EVALUATING TRUST AND EXPLAINABILITY FOR DEEP LEARNING MODELS

QUANTIFYING TRUST IN DEEP LEARNING WITH OBJECTIVE EXPLAINABLE AI METHODS FOR ECG CLASSIFICATION

BY

KASHIF SIDDIQUI, B.Eng.

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(School of Biomedical Engineering)	Hamilton, Ontario, Canada

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plainable AI Methods for ECG Classification
Kashif Siddiqui
B.Eng. (Electrical & Biomedical Engineering),
McMaster University, Hamilton, Canada
Dr. Thomas Doyle

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Lay Abstract/ Thesis statement

The goal of this thesis was to develop a framework of how trustworthiness can be improved for a variety of stakeholders in the use of AI in medical applications. Trust was broken down into basic elements (Explainability, Verifiability, Fairness & Robustness) and 'Explainability' was further explored. This was done by determining how explainability (offered by XAI methods) can address the needs (Accuracy, Safety, and Performance) of stakeholders and how those needs can be evaluated. Methods of comparison (similarity, stability, and novelty) were developed that allow an objective evaluation of the explanations from various XAI methods using repeatable metrics (Jaccard, Hamming, Pearson Correlation, and TF-IDF). Combining the results of these measurements into the framework of trust, work towards improving AI trustworthiness and provides a way to evaluate and compare the utility of explanations.

Abstract

Trustworthiness is a roadblock in mass adoption of artificial intelligence (AI) in medicine. This thesis developed a framework to explore the trustworthiness as it applies to AI in medicine with respect to common stakeholders in medical device development. Within this framework the element of explainability of AI models was explored by evaluating explainable AI (XAI) methods. In current literature a litany of XAI methods are available that provide a variety of insights into the learning and function of AI models. XAI methods provide a human readable output for the AI's learning process. These XAI methods tend to be bespoke and provide very subjective outputs with varying degrees of quality. Currently, there are no metrics or methods of objectively evaluating XAI outputs against outputs from different types of XAI methods. This thesis presents a set of constituent elements (similarity, stability and novelty) to explore the concept of explainability and then presents a series of metrics to evaluate those constituent elements. Thus providing a repeatable and testable framework to evaluate XAI methods and their generated explanations. This is accomplished using subject matter expert (SME) annotated ECG signals (time-series signals) represented as images to AI models and XAI methods. A small subset from all available XAI methods, Vanilla Saliency, SmoothGrad, GradCAM and GradCAM++ were used to generate XAI outputs for a VGG-16 based deep learning classification model. The framework provides insights about XAI method generated explanations for the AI and how closely that learning corresponds to SME decision making. It also objectively evaluates how closely explanations generated by any XAI method resemble outputs from other XAI methods. Lastly, the framework provides insights about possible novel learning done by the deep learning model beyond what was identified by the SMEs in their decision making.

This thesis is dedicated to my darling fiancée and my loving family I could not have done this without you.

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Abbreviations

Abbreviations

AE	Auto Encoder
AFIB	Atrial Fibrillation
AI	Artificial intelligence
AUC	Area Under the Curve
BERT	Bidirectional Encoder Representations from Transformers
BW	Box-and-Whisker plot
CMA	Canadian Medical Association
CNN	Convolutional Neural Network
DARPA	Defense Advanced Research Projects Agency
DC	Direct Current
DCN	Deep Convolutional Network

DL	Deep Learning
DNN	Deep Neural Network
ECG	Electrocardiogram
E_xai	XAI Trustworthiness Vector
\mathbf{GC}	GradCAM
GC++	GradCAM++
GL	Global (vs. see LO)
GSVT	Generalized Supra-ventricular Tachycardia
HC	Healthcare
IMG	Image
IN	Inherent (vs. see PH)
IQR	Interquartile Range
K₋n	Knowledge (Novelty)
LO	Local (vs. see GL)
LOESS	Local polynomial regression
MA	Model Agnostic (vs. see MS)
MITBIH	Massachusetts Institute of Technology-Beth Israel
ML	Machine Learning

 \mathbf{MS} Model Specific (vs. see MA) NHS National Health Service NLM Non Local Means NN Neural Network OTSU Thresholding method named after Nobuyuki Otsu PCr Pearson Correlation Post Hoc (vs. see IN) \mathbf{PH} RELU **REctified Linear Unit** ResNet **Residual Network** Recommended (Overlooked learning) $R_{-}u$ \mathbf{SB} Sinus Bradycardia SME Subject Matter Expert SmG SmoothGrad Snomed CT Systematized Nomenclature of Medicine - Clinical Terms \mathbf{SR} Sinus Rhythm TAB Tables **TF-IDF** Term Frequency - Inverse Document Frequency TSE Technical Self Efficacy

T_xExplainability ScoreVanVanilla SaliencyVGG-16CNN named after Visual Geometry Group from OxfordWFDBWaveform DatabaseWMDWeapons of Mass DestructionXAIExplainable AI

Chapter 1

Introduction

AI is becoming an invaluable tool in the decision making processes in healthcare. Quite often the safety risk associated with an AI's decision is low, this is definitely not the case in healthcare [2]. Human lives can be severely impacted by the decisions made by an AI. As a result the level of trust required in AI is extremely high. There are many challenges to achieving this high level of trust between the various stakeholders and the AI [3].

1.1 Problem Statement

The goal of this research is to gain insight into how deep learning models are making decisions for different user types and to quantify the features of importance. By improving the understanding of an AI model's decisions we can increase a user's trust in how the model identified features are contributing to outcome decisions.

To provide overall context this thesis will present a framework to define Trust

and its individual constituent elements: Explainability, Verifiability, Fairness, & Robustness (Section 2.1.2). Within these elements of trust, "Explainability" will be the focal point of the exploration within this thesis. This body of work will examine how explainability ties into trust, and how this particular component of trust can be quantified for comparisons between different methods of explainability.

In the context of Artificial Intelligence, **explainability** refers to the act of explaining an AI's learned processes. The explanations of AI decisions are provided by Explainable AI (XAI) methods [4,5].

Producing objective and quantifiable measurements of various explanations generated by different XAI methods allows these otherwise subjective explanations to be compared. Current literature provides some insights into smaller testable constituents of explainability: *Similarity, Stability, Novelty* (see Section 2.1). This thesis hypothesizes that by measuring these constituents of an explanation, it can be quantified and therefore compared with other explanations. This allows an objective framework to evaluate the quality of an XAI method.

1.2 Overview

This overview will first examine stakeholder attitudes toward AI, introduce a medical application for study, and present findings from a literature scoping review as a gap analysis.

1.2.1 Attitudes on AI & XAI

To explore the attitudes of clinicians and patients towards AI adoption we must first strive to understand the primary variables responsible for an individual adopting a position in favour of or against a specific technology. New models of user technology adoption suggest that the primary variable is technical self-efficacy (TSE) and it describes the level of comfort a user feels towards using a specific technology [6]. Other predictive variables include things like perceived usefulness and ease of use of technology, as well as perceived risk from a technology [6] [7]. Any exploration of attitudes toward AI adoption should consider these factors as integral towards developing an understanding of what steps need to be taken to improve user adoption.

Clinician Attitudes

A NHS funded study found that a majority of the clinical experts surveyed report never encountering any AI applications at work [8] see figure 1.1. Even with combining those clinicians who report encountering one or more AI applications at work, the overwhelming majority claim poor technological literacy, low levels of TSE, with fewer than 13% of the respondents being able to distinguish between 'Machine learning' and 'Deep Learning', see figure 1.2 [8].

