# SOFTWARE IMPLEMENTATION OF SPACE MAPPING BASED NEUROMODELS OF MICROWAVE COMPONENTS

J.W. Bandler, J.E. Rayas-Sánchez and Q.J. Zhang\*

Simulation Optimization Systems Research Laboratory and Department of Electrical and Computer Engineering McMaster University, Hamilton, Canada L8S 4K1

\* Department of Electronics Carleton University, Ottawa, Canada K1S 5B6

> bandler@mcmaster.ca www.sos.mcmaster.ca



presented at

2000 Micronet Annual Workshop, Ottawa, ON, April 28, 2000

# **Artificial Neural Networks (ANN) in Modeling**

Artificial Neural Networks are suitable in modeling highdimensional and highly nonlinear problems

ANN models are computationally efficient and can be more accurate than empirical models

multilayer feedforward networks can approximate any measurable function to any desired level of accuracy, provided a deterministic relationship between input and target exists (*White et al.*, 1992)

ANNs that are too small cannot approximate the desired inputoutput relationship

ANNs with too many internal parameters perform correctly in the learning set, but give poor generalization ability

ANNs are suitable models for microwave circuit optimization and statistical design (Zaabab, Zhang and Nakhla, 1995, Gupta et al., 1996, Burrascano and Mongiardo, 1998, 1999)

Space Mapping-based neuromodeling techniques significantly decrease the number of EM simulations needed for training (*Bandler et al.*, 1999)



# **Conventional Neuromodeling of Microwave Components**



many learning samples are usually needed to ensure model accuracy

the number of learning samples needed to approximate a function grows exponentially with the ratio of the dimensionality to the function's degree of smoothness (*Stone, 1982*)

even with sufficient training data, the reliability of MLPs for extrapolation may be very poor



# The Aim of Space Mapping

(Bandler et al., 1994-)





# **Neural Space Mapping**

$$x_f \longrightarrow P(x_f) \longrightarrow x_c \qquad x_f \longrightarrow ANN \longrightarrow x_c$$

using a three layer perceptron (3LP)





# Space Mapped Neuromodeling (SMN) Concept



once the ANN is trained





# **Frequency-Dependent Space Mapped Neuromodeling** (FDSMN) Concept



once the ANN is trained





### **Frequency Space Mapped Neuromodeling (FSMN) Concept**



once the ANN is trained





### **Frequency Mapped Neuromodeling (FMN) Concept**



once the ANN is trained





# **Frequency Partial-Space Mapped Neuromodeling** (**FPSMN**) **Concept**



once the ANN is trained





# **Training the ANN**

the neuromapping can be found by solving the optimization problem

$$\min_{\boldsymbol{w}} \| [\boldsymbol{e}_1^T \quad \boldsymbol{e}_2^T \quad \cdots \quad \boldsymbol{e}_l^T]^T \|$$

*w* contains the internal parameters of the ANN (weights, bias, etc.) selected as optimization variables

*l* is the total number of learning samples

 $e_k$  is the error vector given by

for SMN

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f_{i}}, freq_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{c}, freq_{j})$$

 $\boldsymbol{x}_{c} = \boldsymbol{P}\left(\boldsymbol{x}_{f_{i}}\right)$ 

for FDSMN

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f_{i}}, freq_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{c}, freq_{j})$$

$$\boldsymbol{x}_{c} = \boldsymbol{P}\left(\boldsymbol{x}_{f_{i}}, freq_{j}\right)$$

for FSMN

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f_{i}}, freq_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{c}, f_{c})$$



# Training the ANN (continued)

$$\begin{bmatrix} \boldsymbol{x}_c \\ f_c \end{bmatrix} = \boldsymbol{P}\left(\boldsymbol{x}_{f_i}, freq_j\right)$$

for FMN

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f_{i}}, freq_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{f_{i}}, f_{c})$$
$$f_{c} = P(\boldsymbol{x}_{f_{i}}, freq_{j})$$

for FPSMN

$$\boldsymbol{e}_{k} = \boldsymbol{R}_{f}(\boldsymbol{x}_{f_{i}}, freq_{j}) - \boldsymbol{R}_{c}(\boldsymbol{x}_{f_{i}}^{s}, \boldsymbol{x}_{c}^{s}, f_{c})$$

$$\begin{bmatrix} \boldsymbol{x}_{c}^{s} \\ f_{c} \end{bmatrix} = \boldsymbol{P}\left(\boldsymbol{x}_{f_{i}}, freq_{j}\right)$$

with

$$i = 1, \dots, B_p$$
$$j = 1, \dots, F_p$$
$$k = j + F_p (i - 1)$$

# Simulation Optimization Systems Research Laboratory McMaster University

# **Starting Point and Learning Samples**

we chose a unit mapping ( $x_c \approx x_f$  and  $f_c \approx freq$ ) as the starting point for the optimization problem

to keep a reduced set of learning data samples, we consider an *n*-dimensional star distribution for the learning base points (*Bandler et al.*, 1989)

the number of learning base points for a microwave circuit with n design parameters is  $B_p = 2n + 1$ 





