (consistency checking)

techniques to determine the most likely faults

### **CAT Techniques**

computer-aided analog testing

fault detection fault location parameter identification postproduction tuning

uniqueness often essential

sensitivity to changes, fluctuations and uncertainties should be exposed

#### some challenges

robustness against deviations of other elements robustness against measurement uncertainties establish a measure of testability how to use the minimum number of tests insufficient data (degree of diagnosability)



#### Analog Circuit Theory

1. Circuit Analysis and Simulation

component values assumed <u>all</u> possible solutions of interest relevant to experimental validation

2. Circuit Design and Optimization

component values optimizable good solutions of interest more relevant to experimental validation

3. Circuit Diagnosis and Testing

components under investigation <u>unique</u> solutions of interest most relevant to experimental validation

(Bandler and Salama, "Fault diagnosis of analog circuits", Proc. IEEE, 1985, pp. 1279-1325)



#### **Analog Diagnosis Problem**



resistive mesh circuit

only external nodes are available for excitation and measurements

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#### Analog Diagnosis Using $l_1$ Optimization

$$\begin{array}{cc} \text{minimize} & \sum_{i=1}^{n} |\Delta x_{i}/x_{i}^{0}| \\ \mathbf{x} & \end{array}$$

subject to

where

 $x = [x_1 x_2 \dots x_n]^T$ circuit parameters $x^0$ nominal or assumed parameter values $\Delta x_i = x_i \cdot x_i^0$ deviations from the nominal or<br/>assumed values $V_1^m, \dots, V_K^m$ measurements on the circuit under<br/>test $V_1^c(x), \dots, V_K^c(x)$ calculated circuit responses



Optimization Systems Associates Inc.

#### **Analog Diagnosis Using Huber Optimization**

penalty function approach

$$\min_{\mathbf{x}} \sum_{j=1}^{n+K} \rho_k(f_j(\mathbf{x}))$$

where

$$f_i(x) = \Delta x_i / x_i^0, \quad i = 1, 2, ..., n$$
  
$$f_{n+i}(x) = \beta_i (V_i^c(x) - V_i^m), \quad i = 1, 2, ..., K$$

 $\beta_i$  are appropriate multipliers for the penalty terms



**Huber Functions** 

$$\rho_{k}(f) = \begin{cases} f^{2}/2 & \text{if } |f| \leq k \\ \\ k|f| - k^{2}/2 & \text{if } |f| > k \end{cases}$$

where k is a positive constant

the Huber function  $\rho_k$  is a hybrid of the least-squares  $(\ell_2)$ (when  $|f| \le k$ ) and the  $\ell_1$  (when |f| > k)

Huber Optimization

$$\begin{array}{ll} \text{minimize} \quad F(x) \triangleq \sum_{j=1}^{m} \rho_k(f_j(x)) \\ x \end{array}$$

where  $\mathbf{x} = [x_1 x_2 \dots x_n]^T$  is the set of variables

 $f_j$ , j = 1, 2, ..., m, are error functions

Huber Function as a Hybrid  $\ell_1 / \ell_2$ 



the Huber,  $\ell_1$  and  $\ell_2$  objective functions in the onedimensional case

the strikes represent the discrete points on the  $l_1$  curve

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the continuous curve indicates the Huber objective function



#### **Data Containing Wild Points**



run chart of the FET time-delay  $\tau$ 

extracted from multi-device measurements

#### Huber Solution of Analog Diagnosis Problem

#### FAULT LOCATION OF THE RESISTIVE MESH CIRCUIT

Element	Nominal Value	Actual Value	Percentage Deviation		
			Actual	<i>ℓ</i> <sub>1</sub>	Huber
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G,	1.0	0.50	-50.0*	-48.89	-47.28
G.	1.0	1.04	4.0	0.00	-2.46
G,	1.0	0.97	-3.0	0.00	-1.18
G.	1.0	0.95	-5.0	-2.70	-3.16
G,	1.0	0.99	-1.0	0.00	-0.06
$G_{n}$	1.0	1.02	2.0	0.00	-0.19
G,	1.0	1.05	5.0	0.00	-0.41
Ĝ	1.0	1.02	2.0	2.41	3.75
G.o.	1.0	0.98	-2.0	0.00	0.39
G.,	1.0	1.04	4.0	0.00	-0.37
G	1.0	1.01	1.0	2.73	1.32
G.,	1.0	0.99	-1.0	0.00	-0.26
G.,	1.0	0.98	-2.0	0.00	-0.50
G.,	1.0	1.02	2.0	0.00	-0.05
G15	1.0	0.96	-4.0	-3.36	-2.67
G 16	1.0	1.02	2.0	0.00	-0.61
G 17	1.0	0.50	-50.0*	-50.09	-47.33
G18	1.0	0.98	-2.0	-1.41	-3.81
$G_{20}^{19}$	1.0	0.96	-4.0	-4.40	-4.72

\* Faults



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common sense judgement used to "validate" the design

sophisticated validation algorithms could enhance the common sense judgement approach



