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SOS-00-16-V

June 2000

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presented at

2000 IEEE MTT-S International Microwave Symposium, Boston, MA, USA, June 15, 2000



Problem Definition

it is required to optimize a detailed or "fine" model of a microwave circuit

utilizing traditional direct optimization is not possible because of intensive simulation time

Space Mapping (SM) optimization exploits the existence of a coarse model of the circuit

we present a novel SM algorithm that integrates SM optimization and "surrogate model" optimization

the algorithm utilizes a surrogate model expressed as a convex combination between a mapped coarse model and a linearized fine model

we also present a novel approach for utilizing a frequencysensitive mapping

a number of examples illustrate the algorithm

Basic Definitions and Notation

n : number of designable parameters $\mathbf{x}_{f}^{(i)} \in \Re^{n \times 1}$: fine model design at the *i*th iteration $\mathbf{x}_{f} \in \Re^{n \times 1}$: a fine model point in the vicinity of $\mathbf{x}_{f}^{(i)}$, $\Delta \mathbf{x}_{f} = \mathbf{x}_{f} - \mathbf{x}_{f}^{(i)}$ $\mathbf{R}_{f}(\mathbf{x}_{f}, \omega) \in \Re^{N_{r} \times 1}$: fine model response vector at a point \mathbf{x}_{f} and frequency ω

 $\boldsymbol{\omega}$: set of simulation frequencies, where $\boldsymbol{\omega} \stackrel{\Delta}{=} \{ \omega_1, \omega_2, \dots, \omega_{N_{\omega}} \}$ $\boldsymbol{R}_f(\boldsymbol{x}_f) \in \Re^{m \times 1}$: fine model response vector at the point \boldsymbol{x}_f for all frequencies where $m = N_{\omega} N_r$

 $\boldsymbol{J}_{f}^{(i)} \in \Re^{m \times n}$: approximation to the Jacobian of fine model responses at the *i*th iteration

 $\boldsymbol{B}^{(i)}, \boldsymbol{s}^{(i)}, \boldsymbol{t}^{(i)}, \boldsymbol{\sigma}^{(i)}, \boldsymbol{c}^{(i)}$ and $\gamma^{(i)}$: the mapping parameters at the *i*th iteration

SM Optimization vs. Surrogate Model Optimization

the optimal fine model design \boldsymbol{x}_{f}^{*} is obtained by solving

$$\mathbf{x}_{f}^{*} = \arg \left\{ \min_{\mathbf{x}_{f}} U(\mathbf{R}_{f}(\mathbf{x}_{f})) \right\}$$

solving this problem using direct optimization methods can be prohibitive

SM optimization algorithms efficiently solve this design problem

they exploit the existence of a less accurate but fast coarse model of the circuit under consideration

a mapping $\mathbf{x}_c = \mathbf{P}(\mathbf{x}_f)$ is established between the two spaces such that $\mathbf{R}_f(\mathbf{x}_f) \approx \mathbf{R}_c(\mathbf{x}_c)$

the space-mapped design \overline{x}_f is a solution of the nonlinear system

$$\boldsymbol{f}(\boldsymbol{x}_f) = \boldsymbol{P}(\boldsymbol{x}_f) - \boldsymbol{x}_c^* = \boldsymbol{0}$$

the mapping $P(x_f)$ is approximated through Parameter Extraction (PE)



SM Optimization vs. Surrogate Model Optimization (Continued)

the ASM algorithm solves this problem using a quasi-Newton method

the TRASM algorithm integrates a trust region methodology with the ASM technique

surrogate model optimization approximates the fine model at the *i*th iteration by a surrogate model $\mathbf{R}_{s}^{(i)}(\mathbf{x}_{f}) \in \Re^{m \times 1}$

the step suggested is obtained by solving

$$\boldsymbol{h}^{(i)} = \arg\left\{\min_{\boldsymbol{h}^{(i)}} U(\boldsymbol{R}_{s}^{(i)}(\boldsymbol{x}_{f}^{(i)} + \boldsymbol{h}^{(i)}))\right\}, \left\|\boldsymbol{h}^{(i)}\right\| \leq \delta^{(i)}$$

 $\boldsymbol{h}^{(i)}$ is validated using fine model simulation

the accuracy of the surrogate model is improved in every iteration using the simulated fine model points

