Impact of porosity and velocity on the dissolution behaviors of calcium aluminate inclusions in CaO-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> steelmaking slag: in-situ observations and model advancements

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### Abstract:

The dissolution process of CaO·2Al<sub>2</sub>O<sub>3</sub> (CA2) particles in CaO-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> steelmaking slags was in-situ investigated at 1550°C. To better understand the role of particle porosity in dissolution kinetics, the particles with two different porosity levels, i.e., 0.08 and 0.20 were used in this study. The porosity ( $\varphi$ ) and surface area of CA2 particles were characterized through X-ray Computed Tomographic Imaging (XCT), and the surface area ratio ( $f(\varphi)$ ) between the porous and full dense particles was expressed as  $f(\varphi) = 0.9398e^{5.9498\varphi}$ . The obtained results indicated that an increase in the porosity from 0.08 to 0.20 led to an increase in the average dissolution rate from 0.35 to 0.59 µm/s. Moreover, the motion of CA2 particles during the dissolution process was observed, suggesting its importance to include in the modeling approach. A novel mathematical model was developed to predict the dissolution time of inclusion particles by incorporating both the motion and porosity of particles. This model was validated against the existing literature data and aligned well with the current experimental findings. The model predictions demonstrated that the dissolution time of CA2 particles was decreased with an increase in the velocity and porosity of particles and concentration difference of dissolving species between particle–slag interface and molten slag ( $\Delta C$ ), and a decrease in slag viscosity.

**Keywords**: dissolution mechanism models, calcium aluminate inclusion, particle velocity, particle porosity, in-situ observation

#### 1 Introduction

Particle motion and dissolution behavior are widely investigated in both engineering and scientific applications. One of their vital applications in metallurgy is the control of steel cleanliness, where the dissolution process of non-metallic inclusions, referred to as "NMIs" herein, plays a critical role.[1] Once the NMIs enter the slag phase, they are expected to be dissolved in the molten slag as rapidly as possible. Any NMIs that remain as the undissolved particle may re-entrain into the molten steel, posing a significant industrial risk. They may agglomerate or coalesce, leading to clogging of the submerged entry nozzle, thus compromising product quality and production efficiency.

The dissolution mechanisms and kinetics of NMIs in slags have been well studied through experiments[2-4] and simulations[5-8] to support optimization of their removal efficiency from liquid steel during secondary refining of steelmaking. In the past two decades, in-situ observation via High Temperature Confocal Laser Scanning Microscopy (HT-CLSM) [9-14], and Single Hot Thermocouple Technique (SHTT) [15, 16], are the most common experimental methods used to investigate the dissolution process of NMIs. These techniques allow for real-time in-situ observation of the dissolution behavior of micron-size particles in molten slags. The main advantages of HT-CLSM to STHH are 1) image quality, 2) experimental temperature maintenance, 3) reduced particle/slag mass ratio. [17] This third point is particularly important since high particle/slag mass ratio (>1.0 wt. %) could cause the change of slag composition and properties during the particle dissolution process. [10, 18] The STHH typically employs a particle/slag mass ratio at around 5 wt. % magnification, significant exceeding 1 wt. %. [16, 19, 20] In contrast, the particle/slag ratio used in HT-CLSM is less than 0.5 wt%. [11, 21]

The NMIs' size evolution with time, recorded by CCD camera (HT-CLSM), generates a dissolution profile that can be used to validate models of dissolution mechanisms. **Table 1** summarizes prior literature on the dissolution of NMIs in steelmaking slags via HT-CLSM. In these studies, however, it has been assumed that (1) the NMIs are non-porous particles, and (2) solute transfer related to NMI motion can be ignored. However, it is unlikely that NMIs are fully dense given the fact that, after they form within the liquid steel, they undergo growth by coalescence and agglomeration. Moreover, as listed in **Table 1**, the motion and rotation of NMIs have been observed in many studies but their impacts on the kinetics have not been adequately included

within relevant dissolution mechanism models.

Previous investigations have primarily focused on the dissolution mechanisms and/or kinetics of Al<sub>2</sub>O<sub>3</sub> [2, 4, 9, 12, 14, 22-34], MgO [12, 22, 24, 25, 35], CaO[13, 36], SiO<sub>2</sub> [10, 21, 37], ZrO<sub>2</sub> [25, 27], MgAl<sub>2</sub>O<sub>4</sub> [22, 25, 27, 38], TiO<sub>2</sub>·Al<sub>2</sub>O<sub>3</sub> [4, 39] and CaO·2Al<sub>2</sub>O<sub>3</sub> (CA2) [11] in the ternary CaO-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> based slag systems at temperatures ranging from 1250 to 1600°C, and for particle sizes that vary between 50 and 500 μm. The obtained findings indicate that the dissolution kinetics of NMIs are enhanced with increasing temperature and the concentration difference of dissolving species between the NMI-slag interface and bulk slag (i.e., the driving force (Δ*C*)). However, dissolution kinetics are diminished with an increasing slag viscosity [9, 21, 23, 28, 29, 35, 36]. It has also been reported that the dissolution rate of Al<sub>2</sub>O<sub>3</sub> inclusions is increased using slags with high ratios of CaO/Al<sub>2</sub>O<sub>3</sub> or CaO/SiO<sub>2</sub> [2, 23, 33].

A widely accepted approach for modeling the dissolution mechanism of NMIs in molten slag is the application of the so-called shrinking core model [40]. In this model, the limiting step for NMI dissolution is categorized as either chemical reaction (CR) control or boundary layer diffusion (BLD) control [40]. A separate approach, known as diffusion in a stagnant fluid model (DS), has also been used to interpret the dissolution mechanism of NMIs [41]. The dissolution profiles for CR, BLD, and DS, after dimensionless treatment, exhibit a unique profile shape: linear for CR, parabolic for BLD, and sigmoidal for DS. The actual dissolution mechanism of an NMI can be determined by comparing the models' prediction with the experimental dissolution curve. For instance, if the normalized experimental dissolution curve is parabolic, then the dissolution mechanism of NMI is believed to be BLD. As tabulated in Table 1, prior researchers have primarily identified either BLD or DS as the main mechanisms controlling particle dissolution. Only a few studies[24, 25] have reported CR as the limiting step, and even fewer[23] reported mixed control as the limiting step (i.e. CR + BLD, indicating the formation of a solid product layer during dissolution). Nevertheless, it is not uncommon for different researchers to identify varying dissolution mechanisms for similar particle/slag systems. For example, Monaghan et al. reported that BLD was the limiting step for Al<sub>2</sub>O<sub>3</sub> particles in the CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> slag system, while DS was reported by Ren et al. [33, 34] in a similar slag system with slight compositional differences.

NMIs have been observed to not only dissolve but also to move, rotate, and dissociate within the molten slag during dissolution, as schematically illustrated in **Fig. 1**. Such phenomena could significantly impact dissolution mechanisms and kinetics by altering the fluid dynamics at the oxide-slag boundary, resulting in the shape change of the experimental dissolution curve [23, 35, 42].

