

# The Essence of Space Mapping: Less is More

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presented at  
Third International Workshop on Surrogate Modelling and Space Mapping for Engineering Optimization (SMSMEO 2012)  
August 9-12, 2012, Reykjavik University, Iceland

# Physics-based Surrogates

facilitate optimal engineering designs

high-fidelity or “fine-model” simulation accuracy

“coarse-model” simulation speed

# If Knowledge Can Be Built into a Model . . .

## What about “Feel” and Intuition?

**space mapping** exploits the engineer’s traditional “quasi-global” intuition

enhances physics-based surrogates derived from simple mappings of coarse models (the “less”) to realize accurate surrogates of corresponding fine models (the “more”)

**space mapping** explains the engineer’s mysterious “feel” for a problem

# Space Mapping vs. Other Surrogate-based Approaches

how the space mapping concept come into being

how it differs from other approaches that found favor at much the same time

the essential difference (oversimplified for discussion)

**space mapping**: an understanding of the “feel” that an experienced engineer has for a complex design problem

generic surrogate approach: arises from the “feel” that a mathematician has for a generic optimization problem

# “Surrogate” “Model” “Simulation”

confusion sets in when these words are used arbitrarily and interchangeably to mean almost any representation of anything

imply underlying knowledge—nowadays typically the physics embodied in a simulator

this knowledge is manipulated from the “inside” or the “outside”

depends on whether the designer is oriented towards engineering or mathematics (or perhaps both)

# **The Grand Design**

*(Hawking and Mlodinow, 2012)*

“model-dependent realism . . . is based on the idea that our brains interpret the input from our sensory organs by making a model of the world.” (p. 7)

“human behavior is indeed determined by the laws of nature”  
(p. 32)

“it is pointless to ask whether a model is real, only whether it agrees with observation.” (p. 45-46)

“The brain, in other words, builds a mental picture or model.”  
(p. 47)

# The Grand Design

*(Hawking and Mlodinow, 2012, p. 51)*

A model is a good model if it:

[**good: subjective**]

1. Is elegant [**subjective**]
2. Contains few arbitrary or adjustable elements  
[**subjective**]
3. Agrees with and explains all existing observations  
[**all existing observations? “all”?**]
4. Makes detailed prediction about future observations that can disprove or falsify the model if they are not borne out.

# The Grand Design

*(Hawking and Mlodinow, 2012, p. 172)*

“Our brains interpret the input from our sensory organs by making a model of the outside world . . . trees . . . people . . . other universes . . .”



# The Essence of **Space Mapping**: Less is More

the technique is to build a thin layer around existing knowledge

the layer is minimally complex (the mapping is usually linear or very simple)

for model enhancement, the data required is small; a single data sample might be enough; often a star distribution is sufficient

for design, the iteration count is small; manual implementation is possible in many cases

the resulting enhanced model or design can be astonishingly good

## **Writer's Cliché #1: “Less is More”**

Well, “zero” is about as “less” as you can get in terms of putting words to use: a blank sheet of paper if you’re “writing,” total, unbroken silence if you’re “speaking.” Here’s a paradox: either a “zero” writer truly can’t think of anything to say, or is yelling something quite profound from the rooftops.

## **Corollary to Writer's Cliché #1: “More is Less”**

Well, “infinity” is about as “more” as you can get in terms of putting words to use: an essay as large as the Library of Congress if you're “writing,” verbiage of galactic duration if you're “speaking.” Here's a paradox: either an “infinite” writer truly has everything to say about anything and everything, or is yelling something embarrassingly redundant from the rooftops.

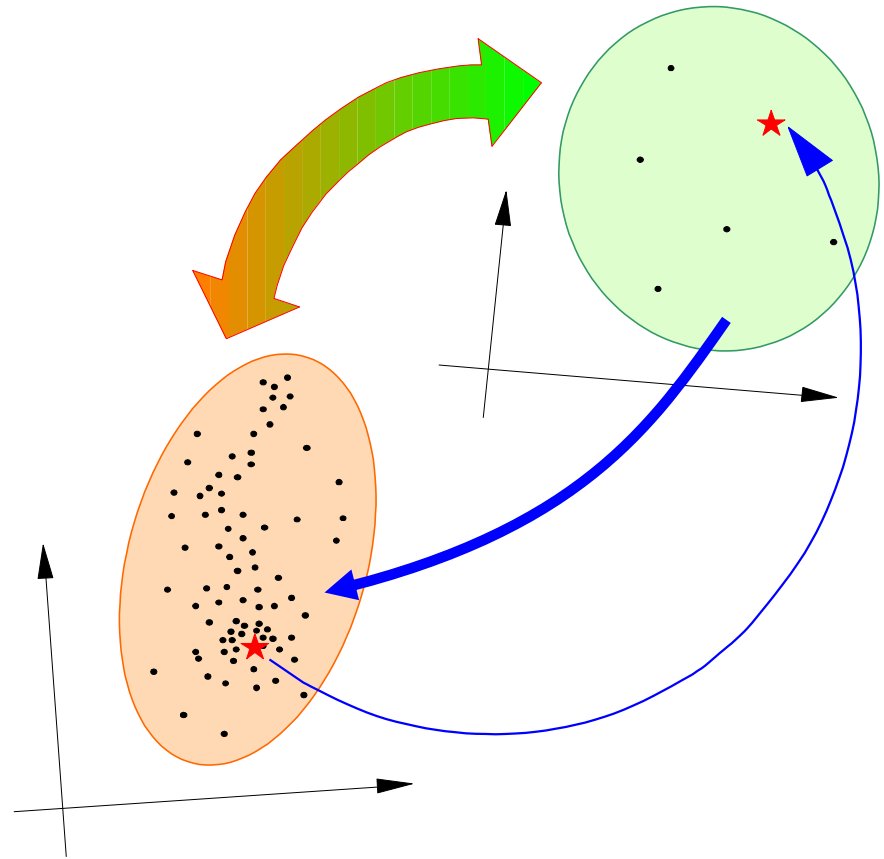
## Space Mapping

(Bandler et al., 1994)

follows the engineer's traditional experience

exploits the engineer's "intuition"