The Surrogate Model

our surrogate model is a convex combination of a mapped coarse model and a linearized fine model

the *i*th iteration surrogate model is

$$\boldsymbol{R}_{s}^{(i)}(\boldsymbol{x}_{f}) = \lambda^{(i)} \boldsymbol{R}_{m}^{(i)}(\boldsymbol{x}_{f}) + (1 - \lambda^{(i)})(\boldsymbol{R}_{f}(\boldsymbol{x}_{f}^{(i)}) + \boldsymbol{J}_{f}^{(i)} \Delta \boldsymbol{x}_{f}), \, \lambda^{(i)} \in [0, 1]$$

the mapped coarse model utilizes the frequency-sensitive mapping

$$\boldsymbol{R}_{f}(\boldsymbol{x}_{f},\omega_{j}) \approx \boldsymbol{R}_{m}^{(i)}(\boldsymbol{x}_{f},\omega_{j}) = \boldsymbol{R}_{c}(\boldsymbol{P}^{(i)}(\boldsymbol{x}_{f},\omega_{j}),\boldsymbol{P}_{\omega}^{(i)}(\boldsymbol{x}_{f},\omega_{j}))$$

where

$$\begin{bmatrix} \boldsymbol{P}^{(i)}(\boldsymbol{x}_f, \omega_j) \\ \boldsymbol{P}^{(i)}_{\omega}(\boldsymbol{x}_f, \omega_j) \end{bmatrix} = \begin{bmatrix} \boldsymbol{B}^{(i)} & \boldsymbol{s}^{(i)} \\ \boldsymbol{t}^{(i)T} & \boldsymbol{\sigma}^{(i)} \end{bmatrix} \begin{bmatrix} \Delta \boldsymbol{x}_f \\ \omega_j \end{bmatrix} + \begin{bmatrix} \boldsymbol{c}^{(i)} \\ \boldsymbol{\gamma}^{(i)} \end{bmatrix}$$

the parameters $\boldsymbol{B}^{(i)} \in \Re^{n \times n}$, $\boldsymbol{s}^{(i)} \in \Re^{n \times 1}$, $\boldsymbol{t}^{(i)} \in \Re^{n \times 1}$, $\boldsymbol{c}^{(i)} \in \Re^{n \times 1}$, $\boldsymbol{c}^{(i)} \in \Re^{n \times 1}$, $\boldsymbol{\sigma}^{(i)} \in \Re^{1 \times 1}$ and $\gamma^{(i)} \in \Re^{1 \times 1}$ are obtained such that the mapped coarse model approximates the fine model over a given set of fine model points $V^{(i)}$ and frequencies $\boldsymbol{\omega}$



The Surrogate Model (Continued)

the mapping parameters are obtained through the optimization process

$$[\boldsymbol{B}^{(i)}, \boldsymbol{s}^{(i)}, \boldsymbol{t}^{(i)}, \boldsymbol{\sigma}^{(i)}, \boldsymbol{c}^{(i)}, \boldsymbol{\gamma}^{(i)}] = \\ arg \begin{cases} \min_{\boldsymbol{B}, \boldsymbol{s}, \boldsymbol{t}, \boldsymbol{\sigma}, \boldsymbol{c}, \boldsymbol{\gamma}} \| & [\boldsymbol{e}_{1}^{T} & \boldsymbol{e}_{2}^{T} & \cdots & \boldsymbol{e}_{N_{p}}^{T}]^{T} \| \end{cases}$$

where

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{m}^{(i)}(\boldsymbol{x}_{f}^{(k)}) - \boldsymbol{R}_{f}(\boldsymbol{x}_{f}^{(k)}) \quad \forall \, \boldsymbol{x}_{f}^{(k)} \in V^{(i)}$$



The Motivation for Utilizing a Frequency-Sensitive Mapping

utilizing a frequency sensitive mapping makes the parameter extraction problem better conditioned