While a sense of comfort with the use of AI tech maybe lacking among medical professionals, other variables like perceived usefulness are high and perceived risk is relatively low [8]. About 4 out of 5 medical professionals believe AI would be useful in their particular line of work, and almost everyone surveyed expresses no concerns with AI replacing their roles at work [8]. As a whole the majority of medical

professionals express some concern regarding privacy laws especially with the rollout of privatized AI applications [8] see figure 1.3. When medical doctors and other medical professionals were specifically asked about their level of fear towards AI, framed as AI being a bigger threat than WMDs, Medical doctors almost entirely rejected the concern that AI is a bigger threat than WMDs but the larger medical community sees AI as a significant threat see figure 1.4 [8].



Figure 1.1: Clinician attitude - How many AI applications are encountered at work







Figure 1.2: Clinician attitude - Knowledge about the differences in DL and ML



Figure 1.4: Clinician attitude - Do you Fear AI

The largest obstacle that remains between clinicians and full integration of AI applications in daily work is a sense of trust towards the technology. While this notion of trust will likely improve with improved TSE with AI. There are methods to improve

the level of trust a clinician is willing to put in AI, by improving interpretability and explainability of AI decisions [3]. Most clinicians can recognize the benefits from advances in AI as they relate to more precise patient care and improved utilization of data generated worldwide [2] [8]. If the barriers to trust are going to be lowered, and clinicians made more willing to embrace the AI technology, efforts need to be focused on understanding trust and addressing the various components of trust.

General Public Attitudes

In the NHS survey [8] a small distinction between medical doctors and the larger medical community was made with the question regarding level of fear with AI. While medical doctors are relatively certain in not being afraid of AI, the larger community of people expressed a bit of fear see figure 1.4 [8]. In an Canadian Medical Association study of over 2000 respondents, conducted as a survey by Ipsos [1], a majority (57%) expressed an excitement about the future of AI used in healthcare. An overwhelming majority (77%) want to see more technological investments in healthcare, with 69% of the respondents believing that AI could address the challenges facing healthcare [1], see Figure 1.5.

When looking at the questions in the study [1], organized by views on utility, sense of trust in AI and concerns regarding AI, see figure 1.5, a pattern emerges. The general public is excited about the prospect of AI being of aid in healthcare and helping us address the challenges facing our modern health concerns. At the same time there is an obvious element of mistrust when physicians are out of the loop or privately managed healthcare services and health monitoring devices are powered by AI alone. There is a deeper sense of distrust when it comes to services and offerings by



Canadian Medical Association Survey by Ipsos

Figure 1.5: Summary excerpt of the CMA survey by Ipsos - 2018 [1] on attitudes of the Canadian public towards use of AI in Healthcare. *HC = Healthcare, AI = Artificial Intelligence.

the private sector in society that translates to a mistrust of the newer AI technology, especially if Physicians are kept out of the loop [1] [9]. There is an 'canonical' sense of trust that exists between the patient and their physician that has been built over a long history of patient-doctor interactions [9]. Part of this trust is grounded in the basis of expert knowledge on the part of the physician.

In reference to the use of AI in healthcare, to an average patient, the physician is expected to do more than just convey the findings of the AI. Rather a physician's role is seen as more of an intelligent expert user who can critically assess the recommendations of an AI and guide the patient so they may receive the best care possible [9]. This expectation on the part of the patients also means that there is an expectation by the physicians to be able to get insights from AI with some explanation and certainty [10] towards why those decisions are made. These relationships of trust between the AI, the physician, the patient and a few other stakeholders are explored in this thesis in the Section 2.1.

1.2.2 Healthcare Application

The healthcare application used in the process of this thesis is classification of a limited set of cardiovascular conditions using the ECG signal records from patients with 2-4 leads of data. The cardiovascular rhythms (conditions) included in this thesis are: Atrial Fibrillation (AFIB), Generalized Supraventricular Tachycardia (GSVT), Sinus Bradycardia (SB), and Sinus Rhythm (SR).

However, this research is applicable to any complex health data to which Deep Learning methods are applied.

1.2.3 Gap analysis

Benefits: Due to the volume of XAI generated explanations, especially as visualizations (image based explanations) there is a significant amount of coverage in literature of the utility XAI generated explanations offer to healthcare professionals [10]. There has been a lot of ground work done in determining and understanding the opinions of clinicians and lay-persons as they relate to AI models and explanations of said AI models used to justify the AI's decisions [2,8,10]. These works help identify the thinking patterns of stakeholders involved in using AI tools in healthcare, and help guide the direction of research for this thesis to identify what gaps in current knowledge and tools may exist.

Gaps: There are quite a few shortcomings in the current literature regarding XAI.

There are numerous definitions and taxonomies that result in a varied approach to the idea of generating explanations for an AI's black-box [11]. While having a multitude of approaches to elicit an explanation is advantageous as it provides a multi-dimensional view of the same processes, this raises the question of which explanation is objectively better, if any, and is there a way to compare the explanations with human performance and against other XAI generated explanations. While the idea of missing objective evaluation of explanations has been raised before [11], there are no known attempts to our knowledge that have aimed to functionally evaluate XAI generated explanations.

Aside from lacking any objective evaluation of the explanations generated by XAI, another gap is the lack of evaluation of the performance of the XAI methods in relation to clinical tasks they are sometimes used for [10]. Often when an XAI method is proposed there maybe some suggestion by the authors of how XAI method may aid in evaluating certain AI models on a specific clinical task [12, 13]. The amount of effort needed to explore the possible and useful XAI explanations for any given AI model for a specific clinical task is tremendously high.

1.3 Proposed solution

This thesis investigates if qualitative explanations of AI's learned processes can be quantified and objectively compared with other explanations. This investigation is performed using the learned processes of an AI classification model for cardiovascular rhythms.

This thesis:

Proposes a framework to examine any explanation using: similarity, stability & novelty.

- 2. Develops an AI model to perform classification of cardiovascular rhythms.
- 3. Generates a number of explanations from multiple XAI methods for the developed AI model.
- 4. Implements the proposed framework to quantify the qualitative explanations.
- 5. Tests the performance of explanations against each other as well as against the gold standard [human subject matter expert (SME)] explanations.

In performing the comparisons between explanations generated by various XAI methods and SME, investigating what remains *unlearned* by the AI is explored. This unlearned component is added to the framework in addition to similarity, stability & novelty.

1.4 Contribution

To the growing field of research in AI models in healthcare as well and XAI methods, this thesis contributes:

• A framework to evaluate trust in AI by examining qualitative explanations in quantifiable ways, based on the needs of stakeholders in the healthcare system.

1.5 Thesis Organization

The Figure 1.6 shows a visualization of a connected process: beginning with defining a healthcare application; identifying modelling question(s) and data type used for analysis; identification of relevant AI model(s); selection of appropriate explainable AI (XAI) method(s), and finally quantifying the XAI's performance to improve the overall state of trust in the entire process.



Figure 1.6: Visualization of overall journey of the thesis - Specifically dealing with the AI model in this section.

This thesis is organized as follows (components of the thesis are shown visually in Figure 1.6):

- 1. Literature Review Presents a brief overview of the state of AI and XAI in contemporary research literature.
- 2. Domain Data A detailed description of the data used in this thesis.
- 3. AI Model Development and evaluation of the AI model that will be applied to the domain data and evaluated using XAI methods.
- XAI Methodology Selected XAI methods and how they are evaluated.
 Results XAI generated explanations and results.
- 5. Quantifying Trust Using trust metrics to evaluate the process.
- 6. Discussion A discussion of results and their implications.
- Conclusion & Future Directions A summary of the thesis outcomes and next steps.

Chapter 2

Literature Review

This chapter discusses the current literature on the topic of trust and verification in AI. This literature review is performed in three stages: i) Identification stakeholders to understand concerns of users, ii) Elements of trust and verification of AI are extracted from literature to define parameters for the tools from the first stage, and iii) Algorithms and tools are identified for trust and verification of AI within the parameters as set by the second stage.