Unfortunately, none of CR, BLD, and DS account for the motion of NMIs, which may explain the differences between the experimental and model prediction results [28, 35]. Pan et al. [42] incorporated the velocity of NMIs via the Péclet number to consider the convective mass transfer of the dissolving component. A better fit was obtained between model predictions and experimental results. However, the velocity was calculated based on the rotation of the NMIs, which normally only occurs for a specified duration and not over the entire dissolution process. As a result, the fixed angular velocity likely does not accurately represent the true velocity over time.

Another factor beyond NMI motion that must be considered is the porosity of NMIs. Since inclusion agglomeration occurs during industrial operations, the morphology of such agglomerated inclusions has been well studied, showing that they have porosity.[43, 44] For example, Yin et al. [45] observed that solid calcium aluminate inclusions were irregular in shape with coarse tips and pores.

The removal efficiency of NMIs from liquid steel during the refining process highly depends on their dissolution mechanisms and kinetics. Therefore, a better understanding of these processes requires investigating how the motion and porosity of NMIs affect their dissolution behaviors. Advancing conventional models to incorporate these factors will enable a more accurate determination of the dissolution mechanisms and prediction of the dissolution time of NMIs. In this study, the dissolution of CaO·2Al<sub>2</sub>O<sub>3</sub> (CA2) particles was examined via HT-CLSM within synthesized CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> metallurgical slag. Prior to experimentation, X-ray computed tomography (XCT) was used to quantify the porosity and surface area of the investigated CA2 particles. The results were used to develop a novel model that incorporates NMI motion and porosity on dissolution kinetics.

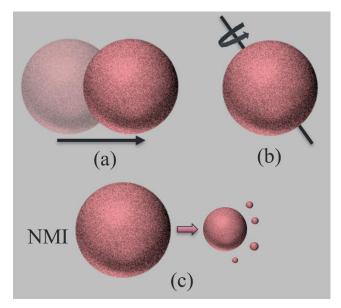


Figure 1. Potential NMI behavior during dissolution: (a) motion, (b) rotation, and (c) dissociation

Table 1 Summary of literature on the dissolution of NMIs in various slag systems using HT-CLSM

	1 a01	C I Sullill	iary or meratur	c on the dissor	ution of Mivits III various stag systems	using III-CLSM	
Authors	year	T (°C)	NMI	Slag system	Observed NMI behavior	Identified Rate limiting step	D*10 <sup>-10</sup> (m <sup>2</sup> /s)
Sridhar et al.[9]	2000	1450- 1550	$Al_2O_3$	CASM	Rotation, dissociation	BLD	
Valdez et al.[22, 23]	2001	1470- 1550	$Al_2O_3$	CASM	Rotation, the interface became smooth	mixed BLD + CR	
			MgO	CASM	morphology change, the interface became smooth	BLD	
			$MgAl_2O_4$	CASM	morphology change Rotation (20-40s), product layer on	mixed BLD + CR	
	2002	1470- 1530	$Al_2O_3$	CAS-(M)	particle surface in CASM slag. A smooth interface formed between CAS slag and particle	mixed CR + BLD	
Yi et al.[24]	2003	1450- 1500	MgO	CAM	Motion, rotation	CR	
			$Al_2O_3$	CAM		DS	
Fox et al.[25]	2004	1250- 1500	$Al_2O_3$	CASMNLB	Motion, rotation	CR	
			$ZrO_2$	CASMNLB	Rotation, particle became transparent, smooth interface		
			${ m MgO} \ { m MgAl_2O_4}$	CASMNLB CASMNLB	Motion, rotation Motion, rotation		
Monaghan et	2004	1477- 1577	$Al_2O_3$	CAS	Motion, rotation	BLD	0.15-3.09
al.[26-28, 38]	2005	1477- 1577	$Al_2O_3$	CAS	Motion, rotation		
			$MgAl_2O_4$	CAS	Motion and motion		
			ZrO2	CAS	Gas bubbles generated around the particle		
	2005	1477- 1577	$Al_2O_3$	CAS	Motion, rotation	BLD	0.15-3.09
	2006	1504	$MgAl_2O_4$	CAS	Rotation	BLD	0.67-2.20
Park et al.[12]	2006	1550	$Al_2O_3$	CAS	Motion		
			MgO	CAS	Motion		
Liu et al.[29, 35]	2007	1500, 1600	MgO	CASM	Rotation (38-46s), detachment, particle became transparent, product layer	BLD	
	2007	1470- 1630	$Al_2O_3$	CAS	Motion	DS	0.24-0.97

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Verhaeghe et al.[30, 31]	2007	1600	$Al_2O_3$	CAS	Motion, slight rotation	DS	0.27-0.42
. , ,	2008		$Al_2O_3$	CAS	motion	DS	0.22-0.28
Guo et al.[13, 36]	2013	1480	CaO	CAS-(M)	Rotation, motion, and product layer on the particle surface	Mixed control (CR+ BLD+PLD)	0.2-1.0
	2014	1450- 1600	CaO	CAS-(M)	Rotation, generation of gas bubble from the particle	Formation of the IR layer	0.20-1.00
Feichtinger et al.[10]	2014	1450	$SiO_2$	CAS	Rotation, motion	Revised DS	0.38-2.40
Michelic et al.[32]	2016	1600	Al <sub>2</sub> O <sub>3</sub>	CASM	Rotation, motion	DS	0.04-33.80
Miao et al.[11]	2018	1500- 1600	CaO·2Al <sub>2</sub> O <sub>3</sub>	CAS	Rotation, motion	BLD	0.06-5.8
Sharma et al.[4]	2018	1550	Al <sub>2</sub> TiO <sub>5</sub>	CAS	Motion, rotation, color change from opaque to transparent	BLD	1-100
Tian et al.[37]	2018	1473- 1573	$SiO_2$	CAS/CASM	Interface becomes smooth	Revised DS	0.25-0.55
Sharma et al.[39]	2020	1500	Al <sub>2</sub> TiO <sub>5</sub>	CAS	Slight motion, rotation	BLD	18-28 (Al <sub>2</sub> O <sub>3</sub> ), 25-38(TiO <sub>2</sub> )
Ren et al.[21, 33, 34]	2021	1450- 1580	$Al_2O_3$	CAS	Dissociation for some particles	DS	0.047-1.1
-	2022	1520- 1570	$SiO_2$	CASM		DS	1.0-10.0
	2023	1500- 1600	$Al_2O_3$	CAS		DS	2.8-4.1
Li et al.[2]	2024	1500- 1600	$Al_2O_3$	CASM	Rotation	BLD	16.6-95.2
Deng et al.[14]	2024	1450- 1550	Al <sub>2</sub> O <sub>3</sub>	CASMT		BLD	2.18-4.18

A: Al<sub>2</sub>O<sub>3</sub>, B: B<sub>2</sub>O<sub>3</sub>, C: CaO, F: FeO, L: Li<sub>2</sub>O, M: MgO, N: Na<sub>2</sub>O, S: SiO<sub>2</sub>, T: TiO<sub>2</sub>.