The Motivation for Utilizing a Frequency-Sensitive Mapping (Continued)

utilizing a frequency-sensitive mapping enables indirect estimation of fine model derivatives

the Jacobian of the mapped coarse model responses at a point $\mathbf{x}_{f}^{(k)}$ and frequency ω_{j} is given by

$$\begin{aligned} \boldsymbol{J}_{f}(\boldsymbol{x}_{f}^{(k)},\omega_{j}) &\approx \boldsymbol{J}_{m}(\boldsymbol{x}_{f}^{(k)},\omega_{j}) = \left(\frac{\partial \boldsymbol{R}_{m}^{T}(\boldsymbol{x}_{f},\omega)}{\partial \boldsymbol{x}_{f}}\right)^{T} \middle| &= \\ \boldsymbol{x}_{f} = \boldsymbol{x}_{f}^{(k)} \\ \boldsymbol{\omega} = \boldsymbol{\omega}_{j} \end{aligned}$$
$$\left(\frac{\partial \boldsymbol{P}^{T}}{\partial \boldsymbol{x}_{f}} \frac{\partial \boldsymbol{R}_{c}^{T}(\boldsymbol{P},\boldsymbol{P}_{\omega})}{\partial \boldsymbol{P}} + \frac{\partial \boldsymbol{P}_{\omega}}{\partial \boldsymbol{x}_{f}} \frac{\partial \boldsymbol{R}_{c}^{T}(\boldsymbol{P},\boldsymbol{P}_{\omega})}{\partial \boldsymbol{P}_{\omega}}\right)^{T} \middle| \boldsymbol{P} = \boldsymbol{P}^{(i)}(\boldsymbol{x}_{f}^{(k)},\omega_{j}) \\ \boldsymbol{P}_{\omega} = \boldsymbol{P}_{\omega}^{(i)}(\boldsymbol{x}_{f}^{(k)},\omega_{j}) \end{aligned}$$

. .

Updating the Trust Region Size

predicted reduction in the objective function

$$r_p = U(\mathbf{R}_s^{(i)}(\mathbf{x}_f^{(i)})) - U(\mathbf{R}_s^{(i)}(\mathbf{x}_f^{(i)} + \mathbf{h}^{(i)}))$$

actual reduction in the objective function

$$r_a = U(\boldsymbol{R}_f(\boldsymbol{x}_f^{(i)})) - U(\boldsymbol{R}_f(\boldsymbol{x}_f^{(i)} + \boldsymbol{h}^{(i)}))$$

define $\rho = \frac{r_a}{r_p}$

if
$$\rho \ge 0.75$$
, let $\delta^{(i+1)} = \pi_1 \delta^{(i)}, \pi_1 > 1.0$

if $\rho \le 0.10$, let $\delta^{(i+1)} = \pi_2 \delta^{(i)}, 0 < \pi_2 < 1.0$

Updating the Surrogate Parameter

the mapped coarse model error

$$\boldsymbol{E}_{m}^{(i)} = \boldsymbol{R}_{m}^{(i)}(\boldsymbol{x}_{f}^{(i)} + \boldsymbol{h}^{(i)}) - \boldsymbol{R}_{f}(\boldsymbol{x}_{f}^{(i)} + \boldsymbol{h}^{(i)})$$

the linearized fine model error

$$\boldsymbol{E}_{l}^{(i)} = \boldsymbol{R}_{f} \left(\boldsymbol{x}_{f}^{(i)} \right) + \boldsymbol{J}_{f}^{(i)} \boldsymbol{h}^{(i)} - \boldsymbol{R}_{f} \left(\boldsymbol{x}_{f}^{(i)} + \boldsymbol{h}^{(i)} \right)$$

the surrogate model parameter update is given by

$$\lambda^{(i+1)} = \frac{\left\|\boldsymbol{E}_{l}^{(i)}\right\|}{\left\|\boldsymbol{E}_{l}^{(i)}\right\| + \left\|\boldsymbol{E}_{m}^{(i)}\right\|} \text{ if } \left\|\boldsymbol{E}_{l}^{(i)}\right\| \le \varepsilon_{l} \text{ otherwise } \lambda^{(i+1)} = 1$$

The Stopping Criterion

the algorithm terminates if the step size becomes sufficiently small or if the algorithm fails to make any progress for n+1 consecutive iterations



Illustration of One Iteration of the Algorithm



- r_p = predicted reduction in the objective function using the surrogate model
- r_a = actual reduction in the objective function