The goal of this review is to create a guide that consolidates information on state-of-the-art artificial intelligence (AI) & machine learning (ML) models, along with interpretable & explainable AI (XAI) methods and relates this information to various categories and disciplines in healthcare as shown in Figure 1.6.

In addition, the review will present a summary from literature of perceptions of trust towards AI. Finally, an equation framework to quantify trustworthiness of AI models used for problem solving in healthcare will be defined.

2.1 Trust in AI

As discussed in Section 1.2.1 there are a myriad of interactions and complex relations of trust between different types of stakeholders when it comes to the use of AI in healthcare. This section discusses the stakeholders, the elements of trust and how those elements of trust interact with the individual stakeholders affecting their levels of trust in the use of AI in healthcare.

2.1.1 Stakeholders



Figure 2.1: Visualization of various stakeholders in the use of AI in medicine

The first step is to identify and understand the stakeholders that are affected by the AI and its decision making. In Section 2.1.3 the individual concerns of of each stakeholder are explored in more detail. Based on broad evaluation of the literature [14–20] provide context for what a framework of AI systems and XAI methods need to provide users. Literature identified users, ranging from AI experts and subject matter experts to more general lay-persons; Each user type may need to interact with AI systems at different levels but may not posses the expertise required to analyse the performance

of the AI or the AI's decisions. Lay-persons, as shown in Figure 2.3, range from regulators [14, 17, 19] (responsibility to ensure transparency in AI decisions) to more naive users (may only interact with the end output an AI decision making system produces). For example, these naive users may be the technical staff or employees [15, 18, 19] [16] who operate the machines or systems with the AI. The final naive user class is the client [14, 16, 17] who may only ever receive the final decisions made by the AI system and have little to no contact with the AI itself.

While the literature discusses the generalized case of stakeholder classes and their relative concerns. For the purposes of this thesis those stakeholder groups were translated to general groups that are more relevant to the healthcare industry. As shown in Figure 2.3 the experts are more distinctly defined to be Developers (AI experts) and Physicians (subject matter experts). While various types of academics (subject matter experts) may exist in the field of medicine, for simplicity only the physicians are mentioned on the figure. The naive users are also more granularly defined to be Medical technicians (technical staff or employees), and this category may also include administrators or nurses. Finally the last type of naive stakeholder in the healthcare industry is the patient (clients).

2.1.2 Elements of Trust

An important step in the path to improve trust for different types of stakeholders when it comes to the use of AI in healthcare, is to understand the word "trust" itself. The first step is to understand the general concepts of trust as they pertain to human interpersonal interactions. According to Ferrario et al. [21], trust between people exists in a variety of contexts and people have specific concerns they want addressed



to achieve said trust, these concerns are discussed in more detail in Section 2.1.3. The "contexts" within which trust is developed are concepts like *reliability* where if one party is able to demonstrate some consistency in how it performs a task, other parties learn to trust it in the context of reliability, even if it may not be trustworthy in other contexts [21, 22]. There are many other contexts like *transparency* and *fairness*, as well as being able to convey ones knowledge or *mastery* of a subject. These "contexts" of trust often have many overlapping definitions and are represented in a myriad of ways between literature [4, 5, 21]; Just as they apply to people they can be similarly applied to developing trust between humans and AI [21]. This thesis aims to reduce a large number of concepts within which trust is developed into four distinct elements, and discuss what overlap may exist between them (in Section 2.1.3.

As shown in Figure 2.2 the myriad concepts discussed in [4,5,21,22] can be summarized into the four elements: Explainability, Verifiability, Fairness and Robustness.

Explainability allows an individual to comprehend what an AI has learned. This requires the AI being able to show its inner thoughts in its decision making process [4] [5]. This element of trust, explainability, is the prime focus this thesis as mentioned in the problem statement.
Verifiability allows the user to trust the decisions made by the AI because this element conveys that the current state of the AI has been validated by some expert [22] and the decisions it makes have some human oversight to ensure adequate rules and regulations for safety are followed [5].

Fairness as an element of trust it's easy to grasp that an individual would be more trusting of an AI that makes fair decisions [4,5,14,20,21]. The trust in an AI's decisions by evaluating its fairness are affected by the individual need for correcting past inequities and the need for justice, which are prime reasons for why AI is even considered by many users as a new decision making paradigm in the first place [5]. Therefore, it is vitally important that an AI and its decisions be demonstrably fair to allow stakeholders to trust the AI's decision making.

Robustness deals with the concept of consistency in the AI's decision making especially as equipment, sensors, processors, and other hardware may change, as well as human subjects that data might be gathered from [4] [5] [16] [20]. This element of trust also conveys how much of a material improvement an AI produces in decision making in various different settings [4].

2.1.3 Impact of Elements of Trust

In the process of identifying the relevant stakeholders and understanding the elements of trust, the individual concerns of stakeholders to achieving trust become an important factor [4] [5] and they are what connect the stakeholders to the elements of trust.

The literature that was surveyed to develop an understanding of stakeholders and the elements of trust for this thesis, naturally provided the discussion that lead identifying five concerns that impact various stakeholders. These concerns are as shown in Figures 2.3 & 2.4; accuracy [14] [16] [20] [4] [5], safety [17] [20] [22] [4], performance [14] [16] [20] [4] [5], transparency [14] [17] [20] [4] [5], & compliance [14] [17] [19] [22].



Safety
Performance
Transparency
Compliance
Figure 2.4: Elements of Trust (columns) an

Verifiability

Fairness

Robustness

Explainability

Accuracy

Figure 2.3: Stakeholders (columns) and their concerns (rows)



Accuracy refers to the general need for correct decisions made by the AI to have any semblance of trust [4,5,14,16,20]. This concern is common for all stakeholders, shown with check-marks in Figure 2.3. Accuracy can be demonstrated by an AI that is Explainable and Fair, shown with filled in coloured boxes in Figure 2.4. The two Figures 2.3 & 2.4 show that when it comes to trusting AI decisions, all stakeholders are concerned with the AI being accurate and that the need for accuracy means they are all concerned with the trust elements of Explainability and Fairness [4,5].

Similar comparisons between all other concerns in Figures 2.3 & 2.4 can be made, to understand how stakeholders and the elements of trust are related.

Safety as a concern is about ensuring the behaviour of the AI remains consistent from one instance of implementation to another [4, 17, 20, 22]. That regulators can

ensure the AI decision making meets standards that would apply to conventional machines or operators [17,20]. And that the decision making processes of the AI can be clearly explained when needed to ensure safe operation [20] [4].

Performance related concern is that AI needs to outperform a human or the conventional machine/tool in use currently, to justify the need for an AI based solution. This is a unique concern for only subject matter experts and AI experts [4, 5, 14], only the developers are concerned with making an AI that can compete with the current standards and subject matter experts are concerned with improving workflow. **Transparency** refers to the need to demonstrate that the AI's decision making is both fair and consistent. But the need for fairness here is distinct from the need to have an explainable AI [20]. The need for transparency exists for almost everyone who engages with the AI on some technical or operational level [4, 5, 20]. Technical users, regulators and experts want to ensure that all the decision making processes are testable and repeatable, something that comes with transparency. In literature explainable and transparent AI are used almost interchangeably [20], but this thesis separates the two ideas into two distinct axes to be able to better understand the distinctions between transparent AI and explainable AI and how each may relate to other elements and stakeholder concerns.

Compliance is a very narrow concern, but its very important to actually making an AI that can be trusted. Regulators and developers play an integral role in making sure an AI and its decisions remains trustworthy. To this effect, both of these stakeholders are concerned with ensuring that the AI systems being built remain compliant with various standards in the respective industries. This means that an AI has to be able to generate a verifiable audit trail of its decision making processes to be considered trustworthy [4, 5].