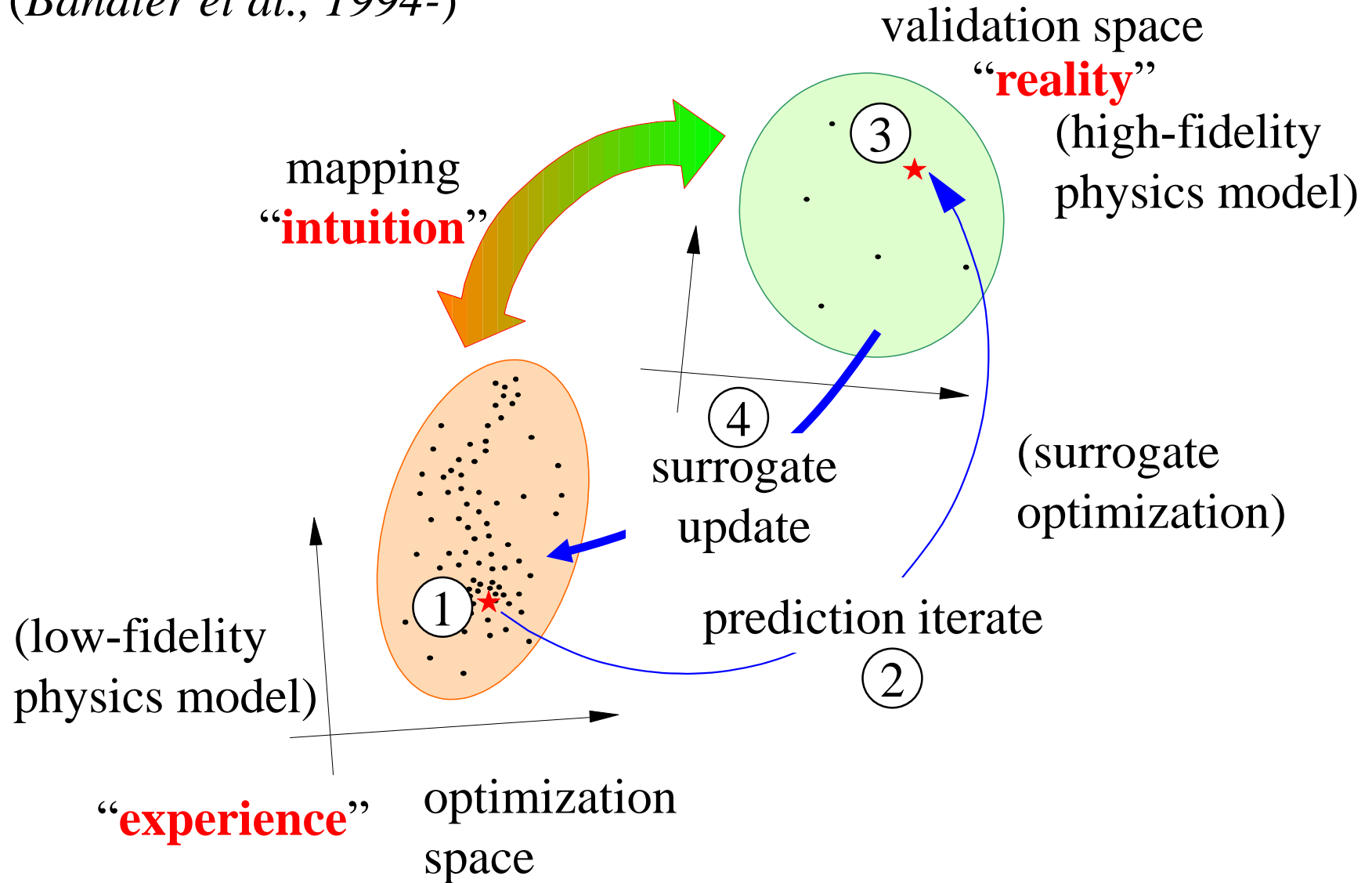
uses iterative enhancement of physics-based surrogates



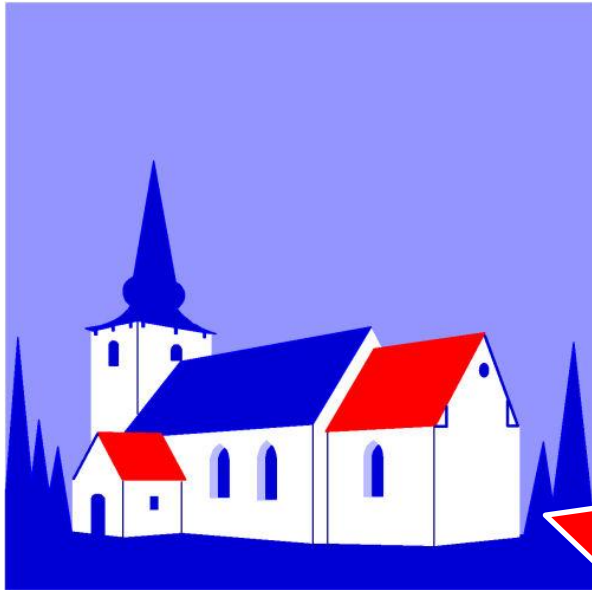
**“space mapping”** offers a quantitative explanation for the engineer's mysterious “feel” for a problem

# The **Space Mapping** Concept

(Bandler et al., 1994-)



**Summer 1993, Near Copenhagen. John Bandler Strolls In A Forest With Mathematician Kaj Madsen . . .**  
**. . . Space Mapping Is Born**