The Algorithm

Step 1. Given $\mathbf{x}_{f}^{(1)} = \mathbf{x}_{c}^{*}$, $\lambda^{(1)} = 1$, $\delta^{(1)}$, α , $\mathbf{J}_{f}^{(1)} = \mathbf{J}_{c}^{*}$ and i=1

Step 2. Construct $V^{(i)}$

Step 3. Obtain the mapping parameters through optimization

Step 4. Obtain the suggested step $\boldsymbol{h}^{(i)}$ using the surrogate model

- Step 5. If $U(\mathbf{R}_f(\mathbf{x}_f^{(i)} + \mathbf{h}^{(i)})) < U(\mathbf{R}_f(\mathbf{x}_f^{(i)}))$, set $\mathbf{x}_f^{(i+1)} = \mathbf{x}_f^{(i)} + \mathbf{h}^{(i)}$ else $\mathbf{x}_f^{(i+1)} = \mathbf{x}_f^{(i)}$
- Step 6. Update $\boldsymbol{J}_{f}^{(i)}$, $\delta^{(i)}$ and $\lambda^{(i)}$

Step 7. If the stopping criterion is satisfied stop

Step 8. Set i=i+1 and go to Step 2



The Algorithm Flowchart





Two-Section 10:1 Capacitively-Loaded Impedance Transformer (*Bandler*, 1969)

"fine model"



"coarse model"





design specifications are

 $|S_{11}| \le 0.50$ for $0.5 \text{ GHz} \le \omega \le 1.5 \text{ GHz}$

the designable parameters are the electrical lengths of the two transmission lines at $\omega = 1.0 \text{ GHz}$

the characteristic impedances are kept fixed at their optimal values

both the coarse and fine models make use of the ideal transmission line model available in OSA90/hope

eleven frequency points are simulated per sweep

five iterations are executed (only two successful)

number of fine model simulations is seven

the real and imaginary parts of S_{11} are used in extracting the mapping parameters

initial trust region size is $\delta^{(1)} = 0.09 \| \boldsymbol{x}_c^* \|_{\infty}$

the extraction radius is $\alpha = 0.09 \| \mathbf{x}_c^* \|_{\infty}$



the final mapping

$$\boldsymbol{B}^{(6)} = \begin{bmatrix} 1.12886 & 0.19245 \\ -0.17669 & 1.19167 \end{bmatrix}, \ \boldsymbol{c}^{(6)} = \begin{bmatrix} 84.52643 \\ 87.95123 \end{bmatrix},$$
$$\boldsymbol{s}^{(6)} = \begin{bmatrix} -0.06863 \\ 0.06035 \end{bmatrix}, \ \boldsymbol{t}^{(6)} = \begin{bmatrix} -0.00026 \\ -0.00212 \end{bmatrix}, \ \boldsymbol{\sigma}^{(6)} = 1.03243,$$
$$\boldsymbol{\gamma}^{(6)} = 0.00983 \text{ and } \boldsymbol{\lambda}^{(6)} = 0.58473$$

Parameter	$oldsymbol{x}_{f}^{(1)}$	$oldsymbol{x}_{f}^{(2)}$	$x_{f}^{(3)}$	
L_1	90.0000	81.9000	81.59880	
L_2	90.0000	81.9000	74.38324	
all values are in degrees				



the initial design



the second design



00-16-18



the final design





the objective function in each iteration



The Double-Folded Stub Filter

(*Rautio*, 1992)

the fine model utilizes Sonnet's em



the coarse model exploits the microstrip line and microstrip Tjunction models available in OSA90/hope

the coupling between the folded stubs and the microstrip line is simulated using equivalent capacitors

the values of these capacitors are determined using Walker's formulas (*Walker et al.*, 1990)

Jansen's microstrip bend model is used to model the folding effect of the stub (*Jansen et al.*, 1983)



The Double-Folded Stub Filter (Continued)

the coarse model



design specifications are

 $|S_{21}| \ge -3$ dB for $\omega \le 9.5$ GHz and 16.5 GHz $\le \omega$

 $|S_{21}| \le -30 \text{ dB}$ for $12 \text{ GHz} \le \omega \le 14 \text{ GHz}$

designable parameters are L_1 , L_2 and S

 W_1 and W_2 are fixed at 4.8 mil

the real and imaginary parts of S_{21} are used in extracting the mapping parameters