2.2 AI in Healthcare

2.2.1 AI Systems in Use

After understanding the point of view of stakeholders and their concerns regarding trust in AI. The next step is to understand on what is the AI doing and how its addressing problems in the field of Healthcare specifically.



Figure 2.5: All the Artificial Intelligence/ Machine Learning models

The AI hierarchy structure is adopted from DARPAs organization of relationships between AI algorithms [15]. Individual Neural Networks (NN) shown in Figure 2.5 are taken from the Asimov Institute's overview of NN taxonomies, which list stateof-the-art as well as historical networks, many of which are still in use [23]. Specific variants like U-Net (CNN), ResNet (DNN), BERT (AE) are not discussed because the scope for thorough coverage is too large & impractical for this review.

The Figure 2.5 aims to sort the myriad machine learning models into 6 total categories and the Neural Networks category is split into two separate groups; commonly used NNs vs uncommon NNs (top and bottom respectively). This separation on common vs uncommon use is based on whether a model provided any search results when searched in conjunction with Healthcare categories or healthcare disciplines shown in Tables 2.1 & 2.2 respectively in the pubmed database. Important to note that this separation does not suggest a conclusion that uncommon NNs could and/or would never be used for solving healthcare problems, rather an organizational artifact borne of a noted effect during literature search.

2.2.2 Utility of Various AI Types

Table 2.1: Categories of Health Applications with Relevant AI & Data Types in Literature

Categories of Care	AI	Data Type	Source
	RNN	GRAPH	[24]
	LSTM	GRAPH	[24]
	GRU	GRAPH	[24]
	MCMC	GRAPH	[24]
	BN	TAB	[25]
Robot-assisted Surgery	CNN	TIME SERIES	[26]
	CNN	TAB	[27]
	GAN	IMG	[28]
	SVM	TAB	[29]
	Logistic Regression	TAB	[29]
	k-NN	TAB	[29]
Virtual nursing Assistant	CNN, AE	TEXT	[30]
	RF	TAB	[31]
	XGBoost	TAB	[31]
	AdaBoost	TAB	[31]
Administrative workflow	Logistic Regression	TAB	[32]
	Logistic Regression	TIME SERIES	[33]
	FF	TIME SERIES	[33]
	BN	TIME SERIES	[33]
	Preceptron	TAB	[34]
	SVM	TAB	[34]
	Logistic Regression	TAB	[35]
F	BN	TAB	[35]
Fraud detection	RF	TAB	[35]
	Classification Trees	TAB	[34]
	k-NN	TAB	[34]
	DBSCAN	TAB	[34]
	FF	TAB	[36]
	RF	TAB	[37]
Medication Management	Undisclosed (Private)	TAB	[38]
	Decision Trees	TAB	[39]
	RF	TAB	[39]
	DRL	TEXT, TAB	[40]
Clinical Trial Participation	AE	TEXT	[40]
	CNN	TAB, IMG	[41]
<u>a</u>	ANY	TAB	[42]
Cybersecurity	ANY	TAB	[43]
Wearables and Monitoring	ML	TAB, TIME SERIES	[44]
Diagnositics	SEE TABLE 2.2		

Table 2.1 shows the various categories of healthcare and related AI models used in literature and identified by [45] as important categories for AI implementation in healthcare. Table 2.1 also shows the type of data used as inputs for the various AI models. The relevant references for each combination are also included in the table.

Table 2.2: Healthcare Disciplines with Related AI, Data types and Tasks in Literature

Healthcare Disciplines	AI	Data type	Task	Source
Allergy and Immunology	CNN	TAB	Using Deep learning to predict the syntax regulatory pathways used by the immune system	[46]
Anesthesiology	DL	TAB	Surgical decision making automation	[47]
Cardiology	CNN, DCN, ML	ANY	A review on diagnostic, and decision making AI available in the cardiovascular domain	[48]
Dentistry	ML	ANY	Improving reliability, reproducibility, accuracy and effectiveness in dentistry	[49]
Dermatology	DL Ensemble	IMG	Detecting and Assessing Melanoma in Skin Lesion Images	[50]
Diagnostic Radiology	CNN, DCN,ML	IMG	Review on Image segmentation and classification of tumors and other radiological findings	[51]
Endocrinology	Undisclosed (Private)	TAB	Optimizing insulin pump dosage compared to an expert physician	[38]
Emergency Medicine	DNN	TAB	Predicting clinical outcomes in emergency triage systems	[52]
Gastroenterology	RF	TAB	Predicting patients who will likely respond to a long term Crohn's treatment	[37]
Gerontology	RF	TAB	Analyzing gene expression to predict heart failure verified by patient records	[53]
Hematology	CNN	IMG	Diagnosing hematological diseases from blood smears	[54]
Hospice and Palliative Medicine	ML, NLP	TAB	Identify the need for and assist in faciliating end of life care	[55]
Internal Medicine / Family Med	DL	ANY	A review of the need to guide ethical development of AI for use by Primary Health Care providers	[56]
Medical Genetics and Genomics	RF, Decision Trees	TAB	Understanding the role of a gene mutation in TB drug resistance	[39]
Nephrology	CNN	TAB	Predict IgA Nephropathy	[57]
Neurology	CNN, RF	ANY	Diagnosing ischemic stroke and occlusions of blood vessels with AI and imaging	[58]
Nuclear Medicine	ML	ANY	Evaluating possible applications of AI in planning, scanning and interpreting in Nuclear Medicine	[59]
Obstetrics and Gynecology	ANN, CNN, ML	ANY	Review of papers presented at ASRM and ESHRE 2018 conferences on human reproduction	[60]
Ophthalmology	CNN, DCN	IMG	Primer on development of AI models for disease detection and diagnoses in opthamology	[61]
Pathology (anatomic / clinical)	CNN	IMG	Assisting with pathological screening of biopsy and histology images	[62]
Pediatrics	NLP, ML	TAB	Assisting physicians with clinical diagnoses by extracting clinically relevant data from EHRs	[63]
Physical Medicine and Rehabilitation	ML	TAB	Developing home rehab system for stroke survivors	[64]
Preventive Medicine	ML	ANY	Building infectious disease surveillence systems using big data	[65]
Psychiatry	FF	TAB	Determining doseage of psychiatric patients	[36]
Radiation Oncology	CNN, DCN	IMG	Tumor detection, segmentation, growth, drug dosage calculation	[66]
Rheumatology	AI	ANY	Modelling the risk of fragile fracture for patients with or at risk of osteoporosis	[67]
Sleep Medicine	DL, AE	ANY	Detection of sleep arousal to improve sleep studies	[68]
SURGERY			See Robot-Assisted Surgery - Table 2.1	
Urology	DL	TAB	Predicting prostate cancer with analysis of many molecular drivers	[69]

Table 2.2 shows the various types of healthcare disciplines compiled from the

AAMC (Association of American Medical Colleges) and related AI models, as well as the type of data used and tasks that were performed with the AI. The relevant references for each combination are also included in the table.

2.2.3 Model Parameters

There are many adjustable model training parameters (different from learnable parameters in an AI - see section 4.1) known as hyperparameters that can be manipulated to optimize the performance of the CNN (AI).

Hyperparameters that were used in the model in section 4.1 include:

1. Freezing/Unfreezing Training - Disabling or enabling the training (changing) of the trainable parameters.

2. Loss function - An error function that is minimized to find the optimal solution, and to understand how the model is performing at any given time [70].

3. **Optimizer** - Used to adjust weights in the model to minimize the loss function [71].

4. Learning Rate - How much the weights are modified during training [71].

5. Momentum - Helps determine the rate of acceleration for gradient descent, it adds a lever of control in adjusting the learning rate [72].

6. Test, Train, Validation Split - The percentage split of the data between training, validation and testing.

7. **Batch Size** - The number of samples presented to the AI model at one time for training.

