# **Space Mapping Based Neuromodeling**

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conventional ANN approach for microwave modeling

neuromodeling using existing knowledge

SM-based neuromodeling

examples

other applications of SM-based neuromodeling





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ANNs are suitable in modeling high-dimensional and highly nonlinear problems

ANN models are computationally efficient and more accurate than empirical models

multilayer feedforward networks can approximate any function to any desired level of accuracy (*White et al.*, 1992)

ANNs that are too small cannot approximate the desired input-output relationship

ANNs with too many internal parameters perform correctly in the learning set, but give poor generalization ability





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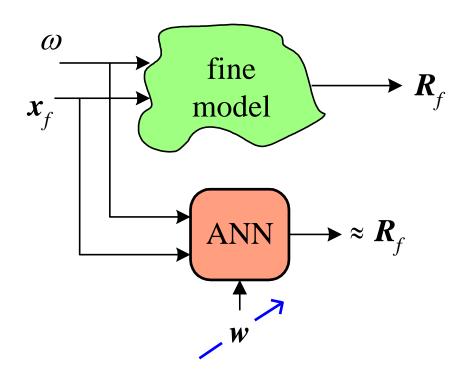
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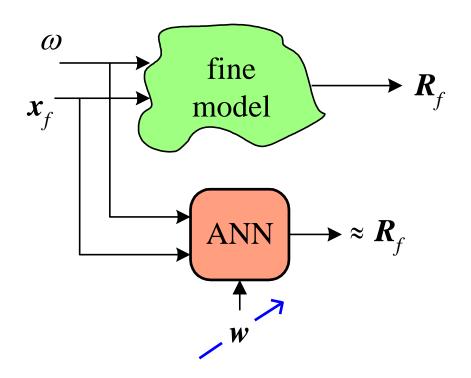
many fine model simulations are usually needed

the number of learning samples grows exponentially with the dimensionality (*Stone, 1982*)

the reliability of multi-layer perceptrons for extrapolation is poor







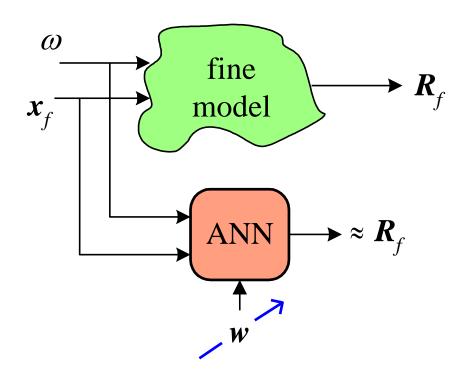
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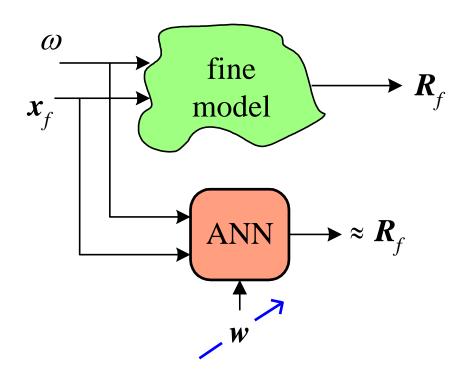
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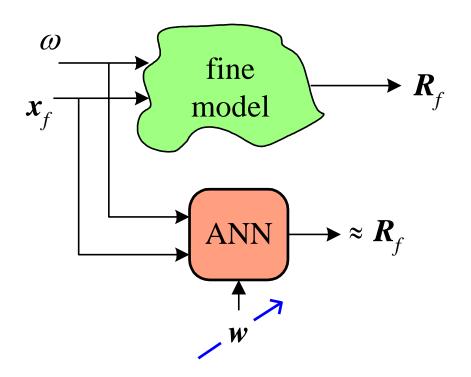
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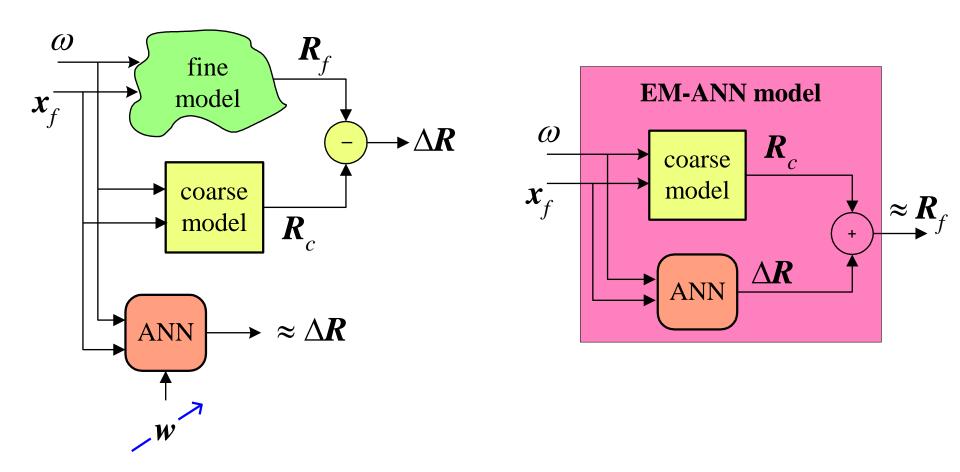
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# **Hybrid "ΔS" EM-ANN Neuromodeling Concept** (*Gupta et al., 1996*)