BLD: boundary layer diffusion; CR: chemical reaction; DS: diffusion in the stagnant slag; PLD: product layer diffusion.

D: determined diffusion coefficient of dissolving species in slags.

# 2 Methodology

- 2 2.1 Experiments
- 3 2.1.1 Material

- 4 High-purity laboratory-grade powder of CaO, Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>, and CaCO<sub>3</sub> (Alfa Aesar, USA)
- 5 was used to produce synthetic inclusion particles and slags. To remove moisture, the CaO was
- 6 roasted in a Si-Mo rod box type resistance furnace (maximum temperature: 1200°C) at 1050°C
- for 12 h, while the Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>, and CaCO<sub>3</sub> were dried in a drying oven (maximum temperature:
- 8 400°C)) at 150°C for 24 h before use.
- 9 To explore the effect of CA2 porosity on the dissolution process, two types of CA2 particles
- were prepared: porous (p-CA2) and dense (d-CA2). Porous CA2 particles, p-CA2, were prepared
- by sintering 100 g of CaCO<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> powder in stochiometric amounts at 1600°C for 24 h under
- an argon atmosphere. The details for powder mixing and sintering are available in one of our
- previous studies [11]. Dense CA2 particles, d-CA2, were obtained by melting approximately 5 g
- of the p-CA2 particles in a water-cooled copper mold using an arc melter. The slag composition
- used in this study, i.e. 33CaO-18Al<sub>2</sub>O<sub>3</sub>-49SiO<sub>2</sub> (wt.%), was the same as a previous study [19].
- 16 2.1.2 Experiments
- An HT-CLSM (VL2000DX-SVF17SP, Yonekura) was used to carry out the CA2 particle
- dissolution experiments, providing continuous in-situ observation. Technical details and
- operation procedures for the HT-CLSM facility are available elsewhere [46, 47]. Each experiment
- was conducted as follows. First, approximately 0.15 g of slag was pre-melted in a platinum
- 21 crucible (5 μm in diameter and 6 μm in height) within the HT-CLSM furnace. Second, a CA2
- particle (either the p-type or the d-type) was placed on top of the pre-melted slag, and the
- assembly was heated to the experimental temperature according to a specified heating profile:
- rapid heating (1000 °C/min) to 50°C below the test temperature, slow heating (50°C/min) to the
- 25 test temperature. The start time of dissolution,  $t_0$ , was defined as the time (at the test temperature)
- 26 when the CA2 particle became fully immersed within the molten slag. The entire dissolution
- 27 process of the CA2 particle was recorded using a CCD camera at a frame rate of 5 frames per
- second. The captured images have a resolution of 1024×1024 pixels, with each pixel
- 29 corresponding to a size of 0.9 μm when using a 5X objective lens and 2.3 μm when using a 2X
- 30 objective lens. Note that the mass of the CA2 particle used in each dissolution experiment was
- less than 0.1% of that of slag. As a result, the slag composition and properties were not affected
- 32 by the dissolution of particle.

Data postprocessing was carried out using the ImageJ software [48] to determine the time-evolution of the dissolution process. Each CA2 particle was segmented from the slag in each frame based on image contrast, and the particle diameter was measured. The measurements were repeated three times to reduce manual error, and then averaged. From this data, the evolution in equivalent radius, assuming a spherical particle, was determined.

## 38 2.1.3 Characterization

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X-ray diffraction (XRD) (Panalytical X'pert diffraction instrument, using a copper source with a wavelength of 1.540 56 Å) was employed to identify the phases present within the synthesized CA2 particles.

X-ray computed tomography (XCT) was conducted on two p-CA2 and two d-CA2 particles using a ZEISS Xradia 630 Versa system to characterize the surface area and internal porosity of the CA2 particles. In total, two XCT scans were performed, one for each type of particle, with the same scan parameters applied for both scans. The field of view for each scan was approximately 2.6 mm × 2.6 mm, with two particles in each XCT scan. This resulted in a volumetric dataset comprising approximately 2036×2036×2036 voxels, with a voxel size of 1.3 µm. For each scan, 2401 radiographs were acquired over a 360-degree rotation with an exposure time of 5.5 seconds per radiograph. An accelerating voltage of 90 kV was used during the imaging process. The CA2 particles were sandwiched between Kapton tape layers to ensure secure positioning on the sample holder and to prevent sample fluttering during image acquisition. Postprocessing was carried out using the Dragonfly software to determine the pore number density, apparent surface area, and pore volume of CA2 particles. Due to the irregular shape of CA2 particles, the volume of the surface-connected pores could not be measured directly and only the internal pores were counted using the Dragonfly analysis software as shown in Fig. 2(a). To address this challenge, the 3D XCT images of all four particles were cropped into spheres with a fixed radius  $r = 150 \mu m$ . This value was chosen since it represents the radius of the maximum sphere that can be fit within the irregularly shaped CA2 particles. The total volume of internal and surface-connected pores was measured without distinction, as cropping could convert internal pores into surface-connected ones (Fig. 2(b)).

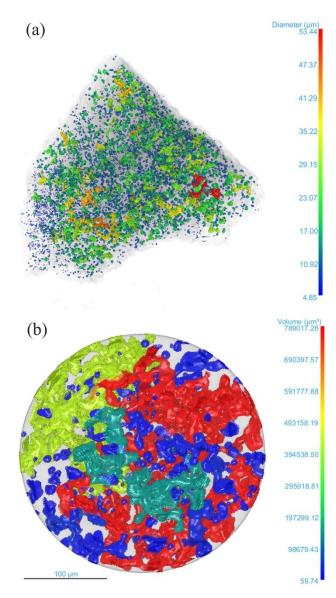


Figure 2. X-ray Computed Tomography images of one d-CA2 particle prepared by arc melting (a) presents the original CA2 particles, and (b) present corresponding cropped spheres (radius 150 μm). Color maps indicate equivalent spherical diameters (a) and pore volumes (b).