8. Learning Epochs - One iteration of presenting all the training/testing data, one epoch may require multiple batches.

7. Early Stopping Parameters - Stopping the training earlier than the predefined number of epochs based on the performance of the AI model monitored at the end of each epoch [71].

2.3 XAI Methods in Use

2.3.1 Types of XAI methods

Table 2.3: AI models, transparency parameters (Inherent or Post Hoc) and Data Type, with related and compatible XAI methods and related properties of the XAI method

AI Models	Tran.	AI Data Type	XAI Methods	Vis. Type	LO/GL	MA/MS	Source
Logistic Regression	IN		-	-	-	-	-
Linear Regression	IN		-	-	-	-	-
Decision Trees	IN		-	-	-	-	-
K-NN	IN		-	-	-	-	-
Rule Based Learners	IN		-	-	-	-	-
General Additive Model	IN	TAB	GA2M	TAB	GL	MS	[73]
Bayesian Model	IN	GRAPH, TAB, TEXT	iBCM	GRAPH, TAB,TEXT	GL	MS	[74]
Ensemble Methods & Decision Trees	PH	TAB	defragTrees	TAB	GL	MS	[75]
Ensemble Methods & Decision Trees	РН	TAB	inTrees	TAB	GL	MS	[76]
Random Forest	$_{\rm PH}$	TAB	Forest Floor	TAB, IMG	Both	MS	[77]
CNN, RNN,	$_{\rm PH}$	IMG, TAB	SWAF (Stacking With	TEXT	LO	MS	[78]
SVM	рц	TAD	hubrid Pulo Extraction	TAP	CI	MS	[70]
SVM	гп	TAD	Benning Method	TAD	GL	MC	[79]
SVM	DU	IAD	Contribution Propagation	IAD	U C	MS	[80]
Lincer SVM	DU	IMC TAR	Heatman coloring viewer	TAR INC	CI	MS	[92]
NN, ANN, FF	РН	TAB	RxREN (Rule Extraction by Reverese Engineering)	TAB, IMG	GL	MS	[82]
NN, Perceptron, RNN w/ GRU,	PH	TAB	Tree Regularization	TAB	GL	MS	[84]
NN, DCN,	$_{\rm PH}$	IMG	Distilling ensemble	IMG	GL	MS	[85]
CNN, DCN	$_{\rm PH}$	IMG	SG (SmoothGrad)	IMG	LO	MA	[86]

The Table 2.3 presents a combination of AI model types, identifies if the models are transparent inherently (IN) vs. need post hoc (PH) transparency methods, as well as

the type of data used by the AI model. This information on AI models is combined with the information on related and/or compatible XAI methods, their visualization of the output data; which includes Tables (TAB), Graphs, Text outputs, and Images (IMG). The scale of the XAI evaluation method is presented as well, whether the XAI evaluates the AI model's Global (GL) properties or Local (LO) properties. If the entirety of the AI model is evaluated then its a global scale XAI vs. if a finite portion of the AI model is evaluated by the XAI, then its a local scale XAI model. Lastly, the XAI models specificity is presented in the table. If the XAI model can work with any AI model then its Model Agnostic (MA) vs. if it only works with specific AI models then its Model Specific (MS) [16] [20] [17].

Table 2.3 is only a truncated summary of the entire list compiled for this literature review, the entire complete table is present in Appendix A in Table A.2.

2.3.2 Utility with various XAI methods

The following selection of XAI methods are chosen for the purpose of detailed evaluation in this thesis: Vanilla Saliency, SmoothGrad, GradCAM, & GradCAM++. More details about the implementation of these methods is discussed in Section 5.1. A brief primer to understand the general concepts of each XAI method are presented here.

Vanilla Saliency was designed to address the need of visualising the neuronal activity of Deep Convolutional Networks (DCNs). For an arbitrary number of layers in a DCN, compute the gradient of output relative to the input:

$$\frac{\partial Output}{\partial Input} \tag{2.3.1}$$

Any pixels with positive gradient values can be identified as pixels where the output value will increase if the input value is increased, this is done by using a RELU activation function in the back-propagation process. Through back-propagation it identifies all the pixels in an input image that when perturbed will create the most change in the output image. This can be done for any layer (not necessarily the final output layer). Finally, the process is to map out a visualization (saliency map) by highlighting only the most informative pixels on the input image for any given classification [87].

SmoothGrad is a more coherent mapping method than Vanilla Saliency. In the previous method, there are noisy pixels with gradients high enough to end up appearing as important input pixels. SmoothGrad, adds (to each pixel) stochastic Gaussian noise in the otherwise same formula that was used in Vanilla Saliency. And then the final gradients are capped at a very high value to capture most of the relevant gradients and remove the errant 'noise' in the gradient mapping. This process then goes one step further and multiplies the final gradient map with the original image pixel values to produce a very coherent and sharp final visualization [86].

GradCAM (Gradient-weighted Class Activation Mapping) produces a coarse visualization highlighting the areas on the input image that are important regions for the classification decision by the AI model. To produce the GradCAM visualization, the model's convolutional layers are cut-off (up to whatever layer the user wishes to analyse) and the fully connected classifier layers are attached up to that cut-off convolutional layer. The input image is passed to the newly modified model and once again a gradient of the classifier's output layer (before the softmax activation layer) relative to the feature maps of the convolutional layer:

$$weight = \frac{\partial OutputClassScore}{\partial Conv.LayerFeatureMap}$$
(2.3.2)

is determined via back-propagation. This weight is multiplied by the activation map and passed to a RELU activation function in the forward direction to create the GradCAM mapping. Shown here:

$$GradCAMHeatMap = RELU(weight * conv.layerfeaturemap)$$
 (2.3.3)

This heatmap is then overlayed onto the original input image and provided to the user to visually identify the AI's understanding of the areas of high importance in the input image [88].

GradCAM++ is a more sophisticated version of GradCAM. The weight calculated during back-propagation in GradCAM is modified:

$$weight = ClassGradientWeights * RELU(\frac{\partial OutputClassScore}{\partial Conv.LayerFeatureMap}) \quad (2.3.4)$$

followed by a forward direction creation of the Heat Map. The ultimate result of this method is the ability to produce better visual localization of objects (in a multi-class problem) in a single image [89].

2.3.3 How XAI impacts people

As presented in Section 2.1.3 and Figures 2.3 & 2.4 everyone is affected by the need for explainability when it comes to developing trust in an AI's decision making. And that explainability element that will adequately address trust for a user will do so by providing insights into the AI's **accuracy**, provide the user with some assurance that the AI's decision making is **safe** and provide some **performance** related advantage for some users.

This thesis uses the Explainable AI (XAI) methods presented in Section 2.3.2 and evaluates them for their ability to provide a measurement of accuracy of the underlying AI. Measures the XAI's performance for consistency, this provides a measurement of safety of the underlying AI. This thesis also evaluates the XAI methods for any insights on AI model's novel learned processes to test if the performance of the workflow is affected by the underlying AI.

Accuracy is more finely defined as the _(similarity) between XAI and SME's outputs. Safety is evaluated by the _(stability) of the XAI relative to other XAI methods. Lastly, the XAI methods evaluate the performance of the AI by identifying any _(novelty) in learning or_(overlooked learning) by the AI.

Similarity is first comparison that provides a measure of objectivity in an XAI's trustworthiness. This is done with comparing the XAI method's output, which is its determination of the AI's learning, against the SME annotations. The two distance metrics used to determine the similarity between the pairwise array are Jaccard Similarity and Hamming Similarity.



(a) Visualizing Jaccard Similarity equation as a Venn diagram. The intersection of the two datasets divided by the union of two datasets.