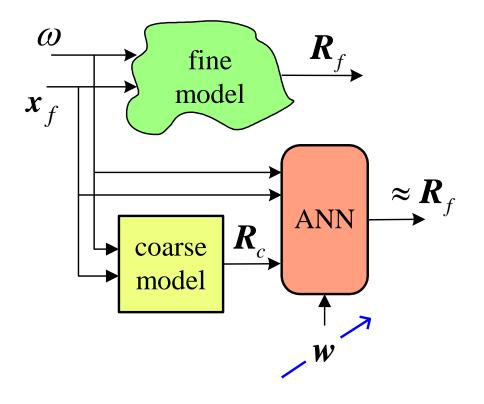


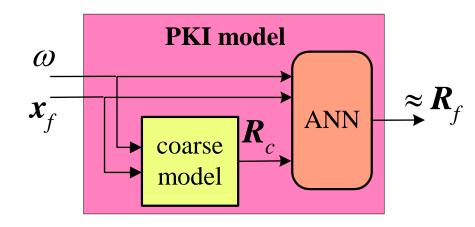




# **PKI Neuromodeling Concept**

(Gupta et al., 1996)



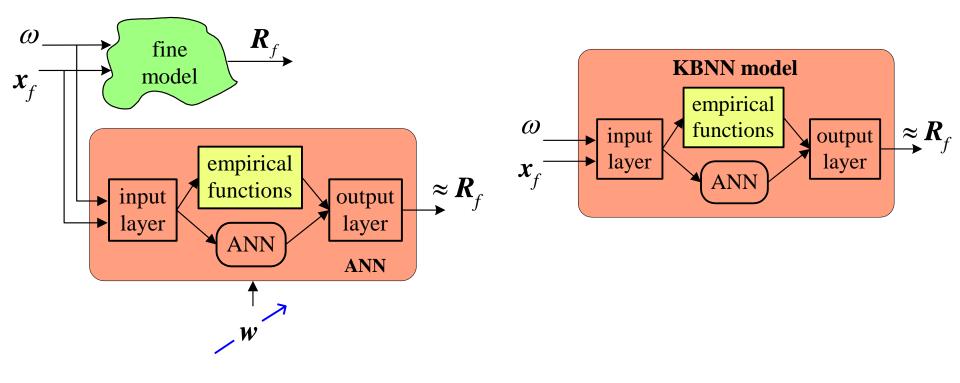






## **KBNN Neuromodeling Concept**

(Zhang et al., 1997)

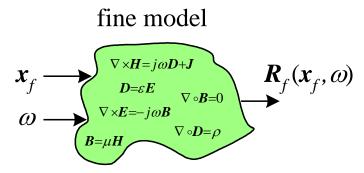






# **Exploiting Space Mapping for Neuromodeling**

(Bandler et. al., 1999)



coarse model  $F_c \rightarrow \overbrace{c_3 = f(w,d)}^{\mathbb{C}} \xrightarrow{c_3 = f(w,d)} R_c(x_c, \omega_c)$ 

find

$$\begin{bmatrix} \boldsymbol{x}_c \\ \boldsymbol{\omega}_c \end{bmatrix} = \boldsymbol{P}(\boldsymbol{x}_f, \boldsymbol{\omega})$$

such that

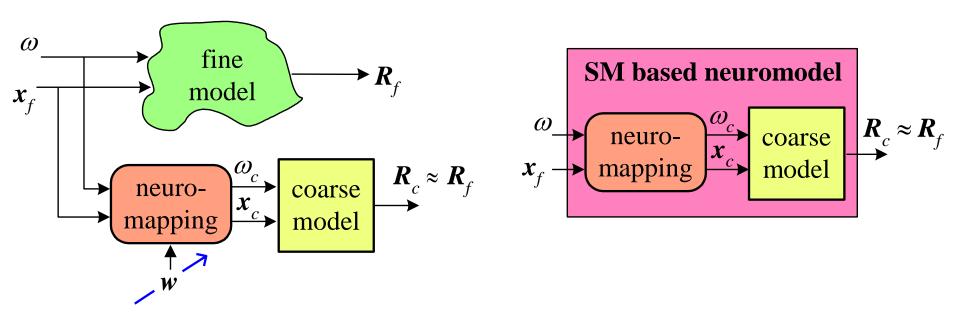
 $\boldsymbol{R}_{c}(\boldsymbol{x}_{c},\boldsymbol{\omega}_{c}) \approx \boldsymbol{R}_{f}(\boldsymbol{x}_{f},\boldsymbol{\omega})$ 





### **Space Mapping Based Neuromodeling**

(Bandler et. al., 1999)