# 2.2 Model development

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During a particle dissolution, a particle's time-dependent mass loss,  $J_1(m/s)$ , is formulated as:

$$J_1 = -\frac{1}{S_S} \frac{dM_P}{dt} \tag{1}$$

where  $M_P$  is the particle mass (kg) and  $S_S$  is the surface area of the particle (m<sup>2</sup>). By assuming that the particle is nonporous and spherical,  $M_P$  and  $S_S$  can be expressed as:

$$M_{p} = V_{P}\rho_{P} = \frac{4}{3}\pi r^{3}\rho_{P}$$

$$S_{S} = 4\pi r^{2}$$
(2)
(3)

$$S_s = 4\pi r^2 \tag{3}$$

where  $V_P$  is the particle volume (m<sup>3</sup>),  $\rho_P$  is the particle density (kg/m<sup>3</sup>), and r is the equivalent 73 spherical radius (m). According to mass conservation, the loss rate of the particle  $J_1$  must equal the 74 mass flux,  $J_2$  (m/s), across the boundary layer: 75

$$J_1 = J_2 \tag{4}$$

where  $J_2$  can be determined from: 77

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$$J_2 = -k_m(C_{sat} - C_0)$$
 (5)

where  $k_m$  is the apparent rate constant,  $C_{sat}$  is the saturation concentration of the dissolving 79 species, and  $C_0$  is the concentration of the dissolving species in the bulk slag. Coupling equations 80 from (1) to (5), the time-dependent radius gives: 81

$$\frac{dr}{dt} = -\frac{k_m(C_{sat} - C_0)}{\rho_P} \tag{6}$$

<u>Chemical Reaction Control:</u> In this approach, it is assumed that the apparent rate constant  $k_m$  is 83 84 controlled by the chemical reaction rate,  $k_c$ , between the particle and molten slag, and further that  $k_c$  is a constant. Integrating both sides of equation (6), from  $r_0$  to r and from 0 to  $\tau$ , gives [40]: 85

$$\frac{r}{r_0} = 1 - \frac{t}{\tau} \tag{7}$$

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$$\frac{r}{r_0} = 1 - \frac{t}{\tau}$$

$$\tau = \frac{\rho_P}{(C_{sat} - C_0)k_c}$$
(7)

- where  $r_0$  is the initial equivalent radius of the particle (m).  $\tau$  is the total dissolution time of the 88 89 particle (s).
- 90 The dissolution limiting step is considered CR if the normalized experimental dissolution curve 91 matches the curve from equation (7).
  - Boundary Layer Diffusion Control: In this approach, it is assumed that the mass transfer rate is governed by mass transport of reactants and products to and from the slag-particle interface, and further that the thickness of the boundary layer and the concentration profile of the dissolving species can be assumed to be constant. Under conditions of "Stokes flow", the influence of convection can also be ignored. As a result, the mass transfer coefficient can be expressed as the ratio of the diffusion coefficient to the particle radius, i.e.,  $k_m = D/r$ . Integrating both sides of equation (6) from  $r_0$  to r and from 0 to  $\tau$ , gives [40]:

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$$\frac{r}{r_0} = (1 - \frac{t}{\tau})^{1/2}$$
 (9)

$$\tau = \frac{\rho_p r_0^2}{2(C_{sat} - C_0)D} \tag{10}$$

The dissolution limiting step is determined as BLD when the normalized experimental 101 102 dissolution curve aligns with the curve predicted by equation (9).

As discussed in the introduction, several studies have reported the motion of particles during the dissolution process, suggesting its importance to include in the modeling. Moreover, the pores

within the particle, affecting the dissolution kinetics by altering the contact area between the 105 106 particle and bulk slag, should also be considered in the modeling.

107 2.2.1 Incorporation of particle porosity

To incorporate particle porosity, Equations (2) and (3) can be rewritten as:

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$$M_P = V_P \rho_P (1 - \varphi) = \frac{4}{3} \pi r^3 \rho_P (1 - \varphi)$$
 (11) 
$$S_S = f(\varphi) 4\pi r^2$$
 (12)

$$S_S = f(\varphi) 4\pi r^2 \tag{12}$$

- where  $\varphi$  represents the particle porosity as compared to a solid sphere of equivalent diameter, 111
- $f(\varphi)$  defines a function that represents the change in particle surface area due to surface porosity. 112
- Equation (6) then becomes: 113

$$\frac{dr}{dt} = -\frac{k_m(C_{sat} - C_0)f(\varphi)}{\rho_P(1 - \varphi)}$$
(13)

- 115 More details on the methodology for determining surface area and particle porosity are provided
- 116 in section 3.1.

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- 2.2.2 Incorporation of particle velocity 117
- Convective flow resulting from particle motion enhances mass transport of the dissolving 118 species thereby reducing the thickness of the boundary layer between slag and particle. The Péclet 119
- number, Pe=2rv/D [49] where v is the particle velocity, is a dimensionless quantity used to 120
- quantify the importance of convective transport as compared to diffusive transport. In this study, 121
- it can be assumed that convection fluxes are caused by natural convection because of the density 122
- gradient in the molten slag. This is because there are no external forces within the HT-CLSM to 123
- otherwise stir the molten slag or induce particle movement. As a result, particle velocity during 124
- dissolution is given by [50, 51]: 125
- For Re < 1, 126

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$$v = \frac{2r^2*(\rho_P - \rho_S)*(1 - \varphi)*g}{9\mu_S}$$
 (14)

For  $1 < Re < 10^5$ 128

$$v = \sqrt{\frac{8gr(\rho_P - \rho_S)*(1-\varphi)}{3\rho_S C_D}}$$
 (15)

 $C_{\rm D} = \frac{24}{\text{Re}} (1 + 0.15 \text{Re}^{0.687}) + \frac{0.42}{1 + 42500 Re^{-1.16}}$ 131 (16)

- where  $Re = \frac{2rv\rho_S}{\mu_S}$  is the Reynolds number with  $\mu_S$  being the viscosity of the slag (Pa·s),  $C_D$  is the 132
- drag coefficient.  $\rho_S$  is the density of the slag (kg/m<sup>3</sup>) and g is the force of gravity (m/s<sup>2</sup>). 133
- Assuming that the mass transfer rate is governed by both the diffusion of the dissolving species 134
- as well as convection due to the particle's motion, [52]: 135
- 136 For  $Pe \le 10000$ ,

$$k_m = \frac{D(4+1.21*Pe^{\frac{2}{3}})^{\frac{1}{2}}}{2r}$$
 (17-1)

138 For Pe > 10000,

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$$k_m = \frac{1.1DPe^{1/3}}{2r} \tag{17-2}$$

141 Coupling equations (13), (17-1), and (17-2), the dissolution rate is given as:

142 For  $Pe \le 10000$ ,

$$\frac{dr}{dt} = -\frac{f(\varphi)(C_{Sat} - C_0)D(4 + 1.21 * Pe^{\frac{2}{3}})^{\frac{1}{2}}}{2r\rho_p(1-\varphi)}$$
(18-1)

144 For Pe > 10000,

$$\frac{dr}{dt} = -\frac{1.1f(\varphi)(C_{sat} - C_0)DPe^{\frac{1}{3}}}{2r\rho_p(1-\varphi)}$$
 (18-2)

The above equations were numerically solved using MATLAB via the ode45 solver. This new model is named Modified Mass transfer-controlled Dissolution Model (MMDM).