Figure 2.6: Visualizing Similarity with Jaccard Similarity and Hamming Distance Metrics

$$D(x,y) = 1 - \frac{|x \cap y|}{|x \cup y|}$$
(2.3.5)

Jaccard Similarity shown above in equation 2.3.5, is commonly used as a predictor of similarity between two datasets [90]. It is also used in machine vision applications to predict labels for image segments [91]. In this thesis, the Jaccard similarity metric is used to identify the similarity between the pairwise arrays of XAI outputs and SME annotations. Figure 2.6a shows of visualization of the equation 2.3.5, the Jaccard similarity metric is derived by dividing the intersection of the two datasets by the union (combined total minus the intersection). An metric value of 1 represents that the two datasets are identical, and a value of 0 represents no overlap at all.

$$D(x,y) = 1 - \frac{1}{n} \sum_{i=1}^{n} 1_{xi \neq yi}$$
(2.3.6)

Hamming Similarity shown in equation 2.3.6, is the inverse of the normally used

Hamming distance metric. Hamming distance provides a metric score representing all the instances of dissimilarity between two datasets. The Hamming distance visualization in Figure 2.6b shows that a unique cluster identified by the XAI output only or an annotation identified by the SME only, will be identified as an asynchronous event between the two vectors and reduce the similarity metric. A Hamming similarity metric of 1 represents two identical datasets, and 0 represents no overlap at all.

Box-and-whisker (BW) plots are used to show how accurately each XAI method can present the underlying learning of the AI model. Given a correct classification by the AI, with no overlooked features and no novel learning possible. The best XAI method output has a similarity score of 1.0 for Jaccard or Hamming similarity metrics. Similarly, for an incorrect classification by the AI the best XAI method identifies a lot of differences between the SME annotations and the XAI output. Thus giving a score of 0.0 for Jaccard and Hamming similarity metrics. Therefore, a BW plot helps visualize the performance of the XAI method, where incorrect classifications by the AI are all in the lower inter-quartile range of the BW plot.

The 'box' shows where 25th, median (50th) and 75th percentile (the inter-quartile range(IQR)) of the underlying data lie on the y-axis (the similarity metric). The upper and lower 'whiskers' represent the min and max points of data that are 1.5 times beyond the IQR in either direction, points beyond the 1.5 IQR are outliers. 'Outlier' is only a statistical term to represent the data point's distance from the IQR. It may or may not have any real world significance, beyond representing the skewness and/or kurtosis of the dataset.

Stability is the next comparison that provides a measure of consistency of an XAI's output. Measuring the consistency of an XAI method presenting the underlying

AI learned processes affect a user's trust in the underlying AI's safety. This measure is provided by comparing the XAI method's output to all other XAI methods' outputs for every test sample.

Pearson correlation, shown in Figure 2.7, determines the degree of correlation between the two datasets. The Pearson correlation coefficient provides a measure of distance between the two datasets, and also a measure of directionality of that relationship. This directionality is not important for the purpose of measuring the stability of the XAI methods.



Figure 2.7: Visualizing Pearson Correlation - Stability Metric. Determines the relationship between two datasets of values [outputs of XAIs].

$$r = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (x_i - \overline{x})^2 \sum (y_i - \overline{y})^2}}$$
(2.3.7)

Pearson correlation output is between -1 and 1 and is a true metric or distance measure [90] because it meets the triangular inequality required for a distance measure. A metric that is not contained between 0 and 1 instead of the -1 and 1, makes comparisons to other metrics used in this thesis difficult. Thus the values of r from Equation 2.3.7 are remapped onto a space between 0 and 1 in Equation 2.3.8 by taking the absolute value.

$$r = abs\left(\frac{\sum(x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum(x_i - \overline{x})^2 \sum(y_i - \overline{y})^2}}\right)$$
(2.3.8)

where:

r is the Pearson Correlation coefficient.

 x_i is value of a single feature in the first XAI output,

 \overline{x} refers to the mean of values in the first XAI output,

 y_i is value of a single feature in the second XAI output,

 \overline{y} refers to the mean of values in the the second XAI output,



Figure 2.8: Pearson Correlation coefficient (R) is independent of slope, it is only a measure of the relationship between two datasets.

It is important to note that the Pearson Correlation coefficient is not a measure of steepness of the slope as shown in figure 2.8, rather it is a measure of how closely data from two variable (XAI methods) maps onto a straight line. There is no assumption of direct relationship between the two XAI methods, rather a confounding variable (learning by the underlying AI) can be the source of correlation between the two variables (XAI methods). Novelty and Overlooked learning is the last XAI comparison. This comparison provides insights about the performance of the underlying AI method. These insights are acquired by evaluating individual features highlighted or overlooked by the XAI output relative to the SME annotations. In this thesis, the novel features and overlooked features are defined as:

Novel features are individual features (combinations of pixels) in an ECG record identified in an XAI output as important for classification, but not identified by the SME.

Overlooked features are individual features (combinations of pixels) in an ECG record that correspond to SME annotations but not identified by the XAI output.

Term Frequency - Inverse Document Frequency (TF-IDF) method is used in this thesis to determine the predictive value of novel features and/or overlooked features towards classification of an ECG record. This method is commonly used in literature for text mining, to determine the semantic importance of terms (features) in a document (ECG record) relative to all other terms in that document within a collection of related documents [91]. In this thesis, TF-IDF is applied to collections of ECG records grouped by their classification.

TF-IDF method first creates a vocabulary of all features present in ECG records of a single class. As shown in equations 2.3.9 & 2.3.10, TF term identifies the frequency with which a feature is present in an ECG record. IDF term identifies the semantic importance of the feature to the ECG record, giving a weighting for the feature relative to the vocabulary.

Figure 2.9 is a cartoon representation of ECG records, to demonstrate how TF-IDF can identify the importance of a feature to a single ECG record. In the thesis, any features common between the SME annotation and XAI output are excluded from this analysis. Thus, the only features being evaluated in figure 2.9 for their importance are those that are already either completely novel (blue) features or completely overlooked (green) features. The remaining features (red and purple) in figure 2.9 are ignored because they are common between XAI output and SME annotations. Calculation of TF-IDF weights shown in figure 2.9 is made using equations 2.3.9 and 2.3.10.



Figure 2.9: Visualization of TF-IDF used to determine the significance of features identified by an XAI output and SME annotations for a given record. Each record is an ECG test sample, coloured circles represent features, blue and green features are novel and overlooked features respectively.

Equation 2.3.9 shows how the TF-IDF score for novel features is determined. Equation 2.3.10 shows how the TF-IDF score for overlooked features is determined. Note t_{-o} value in equation 2.3.10 is calculated differently than t_{-n} in equation 2.3.9.

$$TF - IDF_n = TF \cdot IDF$$

$$TF = log(1 + freq (t, d))$$

$$IDF = log\left(\frac{N}{count (d \in D : t_n \in d)}\right)$$

$$t_n = (X - (A \cap X)) ; X = [x_1, ..., x_i], A = [a_1, ..., a_j]$$

$$d = [t_n | y_{pred} \cap y_{true}] \subset D : D = (A \cup X)$$

$$(2.3.9)$$

where:

$$t_n$$
 is a single term (feature) from X not present in A,

- d is a single document (ECG record),
- D group of all documents (all records for a single class),
- \boldsymbol{X} refers to XAI output array,
- A refers to SME annotations array.

$$TF - IDF_n = TF \cdot IDF$$

$$TF = log(1 + freq (t, d))$$

$$IDF = log \left(\frac{N}{count (d \in D : t_o \in d)}\right)$$

$$t_o = (A - (A \cap X)) ; X = [x_1, ..., x_i], A = [a_1, ..., a_j]$$

$$d = [t_o| y_{pred} \cap y_{true}] \subset D : D = (A \cup X)$$

$$(2.3.10)$$

where:

 t_o is a single term (feature) from A not present in X.