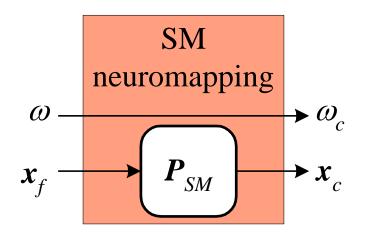


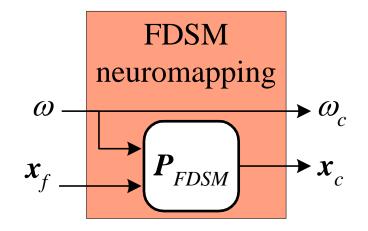


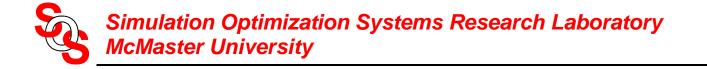
#### Neuromappings

Space Mapped neuromapping

Frequency-Dependent Space Mapped neuromapping





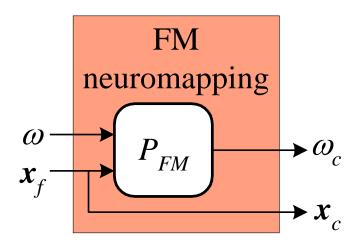


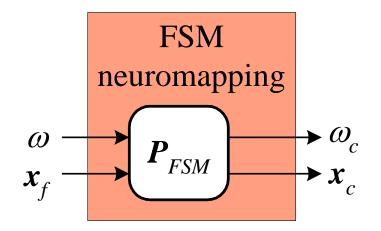


#### **Neuromappings (continued)**

Frequency Mapped neuromapping

Frequency Space Mapped neuromapping



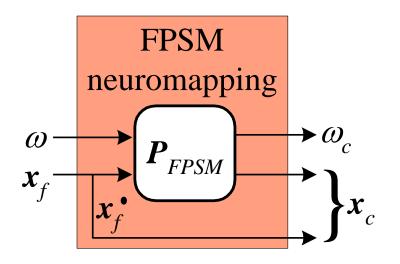






#### **Neuromappings (continued)**

Frequency Partial-Space Mapped neuromapping



it is not always necessary to map the whole set of design parameters

coarse model sensitivities can be used to select the mapped parameters





**Training the SM-Based Neuromodel** 

$$\boldsymbol{w}^{*} = \arg\min_{\boldsymbol{w}} \left\| \begin{bmatrix} \cdots & \boldsymbol{e}_{s}^{T} & \cdots \end{bmatrix}^{T} \right\|$$
$$\boldsymbol{e}_{s} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f}^{(l)}, \boldsymbol{\omega}_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{c_{j}}^{(l)}, \boldsymbol{\omega}_{c_{j}}) \qquad \boldsymbol{e}_{s} \in \Re^{r}$$
$$\begin{bmatrix} \boldsymbol{x}_{c_{j}}^{(l)} \\ \boldsymbol{\omega}_{c_{j}} \end{bmatrix} = \boldsymbol{P}(\boldsymbol{x}_{f}^{(l)}, \boldsymbol{\omega}_{j}, \boldsymbol{w})$$
$$j = 1, \dots, F_{p} \qquad l = 1, \dots, 2n+1 \qquad s = j + F_{p}(l-1)$$

*r* is the number of responses in the model

*P* is the neuromapping function and *w* contains the free parameters of the ANN 2n+1 is the number of training base points and  $F_p$  is the number of frequency points Huber optimization is used to solve this problem

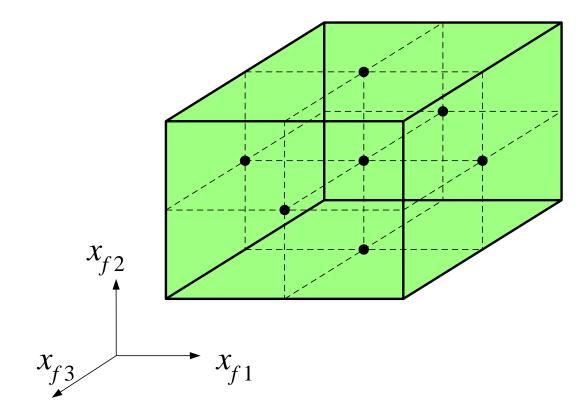




#### **Starting Point and Learning Samples**

we chose a unit mapping ( $\mathbf{x}_c = \mathbf{x}_f$  and  $\omega_c = \omega$ ) as the starting point for the optimization problem

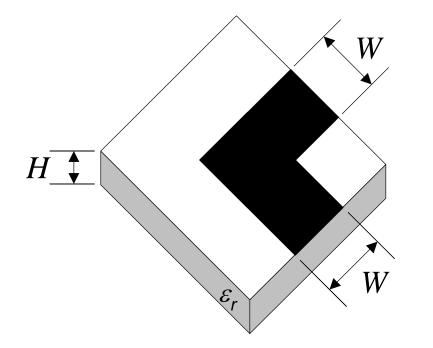
2n+1 points are used for a microwave circuit with *n* design parameters







#### **Microstrip Right Angle Bend**



region of interest  $20\text{mil} \le W \le 30\text{mil}$   $8\text{mil} \le H \le 16\text{mil}$   $8 \le \varepsilon_r \le 10$  $1\text{GHz} \le \omega \le 41\text{GHz}$ 