Korning Kirke, Denmark  
—Asbjorn Lonvig, artist



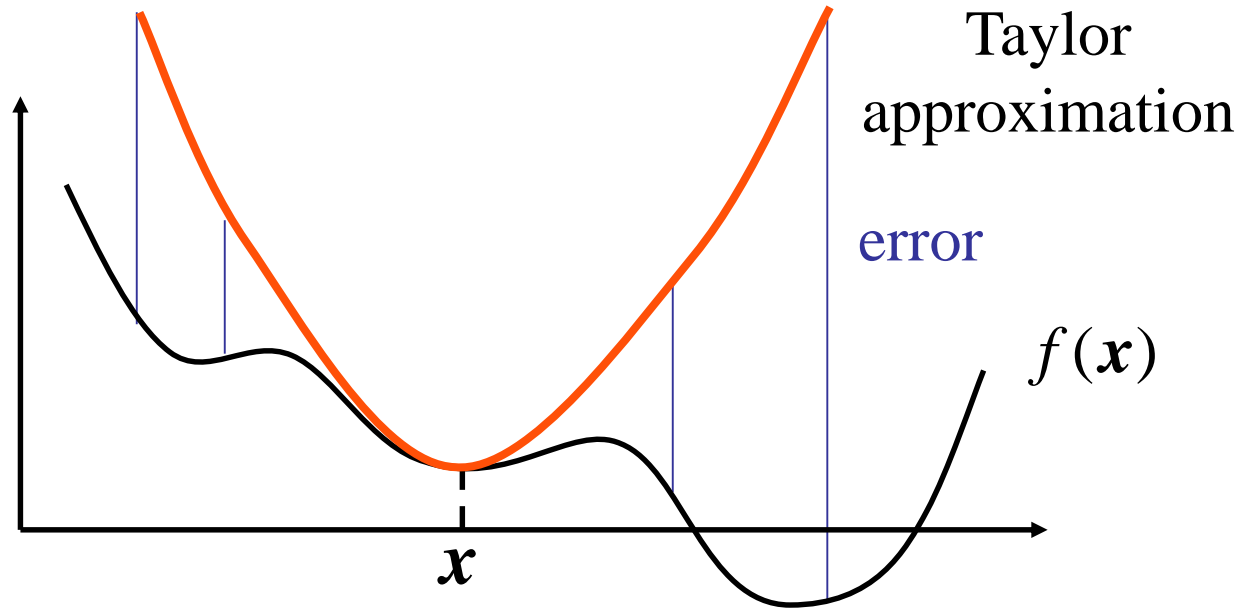
*space mapping*

The cathedral, Cologne  
—historyfish.net

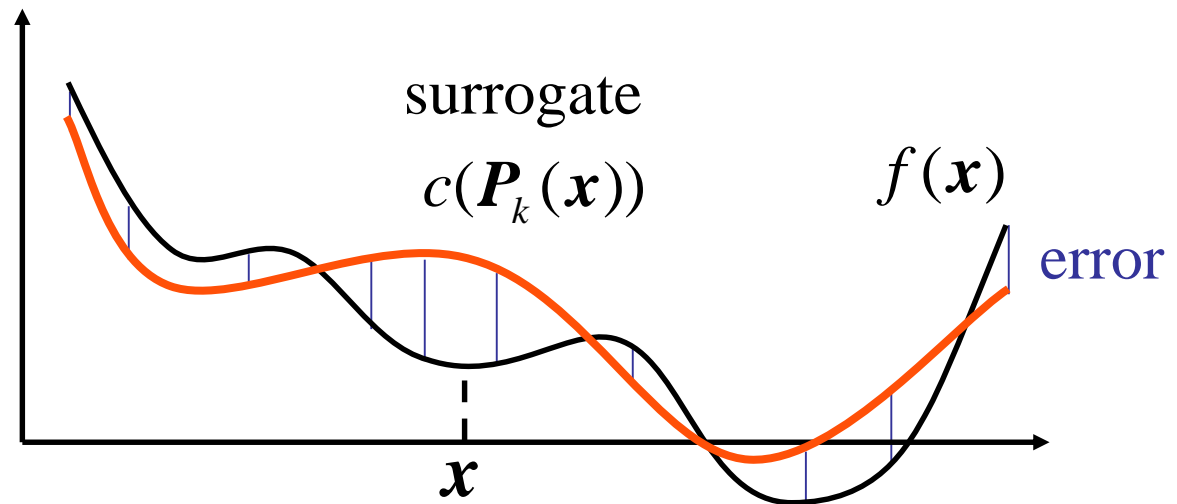
# Space Mapping Optimization Methodologies

(Bakr et al., 2002)