## 3 Results and discussion

3.1 Characterization of calcium aluminates

**Fig. 3** presents the XRD patterns of d-CA2 (blue line) and p-CA2 (red line), which align well with the standard reference CA2 (black line)[53]. The absence of additional phases confirms the successful synthesis of high-purity CA2 particles.

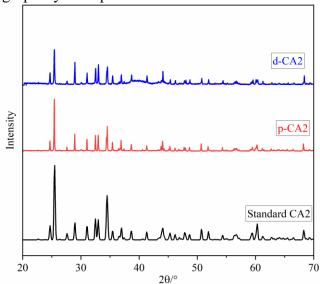


Figure 3. XRD patterns of d-CA2 (blue line), p-CA2 (red line), and standard CA2 (black line)

**Table 2** provides the physical properties of the two p-CA2 and two d-CA2 particles analyzed via 3D XCT. As can be seen, the porosities of p-CA2 particles are higher than that of d-CA2

particles (0.20 and 0.29 vs. 0.08 and 010). This illustrates that the arc melting considerably reduced the porosity of the CA2 particles. In terms of surface area, the table also shows that the ratio of the effective surface area to the surface of an equivalent sphere varies from particle to particle but the values for p-CA2 is always much greater than ones for d-CA2, further indicating the complex geometry and porosity of CA2 particles.

Table 2 Summary of physical parameters of cropped CA2 particles

Particle	Pore Volume (*10 <sup>6</sup> µm <sup>3</sup> )	$f(\varphi)$	Fraction Porosity	
p1-CA2	2.8	3.3	0.20	
p2-CA2	4.1	4.1	0.29	
d1-CA2	1.2	1.2	0.08	
d2-CA2	1.7	2.7	0.12	

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- The values of ratio,  $f(\varphi)$ , can be plotted as a function of porosity  $\varphi$ , as shown in **Fig. 4.** It should
- be noted that the first data point in **Fig. 4** is a theoretical value, corresponding to  $\varphi = 0$ , where
- 168  $f(\varphi) = 1$ . An exponential relationship is observed between  $f(\varphi)$  and  $\varphi$ ,

$$f(\varphi) = e^{5.3469\varphi} \tag{19}$$

- 170 Accordingly, equations (18-1) and (18-2) were rewritten to incorporate this relationship,
- 171 For  $Pe \leq 10000$ ,

$$\frac{dr}{dt} = -\frac{e^{5.3469\varphi}(C_{sat} - C_0)D(4 + 1.21 * Pe^{\frac{2}{3}})^{\frac{1}{2}}}{2r\rho_p(1 - \varphi)}$$
(20-1)

173 For Pe > 10000,

$$\frac{dr}{dt} = -\frac{1.1 * e^{5.3469\varphi} (C_{sat} - C_0) DP e^{\frac{1}{3}}}{2r\rho_p (1-\varphi)}$$
(20-2)

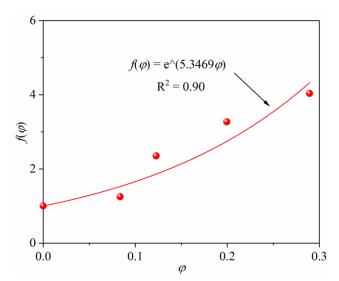


Figure 4. XCT-determined specific surface area  $f(\varphi)$  as a function of porosity,  $\varphi$ , along with a best-fit exponential curve through the data points.

# 3.2 Effect of CA2 particle behaviors on the dissolution kinetics

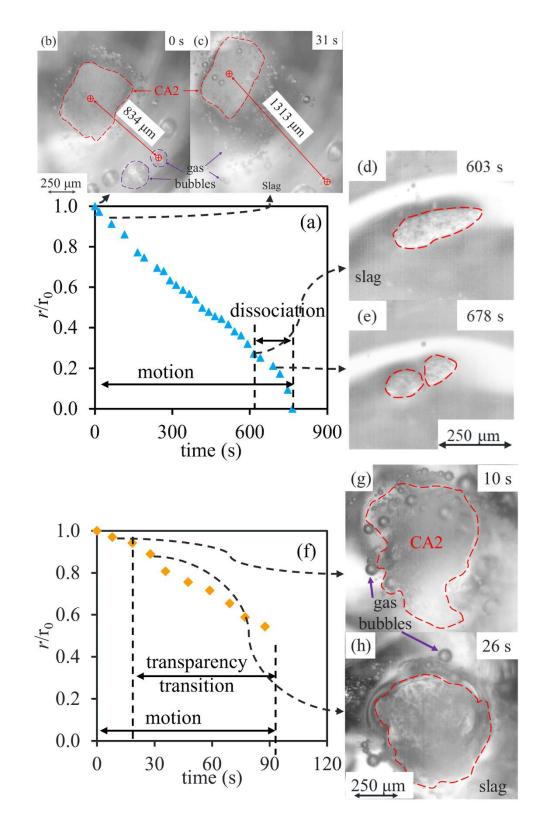
During the dissolution experiments of the CA2 particles at 1550°C in slag, various particle behaviors were observed including motion, dissociation, transparency transition and interaction with gas bubbles. Notably, particle motion was consistently observed, whereas the other behaviors were only observed in specific experiments. **Fig. 5** presents a sequence of images illustrating these behaviors. The solid red and purple boundaries denote projection areas of CA2 particle and gas bubbles, respectively, with the surrounding area comprised of transparent molten slag. The corresponding dissolution curves, normalized by initial radius and segmented by behavioral sections, are also provided.

**Fig. 5 (a-e)** depict the dissolution of the d1-CA2 particle, which exhibited both motion throughout the test and dissociation after 603 s. The particle was observed to move a considerable distance, 479 μm over the first 31 s, resulting in an average velocity of 15.4 μm/s. The dissociation resulted in the formation of two smaller fragments. The dissolution curve shows approximately linear behavior until dissociation. The steepened slope during the dissociation phase indicates that dissociation enhanced dissolution by increasing the contact area between the particle and molten slag. This observation underscores the importance of considering the actual surface area of a porous particle in modeling. Note that after the d1-CA2 particle dissociated into two fragments, the projection area for both fragments was measured separately via the ImageJ software [48]. The total projection area, including both fragments, was then used to determine the equivalent radius

of the dissociated d1-CA2 particle.