"coarse" model: equivalent circuit model (Gupta, Garg and Bahl, 1979)

"fine" model: Sonnet's  $em^{TM}$ 

learning set: 7 base points with "star" distribution

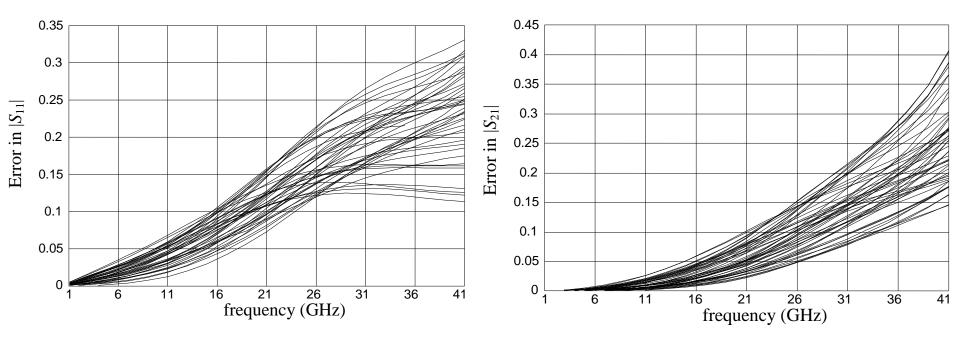
testing set: 50 random base points





#### **Microstrip Right Angle Bend Coarse Model Errors**

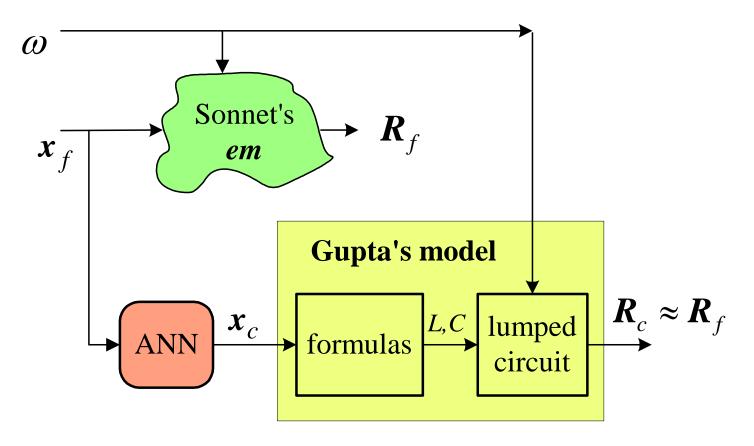
comparison between  $em^{TM}$  and coarse model at 50 random test points







SM Neuromodel for the Right Angle Bend (3LP:3-6-3)



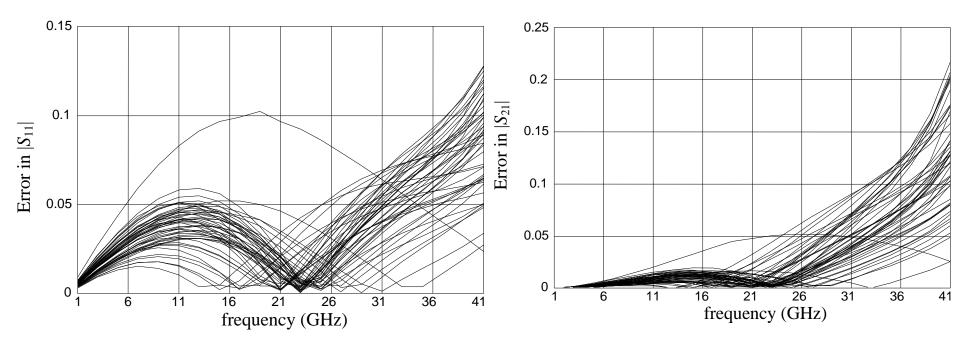
 $\boldsymbol{x}_{f} = [W \ H \ \varepsilon_{r}]^{T}$ 





#### **SM Neuromodel Results for the Right Angle Bend**

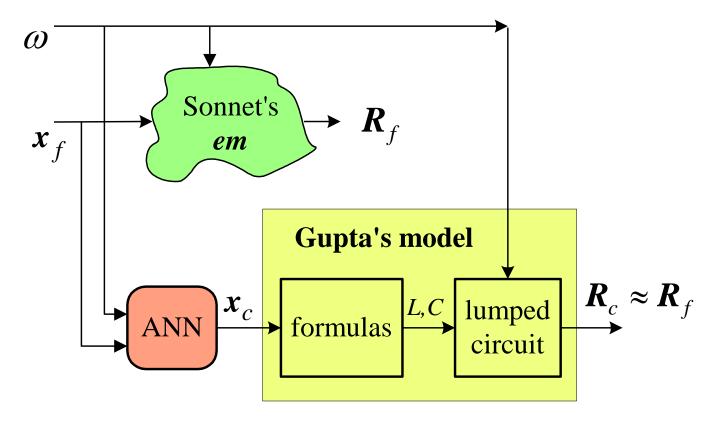
comparison between *em*<sup>TM</sup> and the SM neuromodel