mathematical  
model based on  
local information

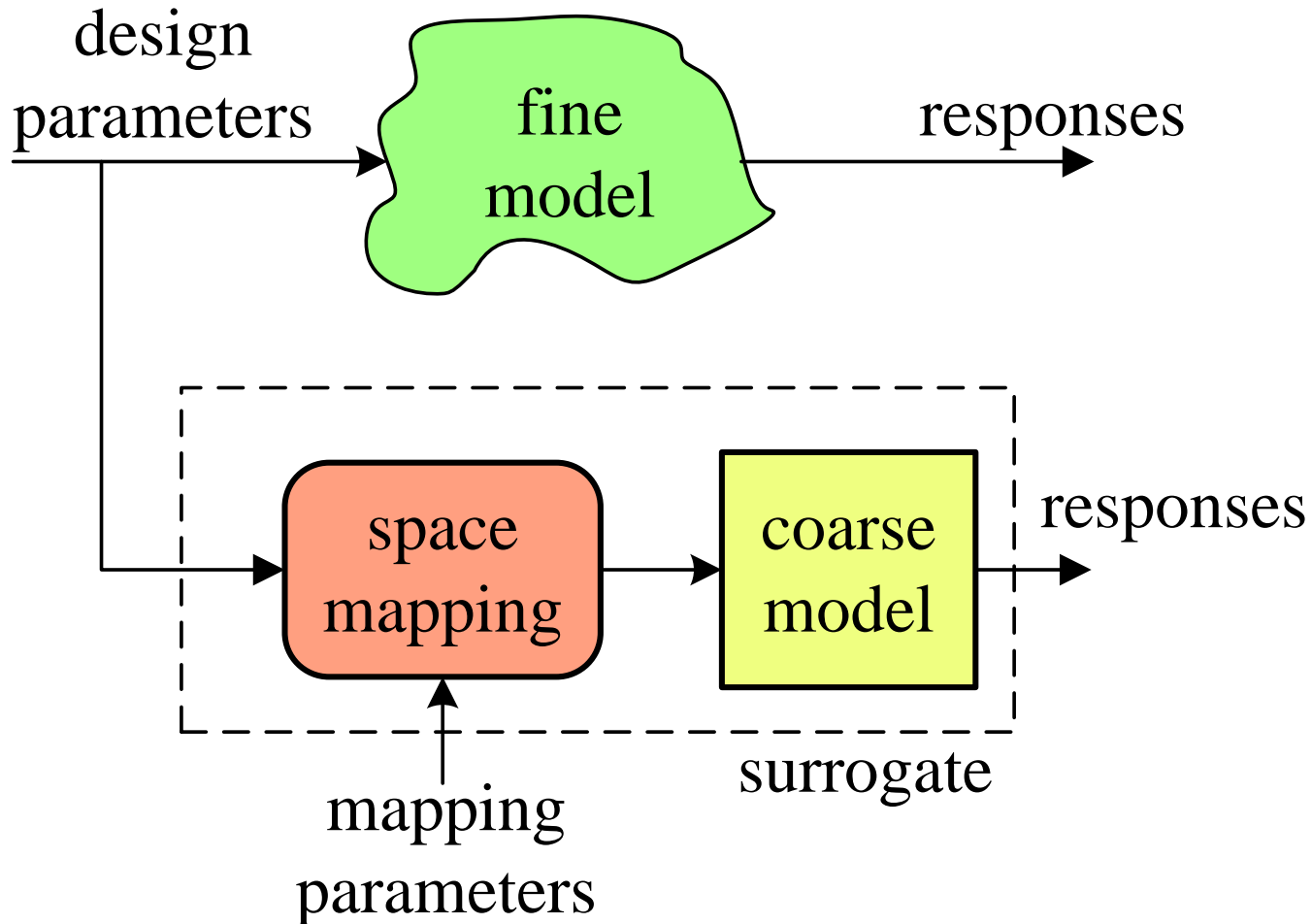


physics-based,  
**space mapping**  
“quasi-global”  
model



# The **Space Mapping** Concept

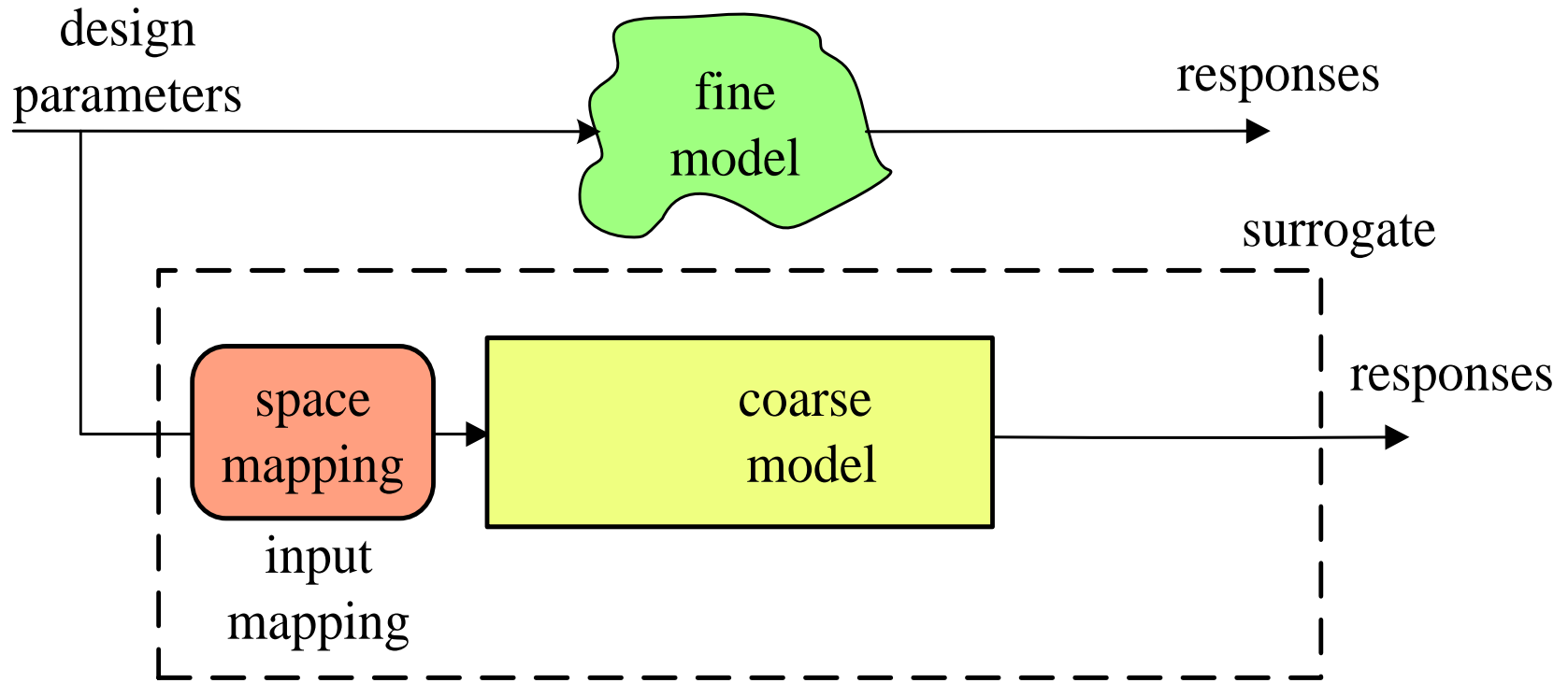
(Bandler et al., 1994-)