# **Microstrip Right Angle Bend**



region of interest

 $\begin{array}{l} 20\text{mil} \leq W \leq 30\text{mil} \\ 8\text{mil} \leq H \leq 16\text{mil} \\ 8 \leq \varepsilon_{\mathrm{r}} \leq 10 \\ 1\text{GHz} \leq freq \leq 41\text{GHz} \end{array}$ 

"coarse" model: Gupta model (Gupta, Garg and Bahl, 1979)

"fine" model: Sonnet's *em*<sup>TM</sup>

learning set: 7 base points with "star" distribution

testing set: 50 random base points in the region of interest



## **Microstrip Right Angle Bend Response Errors**

comparison before neuromodeling between  $em^{TM}$  and Gupta model at 50 random test points





# FSMN Model for the Right Angle Bend (3LP:4-8-4)

strategy implemented in NeuroModeler





### FSMN Model for the Right Angle Bend (3LP:4-8-4)

implementation in NeuroModeler Version 1.2b (1999)



# **Implementation in** *NeuroModeler*

layer one, in green, has the input parameters of the neuromapping (*W*, *H*,  $\varepsilon_r$ , and *freq*) scaled to  $\pm 1$ 

layer two corresponds to the hidden layer of the ANN implementing the mapping (8 hidden neurons with sigmoid nonlinearities)

layer three is linear and contains the coarse design parameters  $x_c$ and the mapped frequency  $f_c$  before de-scaling

layer four de-scales the parameters

Gupta's formulas to calculate *L* and *C* are programmed as the internal analytical functions of the fifth hidden layer, using the built-in MultiSymbolicFixed function

the output layer, in blue, contains a simple internal circuit simulator that computes the real and imaginary parts of  $S_{11}$  and  $S_{21}$  for the lumped LC equivalent circuit (this layer uses the built-in CktSimulatorPS function)



### FSMN Model Results for the Right Angle Bend

errors in the learning set after training (w.r.t.  $em^{TM}$ )





# FSMN Model Results for the Right Angle Bend

errors in the testing set after training (w.r.t. *em*<sup>TM</sup>)





# FSMN Model Results for the Right Angle Bend

## comparison between $em^{TM}$ and the FSMN model





# Conclusions

we present novel realizations of Space Mapping based neuromodels of practical passive microwave components using available software

five powerful SM based neuromodeling techniques are described

these techniques

exploit the vast set of empirical models already available decrease the fine model evaluations needed for training improve generalization ability reduce complexity of the ANN topology w.r.t. the classical neuromodeling approach

frequency-sensitive neuromappings expand the usefulness of empirical quasi-static models

an SM based neuromodel of a microstrip right angle bend is implemented using *NeuroModeler* Version 1.2b (1999)

this model can be entered into Agilent ADS Version 1.1 (1999) as a library component through an ADS plugin module



#### **New Results**

M.H. Bakr, J.W. Bandler, M.A. Ismail, J.E. Rayas-Sánchez and Q.J. Zhang, "Neural space mapping optimization of EM microwave structures," *IEEE MTT-S Int. Microwave Symp. Digest* (Boston, MA), 2000.

M.H. Bakr, J.W. Bandler, K. Madsen, J.E. Rayas-Sánchez and J. Søndergaard, "Space mapping optimization of microwave circuits exploiting surrogate models," *IEEE MTT-S Int. Microwave Symp. Digest* (Boston, MA), 2000.

J.W. Bandler, M.A. Ismail and J.E. Rayas-Sánchez, "Broadband physics-based modeling of microwave passive devices through frequency mapping," *IEEE MTT-S Int. Microwave Symp. Digest* (Boston, MA), 2000.

J.W. Bandler, J.E. Rayas-Sánchez, M.A. Ismail and M.H. Bakr, "Space mapping based device modeling and circuit optimization," *IEEE MTT-S Int. Microwave Symp.*, Workshop WFF (Boston, MA), 2000.