#### FDSM Neuromodel for the Right Angle Bend (3LP:4-7-3)



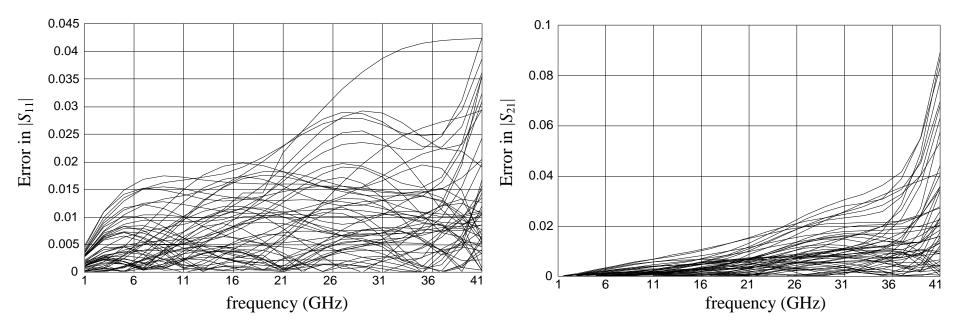
 $\boldsymbol{x}_{f} = [W \ H \ \varepsilon_{r}]^{T}$ 





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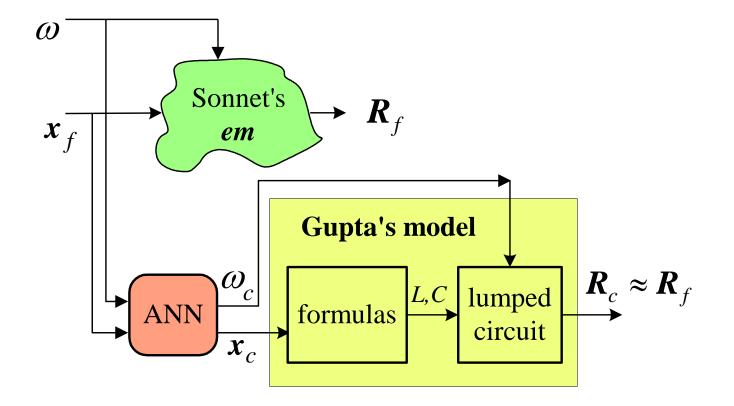
comparison between *em*<sup>TM</sup> and the FDSM neuromodel







#### FSM Neuromodel for the Right Angle Bend (3LP:4-8-4)



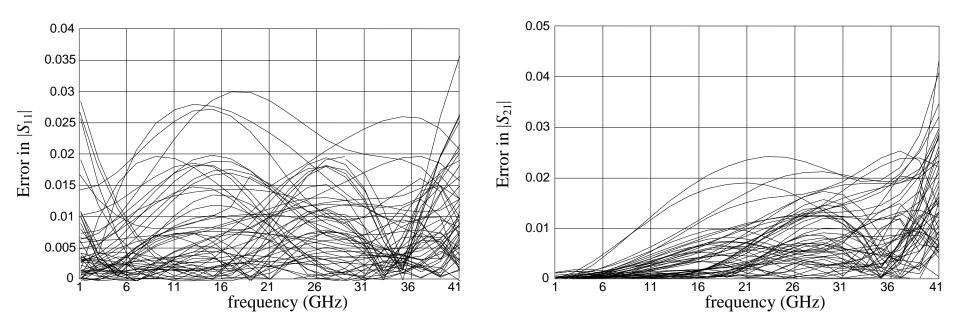
 $\boldsymbol{x}_{f} = [W \ H \ \varepsilon_{r}]^{T}$ 





#### FSM Neuromodel Results for the Right Angle Bend

comparison between *em*<sup>TM</sup> and the FSM neuromodel



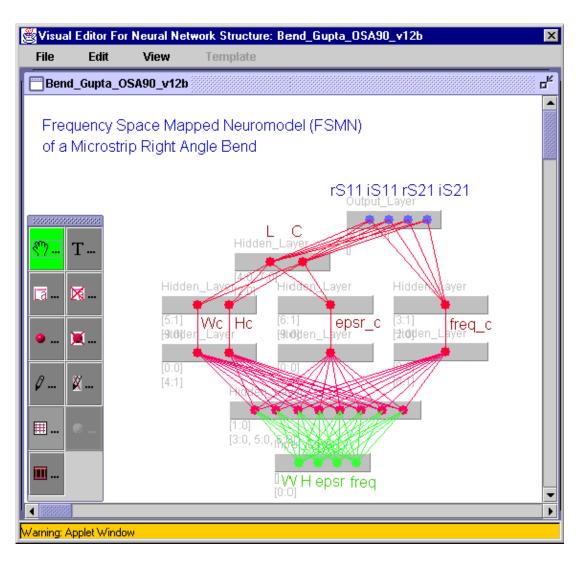




### Implementations in *NeuroModeler*

SM based neuromodels of several microstrip circuits have been developed using *NeuroModeler* version 1.2b (1999)

they are entered into HP ADS version 1.1 (1999) as library components through an ADS plugin module