**Fig. 5 (f-h)** show the dissolution of the p2-CA2 particle, which dissolved rather quickly and dissociated after 90 s. The main feature to highlight with this particle is the transition in transparency, changing from opaque to semi-transparent, from 20 s to 90 s. Changes in inclusion transparency were also reported by Fox et al.[25] for an Al<sub>2</sub>O<sub>3</sub> particle, Liu et al.[35] for a MgO particle, and Sharma et al. [4] for an Al<sub>2</sub>TiO<sub>5</sub> particle. After 90 s, the semi-transparent particle dissociated into numerous smaller fragments, which subsequently dissolved rapidly. Data collected after 90 s was excluded as measuring the projection area of these fragments became impractical. Moreover, the p2-CA2 particle exhibited movement throughout the dissolution process. [4, 25, 35]

Another phenomenon observed during the dissolution process was the interaction of the particle with a gas bubble, as illustrated in **Fig. 5** (i-k). This observation is for the dissolution of a p-CA2 whose porosity and surface area were not determined using XCT. The particle interacted with a gas bubble for ~118 s, between 230 s and 338 s. Initially, the particle dissolved relatively quickly, but dissolution was effectively paused during the period that the particle interacted with the gas bubble. After exiting the gas bubble, the dissolution rate returned to its initial value. As a result, it is clear that the gas bubble obstructed the interaction between the p-CA2 and molten slag, thereby hindering the mass transport of dissolved species from thep-CA2 - slag interface to bulk slag. Note that the radius of the particle within gas bubble was measured through projection area.



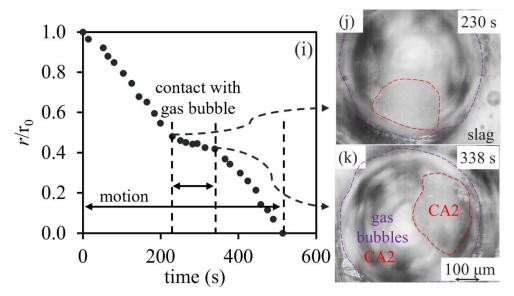


Figure 5. Evolution of normalized radius changes of CA2 particles as a function of time in slag at 1550°C, illustrating different CA2 particle behaviors observed during the dissolution process: (a-e) motion and dissociation in the slag of d1-CA2, (f-h) motion and transparency transition of p2-CA2, and (i-k) motion and interaction with a gas bubble of p-CA2.

# 3.3 Effect of CA2 particle porosity on the dissolution kinetics

The relationship between porosity and dissolution kinetics at 1550°C in slag can be examined by looking at the total dissolution time of three of the four CA2 particles characterized via XCT. However, dissociation occurred very early-on during the experiment for p2-CA2, and so it was excluded. **Table 3** summarizes the dissolution time and rate of CA2 particles with different porosities. For p1-CA2 ( $\varphi$  of 0.20,  $r_0$  = 346  $\mu$ m),  $\tau$  was around 591 s. For d1-CA2 ( $\varphi$  of 0.08,  $r_0$  = 297  $\mu$ m),  $\tau$  was around 603 s. However, that particle only partially dissolved, to 91  $\mu$ m, prior to dissociation. Finally, for d2-CA2 ( $\varphi$  of 0.12,  $r_0$  = 105  $\mu$ m),  $\tau$  was around 295 s. This data can be used to determine a total dissolution rate, which is seen to increase from approximately 0.34  $\mu$ m/s to 0.59  $\mu$ m/s as the porosity increased from 0.08 to 0.20, indicating that higher porosity enhances the dissolution rate. This is attributed to the larger surface area associated with higher porosity, which increases the reaction area between particle and molten slag.

Table 3 Summary of CA2 particle dissolution time and rate at 1550°C

particle	r <sub>0</sub> (μm)	<i>r</i> <sub>τ</sub> (μm)	φ	$\varphi$ $\tau$ (s) $(r_0-r_\tau)/\tau$ ( $\mu$ m/s)	
p2-CA2	346	0	0.20	591	0.59
d1-CA2	297	91	0.08	603	0.34

# 4 Validation and application of MMDM

## 4.1 MMDM validation

Experimental data from the literature[29] were employed to validate the MMDM and compare its performance with other conventional models. The dissolution of a spherical Al<sub>2</sub>O<sub>3</sub> particle into 29.7CaO-24.1Al<sub>2</sub>O<sub>3</sub>-46.2SiO<sub>2</sub> (wt.%) slag observed using CLSM at 1550°C, as reported by Liu et al.[29], was selected for validation. They employed the DS model to determine the dissolution mechanism, which assumes the NMI-slag interface is invariant. This means that the diffusion field would have stayed once the NMI-slag interface had been fixed at the beginning of the dissolution. For a spherical particle dissolution, based on Fick's first and second laws, the dissolution rate of the particle is expressed as[41]:

$$\frac{dr}{dt} = -\frac{c_{sat} - c_0}{c_p - c_{sat}} \frac{D}{r} - \frac{c_{sat} - c_0}{c_p - c_{sat}} \sqrt{\frac{D}{\pi t}}$$

$$\tag{21}$$

This study was chosen due to the spherical shape of  $Al_2O_3$  particles, aligning with a critical assumption: the particle is spherical for all four models. Moreover, Liu et al. reported particle motion during the dissolution process, which they identified as a primary scatter source in their experimental data. Unfortunately, the porosity of the spherical alumina particle was not specified, so a value of  $\varphi=0$  was assumed in the current model for validation. Equations (7 and 8) for CR model, equations (9-11) for BLD model, equation (20-1) for MMDM, and equation (21) for DS model were solved using the parameters provided in **Table 4** from Liu's work[29]. The obtained normalized dissolution curves based on each model are presented in **Fig. 6**. The spherical markers represent Liu's experimental results, while the dashed-doted, dotted, solid, and dashed lines correspond to predictions of the CR model, BLD model, MMDM, and DS model, respectively. The CR model and MMDM initially agreed with experimental data for  $t/\tau < 0.20$ . When  $t/\tau$  is between 0.2 and 0.45, the predictions of both MMDM and DS models are close to the experimental data. Beyond 0.45, only the MMDM aligns well with experimental data. By accounting for the motion of the spherical particle in the molten slag, the MMDM offers a more accurate representation of the dissolution mechanism under experimental conditions.

Table 4 Parameters used in the models

r <sub>0</sub> (μm)	$ ho_{slag} (kg/m^3)$	$\rho_{Al2O3}$ $(kg/m^3)$	μ (Pa·s)	$\Delta C_{\text{Al2O3}}$ (kg/m <sup>3</sup> )	$D  (\mathrm{m^2/s})$	τ (s)
250	2622	3950	2.10	651	2.50E-11	1982

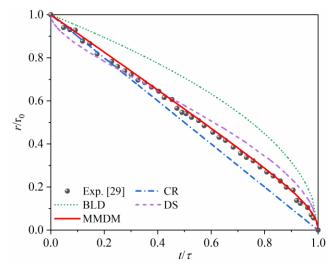


Figure. 6 Normalized dissolution curves for spherical Al<sub>2</sub>O<sub>3</sub> particle in molten slag at 1550°C compared with different dissolution rate-controlling models

To investigate the influence of particle motion on the shape of the dissolution curve, the  $k_{\rm m}$  of Al<sub>2</sub>O<sub>3</sub> particle in 29.7CaO-24.1Al<sub>2</sub>O<sub>3</sub>-46.2SiO<sub>2</sub> (wt.%) slag was analyzed over time using the BLD, and MMDM, with parameters provided in **Table 4**. The CR and DS models were excluded due to their assumptions, which do not yield  $k_{\rm m}$ . In contrast, the BLD and MMDM require D to determine  $k_{\rm m}$ , with D values of 9.57\*10<sup>-11</sup> m<sup>2</sup>/s and 2.75\*10<sup>-11</sup> m<sup>2</sup>/s, respectively. D is back-calculated according to the total dissolution time in both BLD and MMDM. For the same total dissolution time, different D values are obtained with different models.