# Input Space Mappings

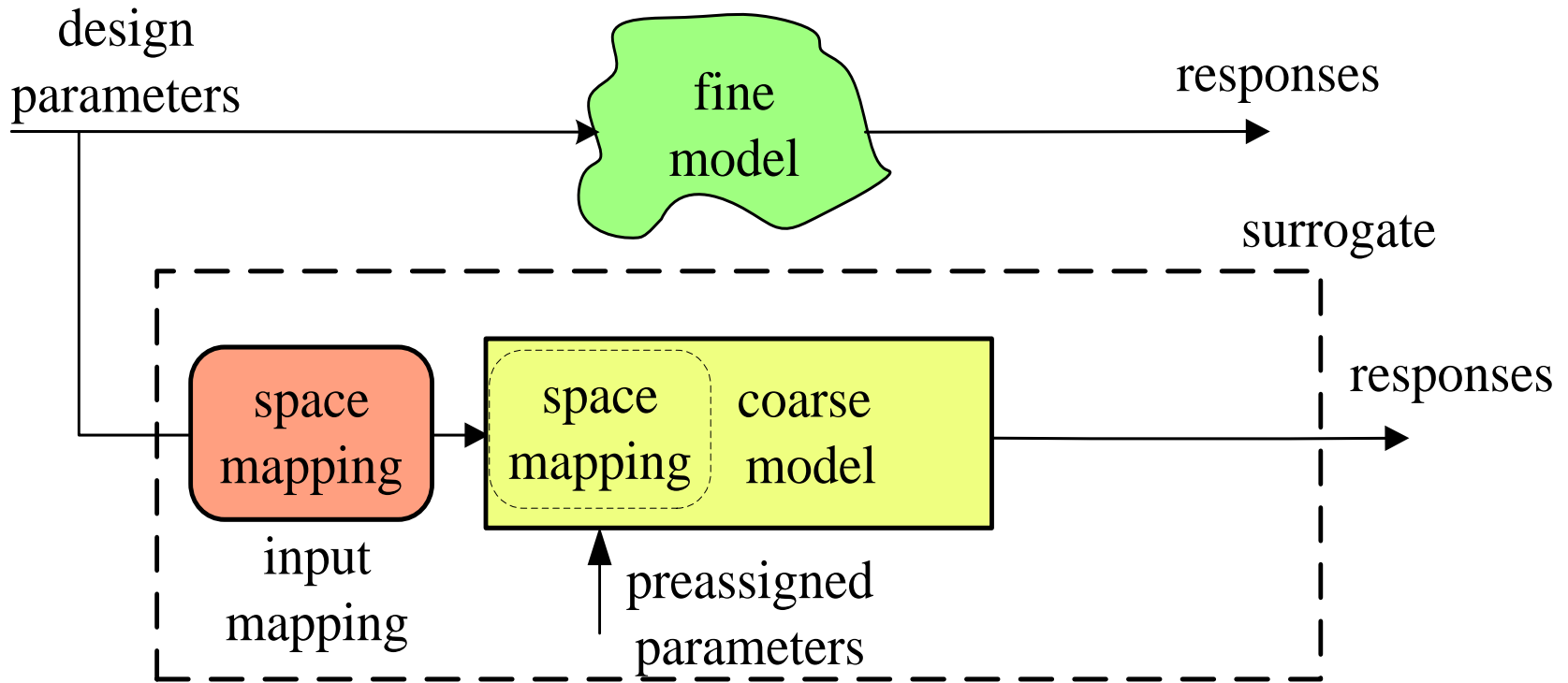
(Bandler et al., 1994-)



expert engineering  
knowledge helpful  
(few designable  
variables)

# Implicit and Input **Space Mappings**

(Bandler et al., 2003-)