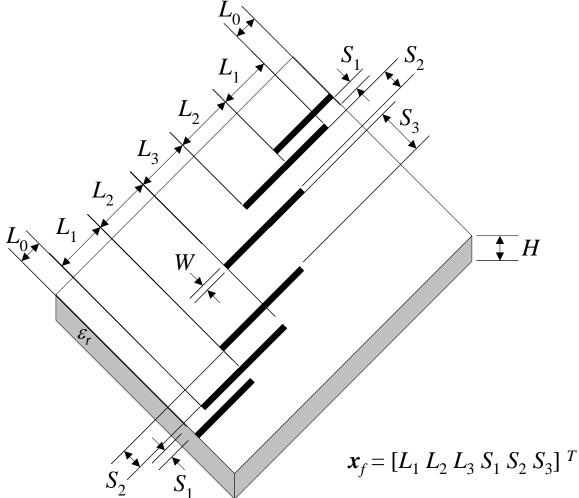






## **HTS Quarter-Wave Parallel Coupled-Line Microstrip Filter**

(Westinghouse, 1993)



region of interest

```
175mil \leq L_1 \leq 185mil
     190 \text{mil} \le L_2 \le 210 \text{mil}
     175mil \leq L_3 \leq 185mil
       18 \text{mil} \le S_1 \le 22 \text{mil}
       75mil \leq S_2 \leq 85mil
       70\text{mil} \le S_3 \le 90\text{mil}
3.901GHz \leq \omega \leq 4.161GHz
```

$$L_0 = 50 \text{mil}$$

$$H = 20 \text{mil}$$

$$W = 7 \text{mil}$$

$$\varepsilon_r = 23.425$$
loss tangent = 3×10<sup>-5</sup>

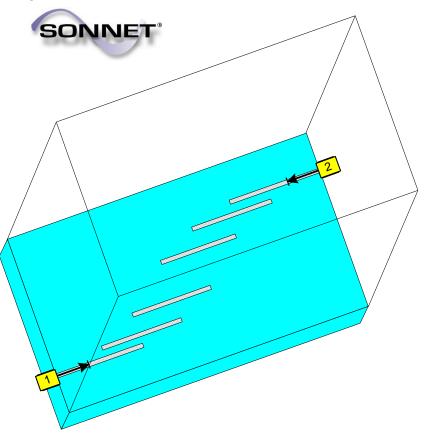




### **HTS Microstrip Filter: Fine and Coarse Models**

fine model:

Sonnet's *em*<sup>™</sup> with high resolution grid



coarse model:

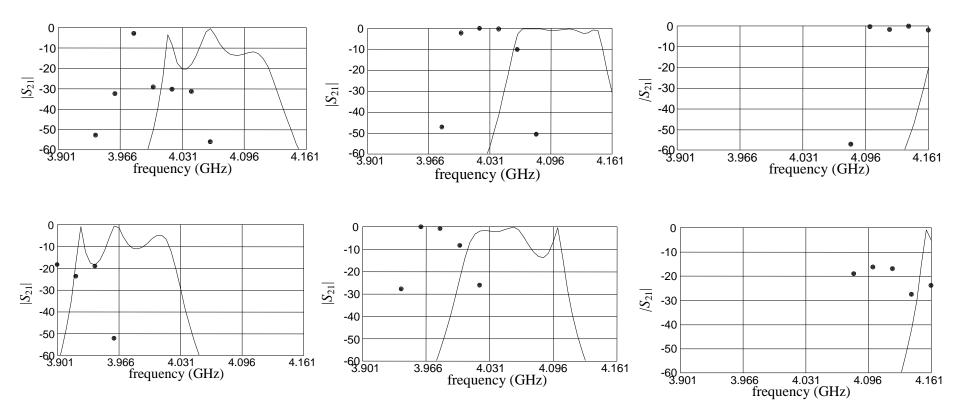
OSA90/hope<sup>™</sup> built-in models of open circuits, microstrip lines and coupled microstrip lines





#### **HTS Filter Responses Before Neuromodeling**

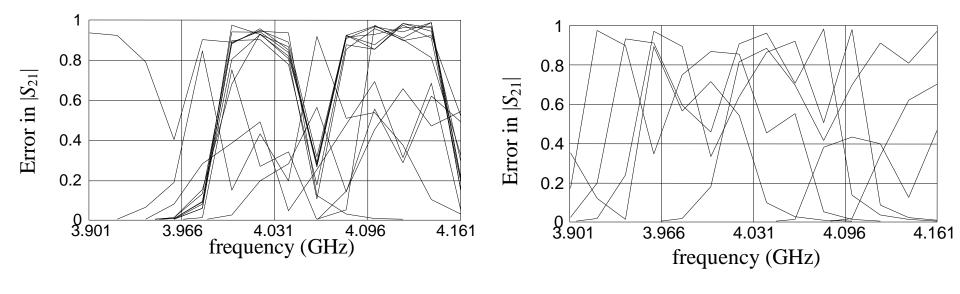
responses using  $em^{TM}(\bullet)$  and OSA90/hope<sup>TM</sup> (-) at three learning and three test points