**Fig. 7(a)** illustrates  $k_m$  as a function of  $t/\tau$ . In both BLD and MMDM,  $k_m$  increases with  $t/\tau$ . Initially ( $t/\tau < 0.7$ ), the  $k_m$  in BLD is slightly lower than in MMDM. However, beyond this point,  $k_m$  in BLD surpasses MMDM, which is inconsistent with expectations. This discrepancy arises because BLD only accounts for diffusion, leading to an overestimated D. In contrast, MMDM incorporates both natural convection and diffusion, resulting in a higher  $k_m$  compared to BLD. **Fig. 7(b)** shows the ratio of  $D/k_m$ , interpreted as the boundary layer thickness. The MMDM consistently predicts a thinner boundary layer than BLD throughout the dissolution process. Given that D remains constant for a specific particle-slag system at a fixed temperature, a thinner boundary layer corresponds to a higher  $k_m$ . Thus, particle motion effectively reduces the boundary layer thickness, enhances  $k_m$ , and leads to a steeper dissolution curve compared to the BLD model (**Fig. 6**).

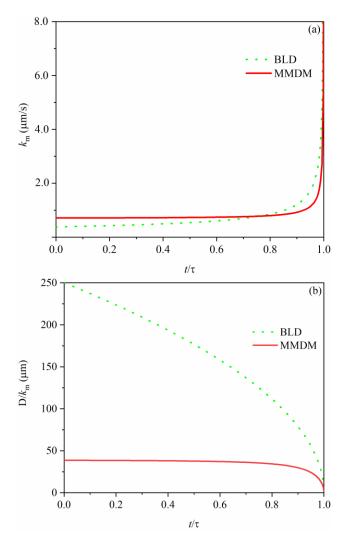


Figure. 7 (a) variation of  $k_{\rm m}$  as a function of  $t/\tau$  for BLD and MMDM. (b) Variation of  $D/k_{\rm m}$  as a function of  $t/\tau$  for BLD and MMDM.

# 4.2 MMDM application

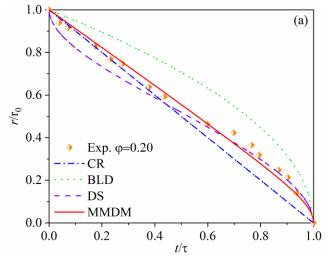
## 4.2.1 Determination of diffusion coefficient of CA2

The dissolution rate-limiting step of CA2 particles was first identified by comparing normalized dissolution curves with model predictions. The best fitted model was then applied to determine the diffusion coefficient of CA2 particle in slag at 1550°C. The  $\Delta C_{\text{Al2O3}}$  and  $\mu$  are 1481 kg/m<sup>3</sup> and 1.36 Pa·s for slag at 1550°C, respectively, which were calculated by FactSage 8.0 with the FToxid databases [54]. The rest of the parameters required for the models' calculation can be found in **Table 2**.

Fig. 8 (a) presents normalized experimental data and predictions of four models (diamonds: experimental data, dashed-dotted line: CR, dotted line: BLD, dashed line: DS, and solid line:

MMDM). As can be seen, when the  $t/\tau$  is less than 0.5, both CR and MMDM aligned well with experimental data. After that, DS and MMDM agreed with the experimental data. Therefore, the MMDM has a much better fitting with experimental data by incorporating the porosity and motion of CA2 particles, indicating that mass transfer, including natural convection and diffusion, is the primary rate-limiting step for CA2 particle dissolution in the slag. The diffusion coefficient,  $1.15*10^{-11}$  m<sup>2</sup>/s, of CA2 in slag at 1550°C was determined using MMDM, which is in the range reported by the literature[11].

The determined diffusion coefficient,  $1.25*10^{-11}$  m<sup>2</sup>/s, was applied to predict the dissolution time for the d1-CA2 and d2-CA2 particles using MMDM in slag at 1550°C. As shown in **Fig. 8** (b), the total dissolution time (including the time after dissociation) for the d1-CA2 particle with radii of 297 µm is 764 s, 51 s shorter than the MMDM prediction of 815 s. This discrepancy is likely due to the particle dissociation observed after 603 s, as discussed in section 3.2. Additionally, the average velocity of CA2 particle, calculated using equation (14), is 14.2 µm/s, closely aligns with the experimentally measured average velocity of 15.4 µm/s, determined from the CA2 particle's displacement during the first 31 s of recorded dissolution images . For the d2-CA2 with a radius of 105 µm, the total dissolution time is 297 s, slightly exceeding the MMDM prediction of 2284 s by 13 s. Despite slight variations, the MMDM predictions closely match the experimental dissolution times. The experimental dissolution curves for both types of CA2 particles align well with the MMDM predictions, confirming that mass transfer is the rate-limiting step for CA2 dissolution. The findings also indicate that particle porosity impacts dissolution time, underscoring its importance in predicting dissolution kinetics accurately.



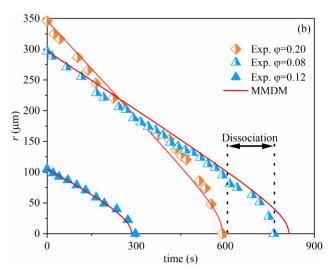


Figure 8. (a) Comparison of normalized dissolution curves for p1-CA2 particles and four models, (b) Comparison of CA2 particle's radius change as a function of time between experiments and MMDM prediction in slag at 1550°C.

## 4.2.2 Prediction of CA2 dissolution time

The MMDM model was applied to predict the total dissolution time of CA2 particles in CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> slags at 1550°C. **Fig. 9** shows two heatmaps, showing  $\tau$  with variations in  $\varphi$  and  $\nu$ , and with variations in  $\mu$  and  $\Delta C$ , for  $r_0 = 200$   $\mu$ m. Beginning with **Fig. 9** (a), it can be seen that as  $\nu$  increases from 0  $\mu$ m/s to 10  $\mu$ m/s,  $\tau$  decreases significantly, particularly for  $\varphi$  is less than 0.2. Beyond  $\nu = 10$   $\mu$ m/s,  $\tau$  decreases slightly with further increasing  $\nu$  to 40  $\mu$ m/s. Similarly, increasing  $\varphi$  from 0 to 0.4 reduces  $\tau$ , highlighting the role of porosity in enhancing dissolution by increasing the effective contact/surface area between molten slag and particle. The combined effects of  $\nu$  and  $\varphi$  demonstrate that higher  $\nu$  and  $\varphi$  lead to shorter dissolution times, emphasizing their importance in accurately modeling particle dissolution in slags. In **Fig. 9** (b), it can be seen that  $\tau$  was decreased when decreasing  $\mu$  and increasing  $\Delta C$ . Moreover, the  $\tau$  is more sensitive to the low  $\Delta C$  region with the same  $\mu$ . For example, when  $\mu = 2$  Pa·s, increasing  $\Delta C$  from 200 kg/m<sup>3</sup> to 800 kg/m<sup>3</sup> reduces  $\tau$  from 2551 s to 637 s, but further increasing  $\Delta C$  to 1600 kg/m<sup>3</sup> reduces  $\tau$  only to 318 s. A similar trend was observed for the changes in  $\mu$ . Note that in this figure,  $\varphi = 0.2$  is assumed.