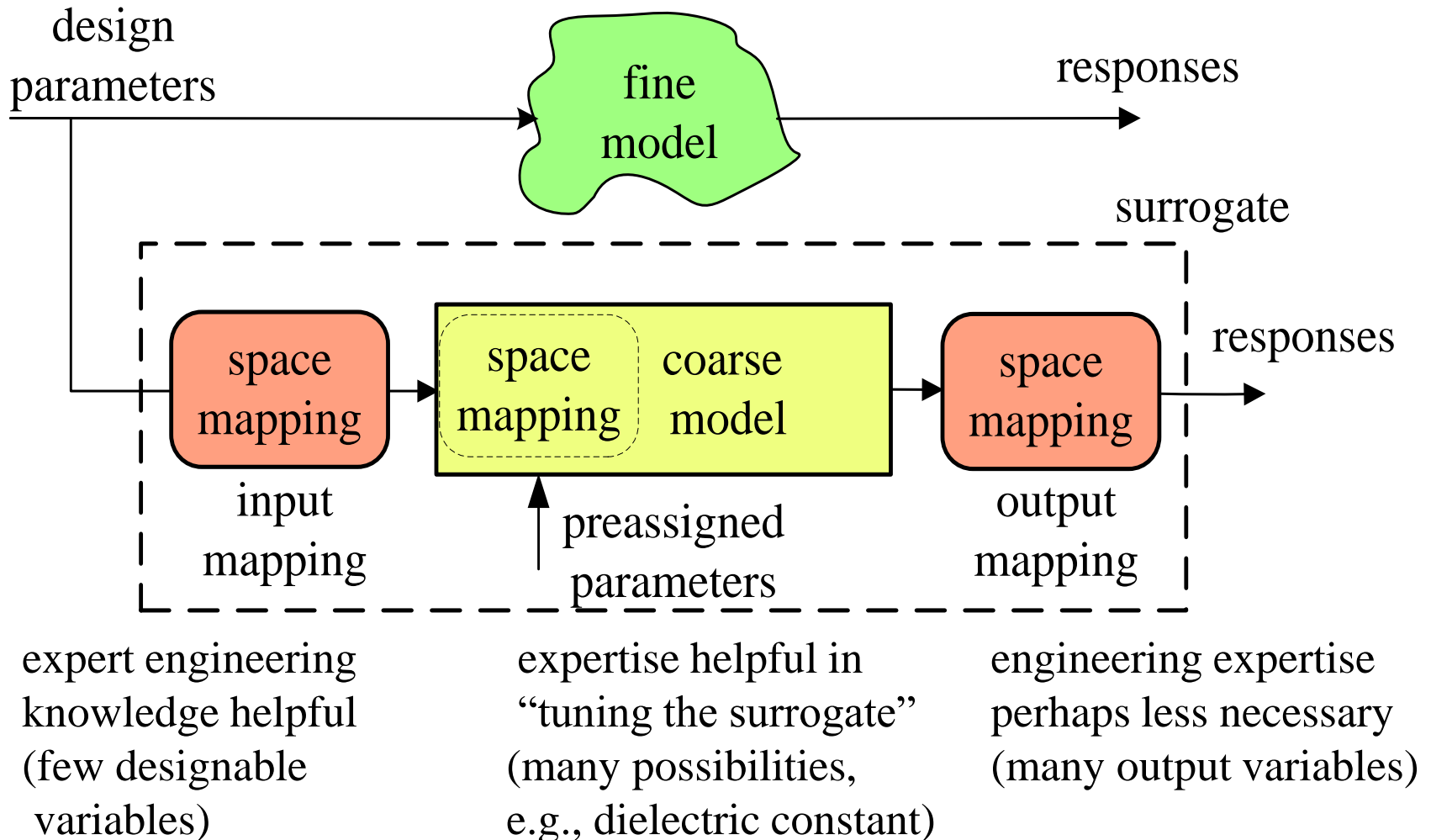


expert engineering knowledge helpful (few designable variables)

expertise helpful in “tuning the surrogate” (many possibilities, e.g., dielectric constant)

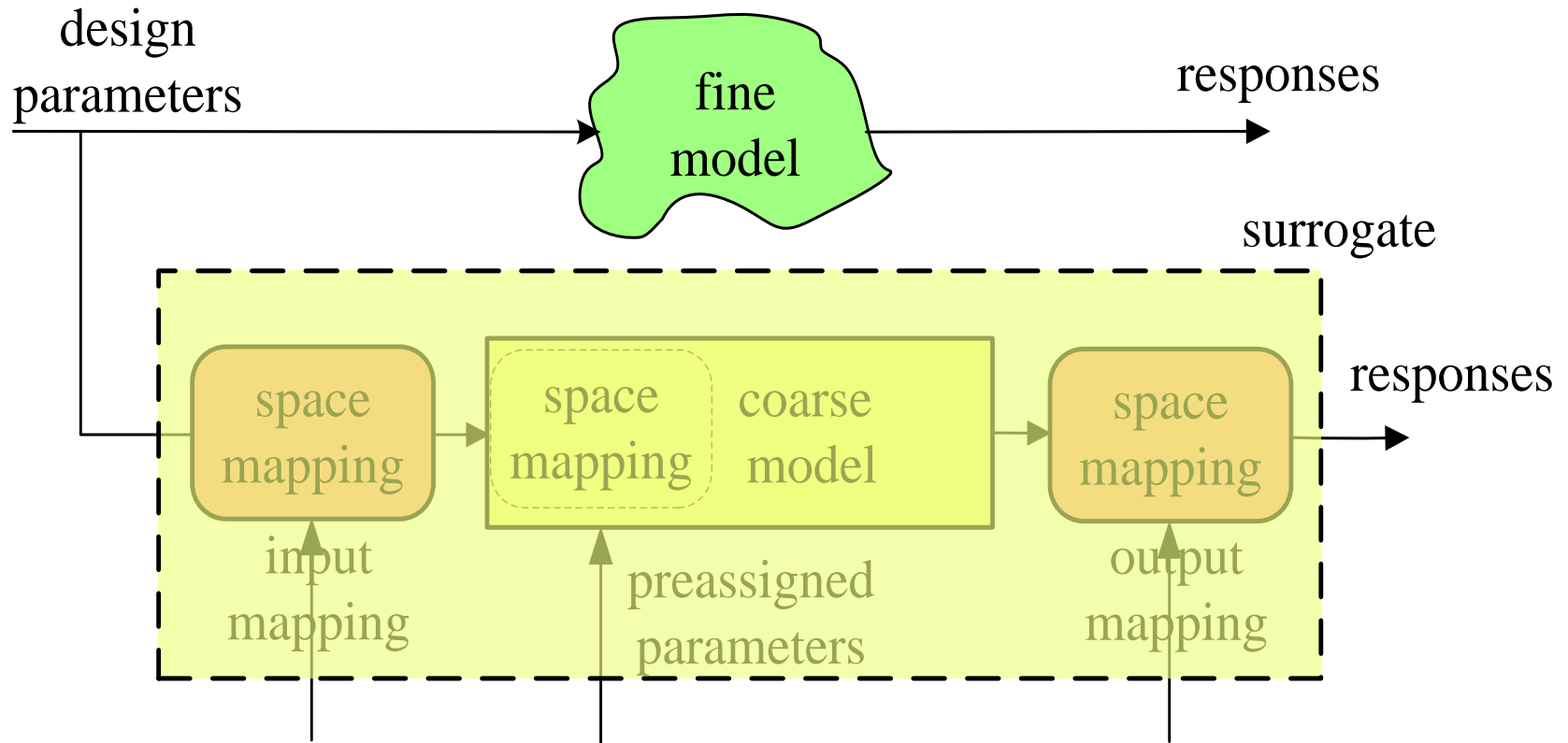
# Implicit, Input and Output **Space Mappings**