All else is the same as equation 2.3.9

2.3.4 Limitations of XAI

Most reviews and primary research papers in literature that deal with trust in AI or explainable AI try and define the concepts of explainable AI and differentiate them from concepts like interpretability and transparency etc. [17] [92]. Then there are papers that actually suggest methods for evaluating XAI with metrics, but they mostly end up creating some new XAI methodology that is easier to evaluate than the current methods and objective XAI evaluations is not actually accomplished [93]. There are fewer papers still discussing the need to build trust especially in the context of AI and healthcare [9] [10].

With the slight exceptions of [88] & [89] there aren't any papers that present a tangible method of objectively evaluating the performance of an XAI method. Even the two papers [88] [89] make a very limited case of 'objective' evaluation which requires a human subject to ultimately determine if the interpretable XAI is indeed interpretable. Also the arguments for trust are very limited and the scope is focused on determining if the XAI methods Grad-CAM and Grad-CAM++ are objectively and subjectively good. To determine if the XAI method is objectively good the XAI has to be 'interpretable' and 'faithful'.

2.4 Quantifying Trust

Based on the literature review regarding the need to improve user trust in AI, the important concepts identified in building trust are combined into a series of equations. This will help provide an objective metric or numerical value of trustworthiness to an AI model. Similar to the mathematics of trust [94] and algorithms used to convey the concept of trust in human (adversarial and non-adversarial) interactions [95] and human to machine interactions [96] the following equation is presented by the author as a method to capture and quantify important elements of trust.

$$T = \left(\left[\frac{\sum_{i} (w_x T_x)_i}{\sum_{i} w_i} \right] + w_v T_v + w_r T_r + w_f T_f \right) / \sum_n w_n$$
(2.4.1)

Equation 2.4.1 is the full Trust equation, combining all the elements of trust; Explainability (T_x) , Verifiability (T_v) , Robustness (T_r) and Fairness (T_f) and the corresponding weights (w) that will have to be determined experimentally.

$$E_{sim} = \frac{\sum (w_0 M_0, w_1 M_1, \dots, w_n M_n)}{\sum w_n} , \ 0 \le M \le 1$$
 (2.4.2)

$$E_{stab} = \frac{\sum (w_0 N_0, w_1 N_1, \dots, w_n N_n)}{\sum w_n} , \ 0 \le N \le 1$$
 (2.4.3)

Equations 2.4.2 and 2.4.3 with names and weights of test metrics:

$$E_{sim} = \frac{\sum (0.5M_{Jaccard}, 0.5M_{Hamming})}{1} , \ 0 \le M \le 1$$
 (2.4.4)

$$E_{stab} = \frac{\sum (N_{PearsonCorr})}{1} , \ 0 \le N \le 1$$
(2.4.5)

 E_{sim} in equation 2.4.2 combines individual metrics (M) used to evaluate the XAI methods and their respective weights (w), represented by $w_n M_n$. Jaccard and Hamming similarity metrics and both are true metrics (distance measures) [90] such that the values of M_n are contained between and 0 and 1.

 E_{stab} in equation 2.4.3 presents the individual metrics (N) used to evaluate the XAI method's stability and their respective weights (w), represented by $w_n N_n$. Pearson Correlation is the stability metric true metrics (distance measures) [90] such that the values of M_n are contained between and 0 and 1.

$$T_x = \frac{\sum (w_{sim} E_{sim}, w_{stab} E_{stab})}{\sum w}$$
(2.4.6)

The Equations 2.4.4 & 2.4.5 relate the concept of similarity and stability to the explainability element of Trust shown in equation 2.4.6. Equation 2.4.6 is the combination of similarity and stability equations that combine together here to provide one trust measure that combines into the overall trust equation 2.4.1. Each additional XAI method used to evaluate the AI model, adds an additional T_x term to the equation 2.4.1.

$$K_n = \frac{\Sigma(Record_n | XAI_{novelty})}{\Sigma(Record_n)}$$
(2.4.7)

$$R_u = \frac{\Sigma(Record_u | XAI_{overlooked})}{\Sigma(Record_u)}$$
(2.4.8)

The Equations 2.4.7 & 2.4.8 are used in equation 2.4.9. K_n and R_u provide a measure of how much novel learning or overlooked learning was identified by a single XAI method respectively.

$$E_{XAI} = [T_x, K_n, R_u], \ 0 \le T, K, R \le 1$$
 (2.4.9)

Equation 2.4.9 is a vector of values that provides insight on the utility of the

individual XAI method from the perspective of Explainability as shown in Figure 2.4. T_x refers to trust conferred on to the individual XAI method derived by Equation 2.4.6. K_n refers to any novel Knowledge that the AI model may have learned that the XAI method can identify. A value approaching 1 means each record had a novel feature identified. R_u refers to any Recommended overlooked learning by the AI model that the XAI can identify, a value approaching 0 means no overlooked features were identified. This vector of values is not meant to combine with any other equation, rather be a standalone vector to inform the user on the utility of the evaluated XAI.

Chapter 3

Domain Data



Figure 3.1: Visualization of overall Journey of the Thesis - Specifically dealing with the Task and Data type in this section.

To evaluate XAI methods it was necessary to apply a machine learning model to a suitably complex data set. The data and its preparation method used for training and testing the machine learning model are described in this section.

3.1 ML Objective: ECG Classification

This thesis utilized continuous time-series data to evaluate ECG signals from patients. The time-series data was used to train a classifier model to identify four cardiovascular conditions.

3.1.1 Domain and Model Datasets

Three databases were used for this Thesis, two ECG databases were used and one machine vision database. ImageNet was the machine vision database used as the default pre-trained weights for Keras' implementation of VGG-16 [71] & [97]. The imageNet dataset has 1000 classes of images, and contains 1,281,167 images for training, 50,000 images for validation and 100,000 images for testing.

The 'MITBIH' database is an open access database acquired from Physionet repository of physiological signals, officially referred to as 'MIT-BIH Arrhythmia Database'¹. 'Chapman' database is also an open access database produced and maintained by the Chapman University and Shaoxing People's Hospital in China. Officially referred to as 'Chapman-Shaoxing database'² [98]. The two ECG databases are discussed in detail in Table 3.1.

¹https://physionet.org/content/mitdb/1.0.0/

²https://figshare.com/collections/ChapmanECG/4560497/1

Database	Original						
	Age	# of	# of	Record	Sample	Classes	Leads
	Range	Subjects	Records	Length	Freq.	Classes	Leaub
Chapman	4-98	10646	10646	10 sec	$500 \ Hz$	11	12
MITBIH	23-89	47	48	30:06 min	$360~\mathrm{Hz}$	15	2
	Modified						
	Used in	# of	# of	Record	Sample	Classos	Londa
	Training	Subjects	Records	Length	Freq.	Classes	Leaus
Chapman	Step 1	10646	10646	10 sec	500 Hz	4	4
MITBIH	Step 2	47	7414	10 sec	$500~\mathrm{Hz}$	4	2

Table 3.1: Statistics of ECG signal	databases [Chapman &	& MITBIH] used for t	raining, as original
datasets and after modificat	tion with reduced classe	es and harmonized rec	cord lengths

3.2 Data Labelling

The two ECG datasets presented below are utilized by the CNN model, as presented in Section 4.1 to make classification decisions between four distinct cardiovascular rhythms.

Chapman Dataset: This dataset has a total of 10,646 records of 12 lead data. Each record corresponds to an individual subject (patient), and is 10 seconds in length, sampled at 500 Hz. The original ECG data was classified by 11 different rhythms, these 11 rhythms were then combined together to form 4 groups of rhythms. These mergers of rhythm classes were done by trained Cardiologists as presented in [99].