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built on a 25 mil thick alumina substrate with a relative dielectric constant of 9.8

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100 seconds for the inductor10 seconds for the center capacitor8 seconds for the end capacitor

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symmetry of the filter is utilized by simulating only one inductor and one end capacitor

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**EM**-Simulation and Measurements of the Low-Pass Filter (Swanson, 1991)



electromagnetic simulation using em<sup>™</sup>

very good approximation of filter behaviour, in particular around the cut-off frequency

### **Optimization Technology for Automated CAD**

parameterized models based on physics, fields, circuits, experiments

circuit theory for interconnection

numerical algorithms for simulation and optimization

### objectives

meet parameter constraints exceed performance specifications tolerance optimization yield maximization cost minimization

uniqueness not essential

sensitivity to changes, fluctuations and uncertainties should be considered but their effects minimized



Integrated Approach to Microwave Design (Bandler Liu and Tromp, 1975)

benchmark considerations of the integrated approach

optimal design centering optimal design tolerancing optimal design tuning parasitic effects uncertainties in models and reference plane mismatched terminations

we now need an <u>integrated approach</u> to experimental validation to address some of Rautio's questions

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#### **Three-Section 3:1 Microstrip Impedance Transformer**



designed on a 0.635 mm thick substrate with relative dielectric constant of 9.7

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Yield-Driven Electromagnetic Optimization of the Microstrip Transformer

yield optimization started from the solution of a nominal minimax design

single vs. multilevel modeling - two experiments:

yield optimization using single-level (component) modeling

yield optimization using two-level (component and circuit response) modeling

the Q-models were updated during optimization whenever necessary

selection of optimization variables - two experiments:

all six variables  $W_1, W_2, W_3, L_1, L_2$  and  $L_3$  selected

only three variables  $W_1$ ,  $W_2$  and  $W_3$  selected



### Three-Section Microstrip Transformer After Yield Optimization



modulus of the reflection coefficient vs. frequency optimization using single-level (component) Q-models 100 statistical outcomes used for yield optimization yield is increased to 86%



three-section 3:1 microstrip transformer

sensitivity analysis performed at the solution of yield optimization with all six optimization variables

seven experiments:

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- each of the six optimization variables is individually swept

yield is very sensitive to the widths of all the sections and is quite insensitive to the lengths

250 Monte Carlo outcomes used for yield estimation

the results were obtained with little additional computational effort



### Yield Sensitivity of the Microstrip Transformer



yield vs. specification on  $|S_{11}|$ 

high sensitivity of yield w.r.t. the specification

yield varies from 0% to 100% over a very small range of the specification





yield vs.  $W_1$ 

relatively high sensitivity of yield w.r.t.  $W_1$ 

yield estimated with 250 Monte Carlo outcomes



#### Yield Sensitivity of the Microstrip Transformer



yield vs.  $W_2$ 

high sensitivity of yield w.r.t.  $W_2$ 





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high sensitivity of yield w.r.t.  $W_3$ 

yield estimated with 250 Monte Carlo outcomes



#### Yield Sensitivity of the Microstrip Transformer



yield vs.  $L_1$ 

low sensitivity of yield w.r.t.  $L_1$ 







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yield estimated with 250 Monte Carlo outcomes



#### Yield Sensitivity of the Microstrip Transformer



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these CAD tools merge multi-circuit/device/domain/bias modeling principles with novel  $l_1$  objectives to enhance precision and uniqueness

robustized modeling and design using Huber functions are coming



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smart connection of OSA90/hope<sup>™</sup> with Sonnet's *em*<sup>™</sup> field simulator for interprocessing circuit/field/measurement data

a significant step towards the required <u>integrated approach</u> offering

simulation, modeling, parameter extraction optimization, sensitivity analysis, statistical analysis error analysis (probability of satisfying error specs) automated processing of circuit/field/measurement data fixed or optimizable geometries simulated by *em*<sup>TM</sup>

recent applications include

EM microstrip filter design yield-driven direct EM optimization EM statistical sensitivity analyses

more relevant experimental validation applications to come!

Parameterized (Optimizable) Microstrip Library of Empipe<sup>™</sup>

bend cross junction double patch capacitors interdigital capacitors line mitered bend open stub overlay double patch capacitors rectangular structure spiral inductors step junction symmetrical and asymmetrical folded double stubs symmetrical and asymmetrical gaps symmetrical and asymmetrical double stubs T junction



#### Conclusions

sensitivity evaluation well-understood in analysis, design and testing

error analysis already part of statistical modeling/design systems

measurements made at a difficult frequency see work on multifrequency testing

too many "confounding" variables similar treatment as for "soft faults"

the experimenter has a desired outcome in mind quite an opposite outcome in fault diagnosis!

incorrect objective answered by diagnosability and testability theory

CAD software frameworks available for immediate exploitation

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subject to

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.  
.  
.  
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penalty function approach

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the Huber,  $\ell_1$  and  $\ell_2$  objective functions in the onedimensional case

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the source and load impedances are 50 and 150 ohms

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