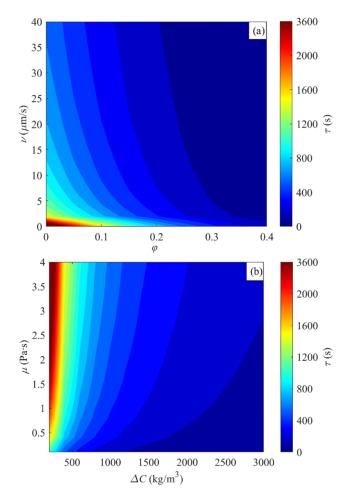


Figure. 9 Prediction of the total dissolution time of CA2 particles in CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> slag at 1550°C a) variation of v and  $\varphi$ , b) variation of  $\mu$  and  $\Delta C$ . (the color bar is nonuniform)

A parameter sensitivity study was conducted to evaluate the relative influence of v,  $\Delta C$ ,  $\varphi$  and  $\mu$  on  $\tau_i$  predicted by the used the MMDM. The reference parameters  $(X_{r(i)})$  were set as  $v=10 \,\mu\text{m/s}$ ,  $\varphi=0.1$ ,  $\mu=1 \,\text{Pa}\cdot\text{s}$  and  $\Delta C=1000 \,\text{kg/m}^3$ , yielding a baseline dissolution time of  $\tau_r=790 \,\text{s}$ . Each parameter  $(X_i)$  was varied independently by increasing or decreasing its value fourfold relative to the reference, with a step change of twofold, except  $\Delta C$ , which was halved. **Fig. 10** presents the percentage change of  $\tau$  as a function of parameter variation. For  $0.25 \leq X_i/X_{r(i)} \leq 2$ ,  $\Delta C$  has the most significant effect on  $\tau$ , while  $\mu$  has the least impact. However, for  $2 < X_i/X_{r(i)} \leq 4$ ,  $\varphi$  becomes the most influential parameter, and v has the smallest impact on  $\tau$ . Consequently, the order of parameter influence is for  $0.25 \leq X_i/X_{r(i)} \leq 2$ ,  $\Delta C > \varphi > v > \mu$ , and for  $2 < X_i/X_{r(i)} \leq 4$ ,  $\varphi > \Delta C > \mu > v$ . Moreover, the sensitivity of  $\tau$  to parameter variations is more pronounced at lower values than at higher ones.

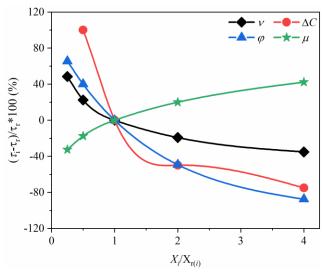


Figure. 10 Effects of parameters variation  $(v, \Delta C, \varphi \text{ and } \mu)$  on the total dissolution time in percentage

## Conclusions

In this study, two types of porosity level CA2 particles, p-CA2 and d-CA2, were prepared by sintering and arc melting, respectively, with their porosities and surface areas characterized using XCT. The dissolution process of these CA2 particles in CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> type slag was investigated through in-situ observation. A dissolution model was then developed, incorporating the motion and porosity of CA2 particles. The key findings are as follows:

- 1) The dissolution behavior of CA2 particles, including motion, dissociation, and interaction with gas bubbles, has been observed and described during the experiments. The first two behaviors enhanced the dissolution of the CA2 particles while the interaction with the gas bubble slowed down dissolution.
- 2) Increasing the porosity of CA2 particles enhances dissolution kinetics, with the average dissolution rate rising from 0.35  $\mu$ m/s to 0.59  $\mu$ m/s as porosity increases from 0.08 to 0.20.
- 3) A mathematical model named "modified mass transfer-controlled dissolution model (MMDM)" was developed by incorporating particle velocity and porosity assuming natural convection. This model can provide a better fit with experimental results as compared to the conventional models lacking these considerations. The MMDM prediction showed that the total dissolution kinetics of CA2 particles was enhanced by an increase in  $\varphi$ , v and  $\Delta C$ , and a decrease in  $\mu$ . The parameter sensitivity analysis found that the order of parameter influence is for  $0.25 \le X_i/X_{r(i)} \le 2$ ,  $\Delta C > \varphi > v > \mu$ , and for  $2 < X_i/X_{r(i)} \le 4$ ,  $\varphi > \Delta C > \mu > v$ .

#### 388 Nomenclatures

Nome	Nomenclatures					
$J_1$	the mass loss rate of the particle (m/s)					
$J_2$	mass flux through boundary layer (m/s)					
$M_{ m P}$	mass of particle (kg)					
$S_{ m S}$	the nonporous surface area of the particle (μm <sup>2</sup> )					
$S_1$	the porous surface area of the particle $(\mu m^2)$					
$ ho_{ ext{P}}$	density of particle (kg/m <sup>3</sup> )					
$ ho_{ m S}$	density of slag (kg/m3)					
r	radius of particle (μm)					
$r_0$	initial radius of particle (μm)					
τ	total dissolution time of particle (s)					
t	dissolution time particle (s)					
K	mass transfer coefficient of dissolving species (m/s)					
D	diffusion coefficient of dissolving species (m <sup>2</sup> /s)					
$C_{\mathrm{sat}}$	saturation concentration of dissolving species (kg/m <sup>3</sup> )					
$C_0$	concentration of dissolving species in bulk slag (kg/m <sup>3</sup> )					
$C_{\mathrm{P}}$	the concentration of dissolving species in particles (kg/m <sup>3</sup> )					
$\Delta C$	concentration of dissolving species between that at x and bulk slag					
	$(kg/m^3)$					
$\varphi$	porosity of particle					
Pe	Péclet number					
Re	Reynolds number					
v	velocity of particle (m/s)					
$\mu_{ m S}$	viscosity of slag (Pa·s)					
$C_{\mathrm{D}}$	drag coefficient					
g	gravity (m/s <sup>2</sup> )					

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396 Statements and Declarations

On behalf of all authors, the corresponding author states that there is no conflict of interest.

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