#### HTS Coarse Model Error w.r.t. *em*<sup>™</sup> before any Neuromodeling



in the learning set

in the testing set

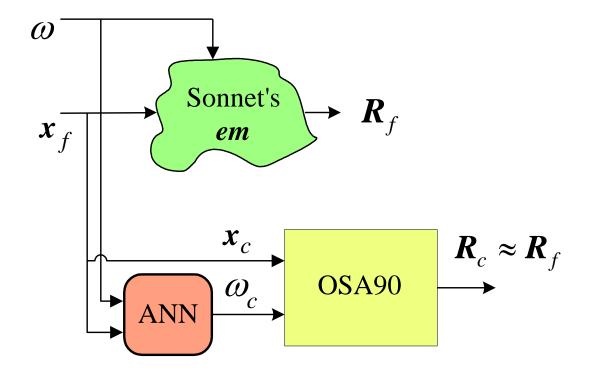
learning set: 13 base points with "star" distribution

testing set: 7 random base points in the region of interest (not seen in the learning set)





#### FM Neuromodel for the HTS Filter (3LP:7-5-1)



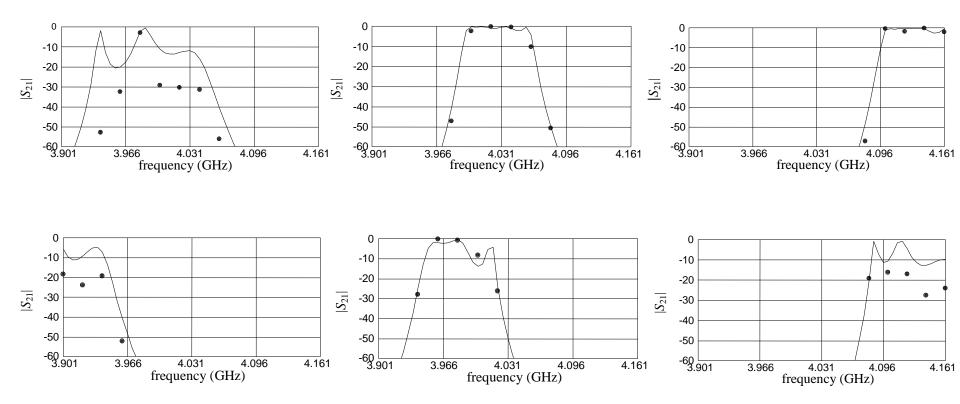
 $\boldsymbol{x}_{f} = [L_{1} \ L_{2} \ L_{3} \ S_{1} \ S_{2} \ S_{3}]^{T}$ 





#### FM Neuromodel for the HTS Filter (3LP:7-5-1)

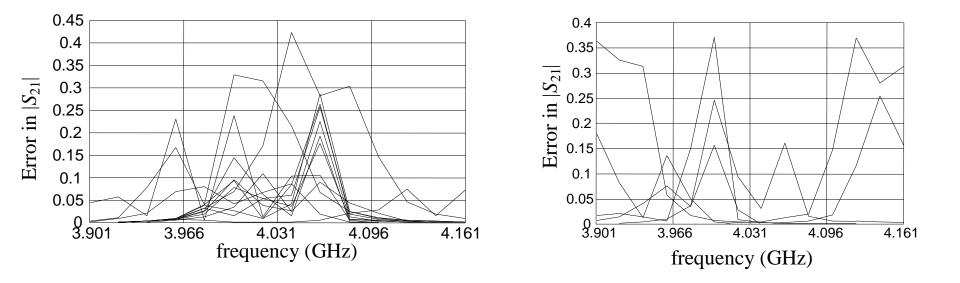
responses using  $em^{TM}(\bullet)$  and FMN model (-) at the three learning and three testing points