(Bandler et al., 2003-)



# Implicit, Input and Output **Space Mappings**

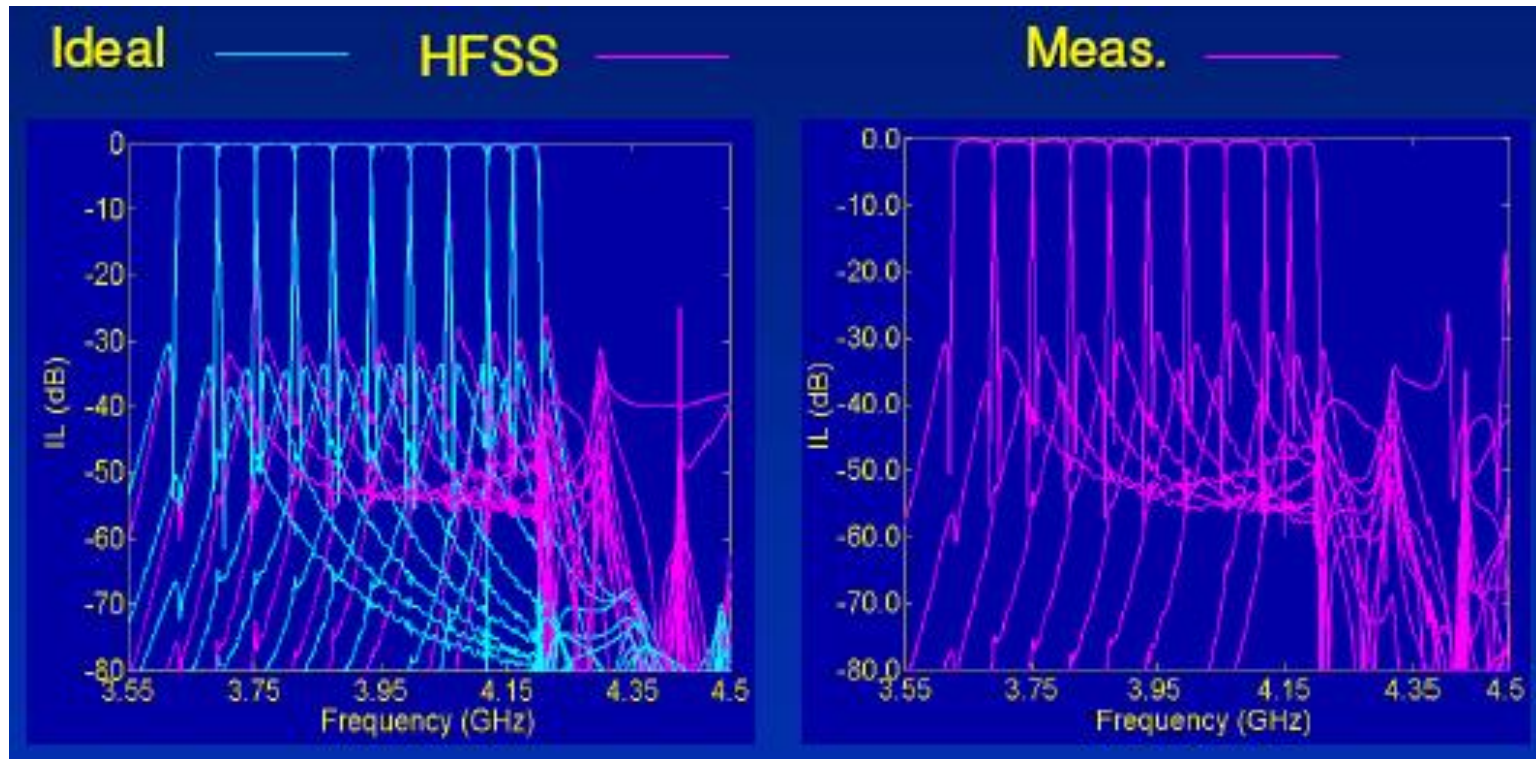
(Bandler et al., 2004-)



but all types of **space mapping** can be viewed as special cases of implicit **space mapping**

# Aggressive Space Mapping Design of Dielectric Resonator Multiplexers (Ismail et al., 2003, Com Dev, Canada)

10-channel output multiplexer, 140 variables



# Space Mapping Crashworthiness Design of Saab 9<sup>3</sup>

(*www.studyinsweden.se, 2005*)

space mapping cuts calculation times by three fourths compared with traditional response surface optimization methods

driven straight into a steel barrier  
at 56 km/h

penetration of the passenger space  
by the material was reduced by  
32 percent





# Twelve Section H-plane Waveguide Filter (Cheng et al., 2012)

HFSS fine model

$$x_f = [L_1 \ L_2 \ L_3 \ L_4 \ L_5 \ L_6 \ W_1 \ W_2 \ W_3 \ W_4 \ W_5 \ W_6 \ W_7]^T$$

(symmetrical w.r.t. the mid-plane septum)

specifications:

$$|S_{11}| \leq 0.075 \text{ for } 5.4 \leq \omega \leq 10.4 \text{ GHz}$$

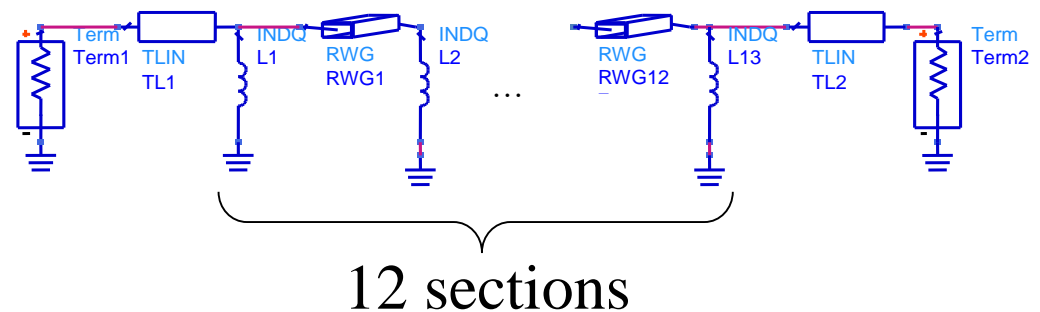
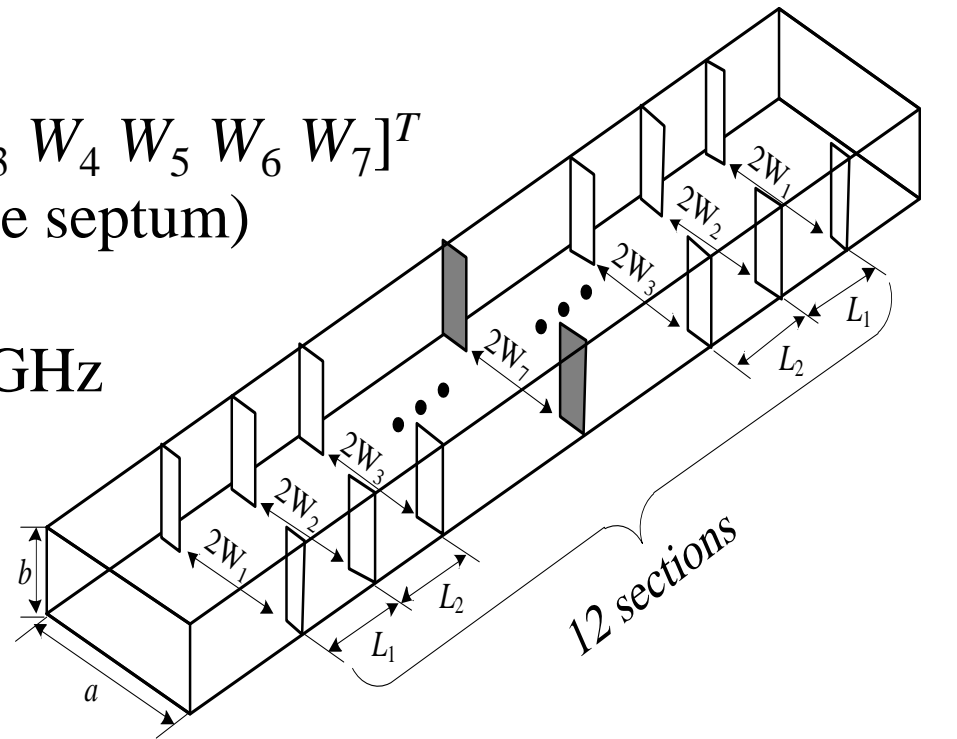
$$|S_{11}| \geq 0.95 \text{ for } \omega \leq 5.25 \text{ GHz}$$

$$|S_{11}| \geq 0.6 \text{ for } \omega \geq 10.7 \text{ GHz}$$

ADS coarse model

preassigned parameters:

section widths and  
frequency coefficients  
of inductive susceptances





# Twelve Section H-plane Waveguide Filter (*Cheng et al., 2012*)

## Modeling Relative Error<sup>a</sup> Using 50 Random Test Points

PE samples (linearly- approximated samples)	+/-5% region	+/-10% region	+/-10% region <sup>b</sup>	+/-15% region	+/-15% region <sup>c</sup>
before PE	120.7%	104.2%	107.4%	95.3%	97.3%
1(0)	6.6%	10.2%	10.4%	14.3%	14.5%
1(13)	6.7%	9.2%	9.4%	13.2%	13.5%
14 <sup>d</sup> (0)	6.6%	9.8%	10.1%	14.2%	14.4%
27 <sup>e</sup> (0)	6.9%	9.2%	8.9%	12.5%	12.9%
27 <sup>e</sup> (27x13)	6.7%	9.2%	9.0%	12.6%	13.1%

a.  $(\|R_f - R_s\| / \|R_f\|)$ ; b. HFSS fast sweep; c. solution frequency at 5 GHz;  
d. half of star distribution; e. star distribution.

# Space Mapping: a Glossary of Terms (*Bandler et al., 2009*)

- space mapping** transformation, link, adjustment, correction, shift (in parameters or responses); “internal” fine-tuning transformation
- coarse model** simplification or convenient representation, companion to the fine model, auxiliary representation, cheap model, “idealized” model
- fine model** accurate representation of system considered, device under test, component to be optimized, expensive model, an optimization process

## Space Mapping: a Glossary of Terms (*Bandler et al., 2009*)

surrogate	model, approximation or representation to be used, or to act, in place of, or as a (temporary) substitute for, the system under consideration
(updated) surrogate	mapped or enhanced coarse model, corrected coarse model, tuning-parameter-augmented fine-model iterate
surrogate model	alternative expression for surrogate
target response	a response the fine model should achieve, (usually) the optimal response of an idealized “coarse” model, an enhanced coarse model, or surrogate

## Space Mapping: a Glossary of Terms (*Bandler et al., 2009*)

- surrogate update** rebuilding of a coarse- or ideal-model-based surrogate using, e.g., parameter extraction; supply new fine-model data to a surrogate
- surrogate optimization** prediction of the next fine model; “internal” fine tuning of a tuning-parameter-augmented fine-model iterate (tuning model)
- parameter extraction** aligning a coarse model or surrogate with the corresponding fine model

# Conclusions

**space mapping** harnesses physics-based “quasi-global” surrogates (knowledge) to achieve fast model enhancements

**space mapping** facilitates full-wave electromagnetics-based as well as multidisciplinary engineering design and modeling

**space mapping** offers a quantitative explanation for the engineer’s mysterious “feel” for a problem

the essence of **space mapping**: less is more

**space mapping** is “elegant”

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