The Double-Folded Stub Filter (Continued)

eleven frequency points per sweep are utilized

initial trust region size is $\delta^{(1)} = 0.09 \| \boldsymbol{x}_c^* \|_{\infty}$

extraction radius is $\alpha = 0.09 \| \boldsymbol{x}_c^* \|_{\infty}$

the width is scaled by a factor of 6.0 to make the problem better conditioned

the interpolation option of Empipe is disabled for this example



The Double-Folded Stub Filter Results

the grid size used is 1.6 mils for each parameter

the algorithm required 11 successful iterations (16 total iterations) with a total of 18 calls to Empipe (18 *em* simulations)

$$\boldsymbol{B}^{(17)} = \begin{bmatrix} 1.03074 & 0.11174 & 0.00031 \\ -0.20595 & 0.96384 & 0.00365 \\ -0.35144 & 0.34204 & 0.78257 \end{bmatrix}, \ \boldsymbol{c}^{(17)} = \begin{bmatrix} 236.1134 \\ 21.5218 \\ 74.8218 \end{bmatrix}, \\ \boldsymbol{s}^{(17)} = \begin{bmatrix} 0.44639 \\ 0.70939 \\ 0.50045 \end{bmatrix}, \ \boldsymbol{t}^{(17)} = \begin{bmatrix} 0.03854 \\ -0.01167 \\ 0.00439 \end{bmatrix}, \ \boldsymbol{\sigma}^{(17)} = 1.13771, \\ \end{bmatrix}$$

$$\gamma^{(17)} = -0.55168$$
 and $\lambda^{(17)} = 0.03526$

Parameter	$oldsymbol{x}_{f}^{(1)}$	${m x}_{f}^{(17)}$		
S	9.60	6.4		
L_2	60.80	84.8		
L_1	67.2	86.4		
all values are in mil				



The Double-Folded Stub Filter Results (Continued)

initial response



final response





The Double-Folded Stub Filter Results (Continued)

the objective function in each iteration



The HTS Filter

(Bandler et al., 1995)



design specifications are

 $|S_{21}| \le 0.05$ for $\omega \le 3.967$ GHz and 4.099 GHz $\le \omega$ $|S_{21}| \ge 0.95$ for 4.008 GHz $\le \omega \le 4.058$ GHz

designable parameters are L_1 , L_2 , L_3 , S_1 , S_2 and S_3

we take $L_0 = 50$ mil and W = 7 mil

the coarse model exploits the empirical models of microstrip lines, coupled lines and open stubs available in OSA90/hope

the fine model employs Sonnet's em through Empipe



The HTS Filter (Continued)

the coarse model



the real and imaginary parts of both S_{11} and S_{21} are utilized in extracting the mapping parameters

the initial trust region is $\delta^{(1)} = 0.20 \| \boldsymbol{x}_c^* \|_{\infty}$

the interpolation option of Empipe is disabled to make the optimization time reasonable



The HTS Filter (The First Case)

the problem is solved for two different cases

first, the substrate is assumed lossless and a relatively coarse grid size is used (1.0mil×1.75mil)

the fine model is simulated at 16 frequency points per sweep

starting from the snapped optimal coarse design, the final design is reached in 7 iterations only

a total of 7 fine model simulations are used



The HTS Filter (The First Case)

the initial and final response of the fine model





The HTS Filter (The First Case)

the fine model response at the end of the first iteration



the objective function in every iteration





The HTS Filter (The Second Case)

the problem is resolved assuming a lossy substrate (loss tangent=3.0e-5) and a finer grid (1.0mil×1.0mil)

the fine model is simulated at 9 frequency points per sweep

starting from the snapped optimal coarse design, the final design is reached in 4 iterations only

a total of 5 fine model simulations are used



The HTS Filter (The Second Case)

the final fine model response



the objective function in each iteration





Conclusions

we present a novel SM optimization algorithm for microwave circuits

SM optimization is formulated as a general optimization problem of a surrogate model

the surrogate model utilized is a convex combination of a linearized fine model and a mapped coarse model

we also integrated, for the first time, a linearized frequencysensitive mapping with SM optimization

frequency-sensitive mappings make the parameter extraction problem better conditioned

the algorithm is illustrated through a number of examples

the new SMX system incorporates our results