#### HTS FM Neuromodel Error w.r.t. em<sup>™</sup>



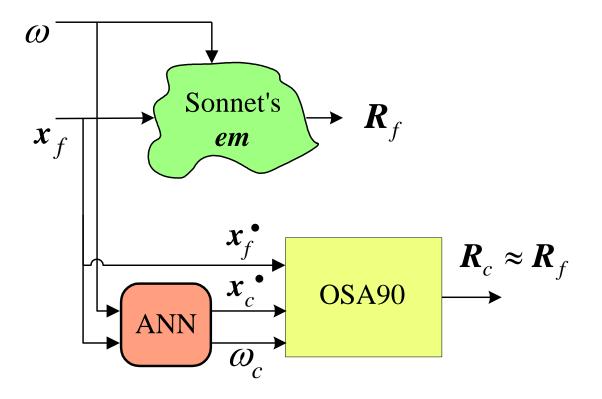
in the learning set

in the testing set





#### **FPSM Neuromodel for the HTS Filter (3LP:7-7-3)**



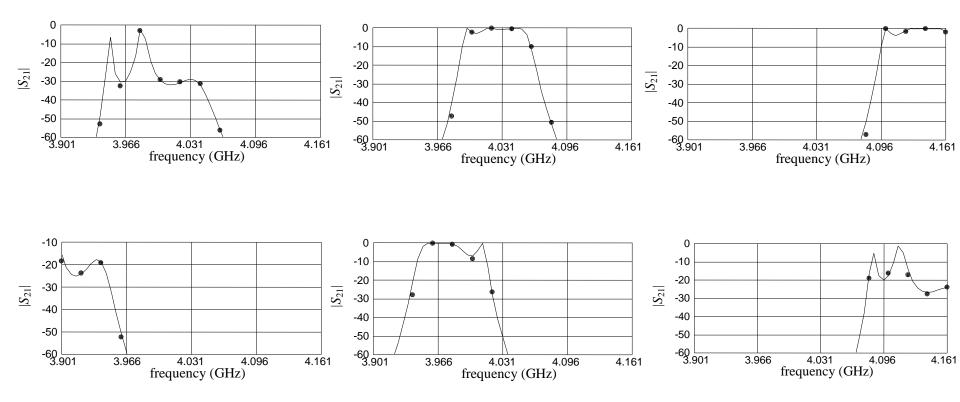
 $\boldsymbol{x}_{f} = [L_{1} \ L_{2} \ L_{3} \ S_{1} \ S_{2} \ S_{3}]^{T} \qquad \boldsymbol{x}_{f}^{\bullet} = [L_{2} \ L_{3} \ S_{2} \ S_{3}]^{T} \qquad \boldsymbol{x}_{c}^{\bullet} = [L_{1c} \ S_{1c}]^{T}$ 





#### **FPSM Neuromodel for the HTS Filter (3LP:7-7-3)**

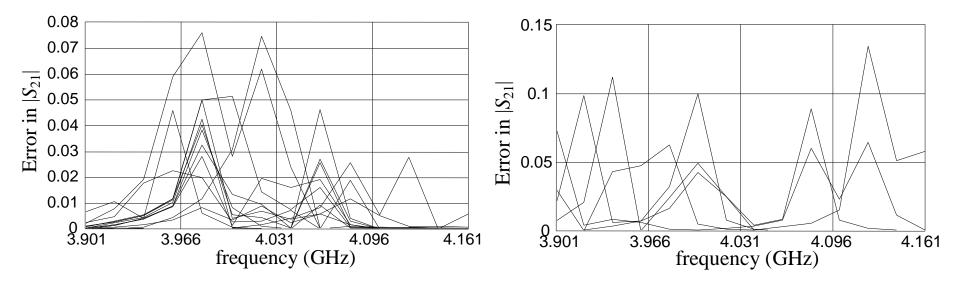
responses using  $em^{TM}(\bullet)$  and FPSMN model (-) at the three learning and three testing points







#### HTS FPSM Neuromodel Error w.r.t. *em*™



in the learning set

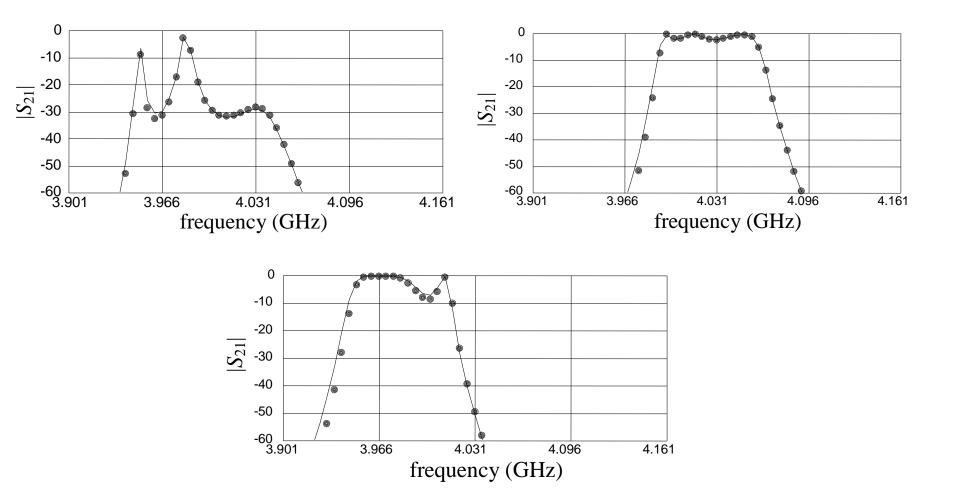
#### in the testing set





#### **FPSM Neuromodel for the HTS Filter: Fine Frequency Sweep Results**

comparison between  $em^{TM}(\bullet)$  and FPSMN model (-) at two learning and one testing points







(Bandler et al., 2000, 2001)

Neural Space Mapping (NSM) Optimization

**EM-based Statistical Analysis** 

**EM-based Yield Optimization** 





(Bandler et al., 2000, 2001)

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five powerful SM based neuromodeling techniques are described

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- improve generalization ability
- reduce complexity of the ANN topology

w.r.t. classical neuromodeling

frequency-sensitive neuromappings expand the usefulness of empirical quasi-static models





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