MITBIH Dataset: This dataset originally contains 2 lead ECG recordings from 47 subjects with 30:06 minute long ECG recordings for each individual subject, sampled at 360 Hz [100] & [101]. The original data was classified by 15 different rhythms,

these were once again grouped into 4 groups to reduce the number of total classes. The merging of classes in the MITBIH dataset was done by combining classes with the same SNOMED CT codes as the 11 classes in Chapman dataset. The SNOMED CT codes for the classifications from both datasets were acquired from the PhysioNet competition [17]. In addition to the overlapping SNOMED CT codes, an online ECG library maintained by Dr. Robert Buttner of Monash University and Alfred Emergency & Trauma Center - an expert in ECG and Ultrasound diagnostics, was used to confirm if some labels under the MITBIH dataset could be merged into the GSVT category. If no unambiguously clear answer was found by either means (SNOMED CT and ECG library) the label was placed into a separate category and omitted from consideration. A full table of all conditions and their corresponding SNOMED CT codes are presented in the Appendix A

Dataset Overlap: The Chapman dataset provides 12 lead ECG data for each of the 10,646 records of data. The MITBIH provides 2 leads of ECG data for each record that are various combinations of the 4 ECG leads (II, V1, V2, V5). Four leads of data (II, V1, V2, V5) from the Chapman were used for training the VGG-16 Model as shown in figure 4.2, to ensure overlap and parity between training data from the Chapman and MITBIH datasets.

Chapman	Merged Labels	MITBIH	SNOMED CT
AFIB,	ΔFIB	AFIB,	164889003,
AF	AT ID	AFL	164890007
SVT			427084000,
лт.		VT	713422000,
		vı,	233897008,
SAAWR,	GSVT	1,	164895002,
ST,		VFL,	111288001,
AVNRT,		SVTA	251180001,
AVRT			426761007
SB	SB	SBR	426177001
SR, SI	SR	Ν	426783006
		PREX, B, IVR,	
	Omitted	P, BII, NOD,	
		AB	

Table 3.2: Merged class labels for both datasets [MITBIH & Chapman] and corresponding SNOMED CT codes

3.2.1 Domain Data Pre-processing



Figure 3.2: Data Windowing Visualization. In the Chapman [labelled, Hangyuang] dataset 10646 subjects contributed to 10646 10-second ECG records. In the MITBIH dataset 47 subjects contributed 47 30:06-minute records windowed to 7414 10-second ECG records.

The datasets shown in Figure 3.3 are shown with record labels already having been merged according to the Table 3.2.

Chapman Dataset:

The Chapman dataset was not processed beyond the relabelling of the records with the merged classes. The dataset was already pre-processed by the curators of the dataset. The same methodology used by the curators of the Chapman dataset to denoise and filter the signal was eventually implemented for the MITBIH dataset.

MITBIH Dataset:

The MITBIH dataset was originally 47 subjects with each subject having a single 30:06 min long record. Each 30:06 minute, 2 Lead ECG signal is truncated into a

series of records of 10 second windows with no overlap between adjacent records. The individual signal annotations available for the MITBIH dataset were used to relabel each of the truncated windows with one of the 4 merged class labels. Some subjects would have had multiple different labels throughout the long signal and each truncated signal record was labelled with the preceding record's label unless there was a label change within the file itself. In case of multiple classifications in a single truncated record, the record was removed from consideration. Also, as shown in Table 3.2 there was a small list of classification labels that didn't fit in with any of the other 4 merged classes and were also omitted form consideration. After all the truncating and omissions 7414 total records were produced to be split between testing and training.

3.2.2 Signal filtering

As discussed in Section 3.2.1 the Chapman dataset signals were pre-processed by dataset curators [99] to produce a denoised signal, with all power noise, motion artifacts and random noise as thoroughly minimized as possible. The signal also had any DC signal offset (baseline wander) removed. This was done by implementing a series of very specific filters to accomplish this.

First [99] implemented a low pass butterworth filter with a passband from 0.5 Hz to 50 Hz and a stopband to 60 Hz with 2.5 db attenuation to remove power noise that exists at 60 Hz. This was followed by a LOESS (Local polynomial regression) smoother to remove the baseline wander of the signal. Lastly, a NLM (non local means) noise reduction algorithm was also used to smooth out the high frequency noise that might have appeared after the LOESS smoothing [99].

The denoising tools discussed are available in opensource matlab code available at https://github.com/zheng120/ECGDenoisingTool, provided by the curators of the dataset. All MITBIH 10 second windowed signals were passed through the denoising tool to achieve parity in denoising with the training dataset. Because the code in matlab was very slow to process and took a very long time to denoise even a single file with 2 ECG leads. The code was re-implemented in python using all the same parameters presented in great detail in the matlab tool.



Figure 3.3: Signal filtering - Each step of the signal filtering process visualized. The Original Signal is passed through a Lowpass Butterworth filter, A LOESS filter to remove baseline DC wander, then NLM denoising to remove high frequency components introduced in the previous filtering efforts.

Once the signals were filtered and denoised, they were plotted as binary images with the background set to black or 0 and the signal's pixel values set to white or 1 of size 500 x 500 pixels. This image was plotted with only the ECG leads 'II, V1, V2, & V5' as these are the only combination of leads used by the MITBIH database (with the exception of MITBIH subject 124 that recorded has leads II % V4, and lead V4 was not plotted for consistency). As shown in figure 4.4

Following the plotting of the signals, the signals were once again filtered using threshold binary and OTSU filtering methods to remove any aliasing artifacts or noise from the plotting process. The reason the images were kept as plotted images and not just stored as an array from the beginning, was because the XAI methods discussed in Section 5.1 required images to be fed into some XAI methods and the plotted images were created for convenience of usage later in the process. The plotted image that had been filtered with threshold binary and OTSU filtering were stored in an sequential array, to be passed on to the CNN along with an array of matching labels. From this point onward, these will be referred to as 'plotted images'.





(a) Record from Chapman Dataset - Leads II, V1, (b) Record from MITBIH Dataset - Leads II, V4 V2, V5 and 2 empty leads

Figure 3.4: Potting Leads II, V1, V2, V5. These images show the visualization of records from each dataset [Chapman & MITBIH] presented to the AI model for training and testing.

Chapter 4

AI Model: ECG Classifier



Figure 4.1: Visualization of overall Journey of the Thesis - Specifically dealing with the AI model in this section.

This section discusses how the underlying AI model is built, the rationale behind each component and the decisions for the parameters.

4.1 Model Architecture

The VGG-16 (a 16 layer, 2-D convolutional neural network) was used as the primary component of the AI model, along with a fully connected classifier connected at the final stage. [102, 103] Demonstrated the use of a variety of 2-D CNNs to perform

classification tasks involving biomedical signals. [102] Utilized a two lead raw ECG signal and converted the signal into a 2-D binary image to be classified using the VGG-CNN architecture as a powerful feature detector. Similarly [103] demonstrated the use of 2-D VGG-CNN, among other CNN architectures, to be superior in performance compared to a traditional 1-D signal processing method commonly used with time-series data like ECG signals.

The benefit of using a deep learning architecture like VGG was the ability to utilize a well pre-trained neural network with many specialized, complex feature-detecting kernels. Greatly reducing the need to manually perform complex feature detection work prior to classification [104].

As shown in [102, 103] other similar architectures such as Inception, Xception, ResNet, AlexNet, could have been used as well. The VGG-16 model had a similar accuracy as the other models, but with a much larger number of trainable parameters. This made VGG-16 more expensive computationally relative to the ResNet, Xception and Inception models [105]. This model selection assumed that more learnable parameters, may allow for more detailed insights at each layer when the XAI methods are implemented. This assumption did not hold true, based on how XAI methods work. Other computationally lighter AI models could have been used instead.

4.2 Training Paradigm

The training paradigm was developed through a series of design iterations. The best combinations of model parameters (discussed in detail in the section 4.3) was determined with a combination of cross-validation and exploring literature. Graphical representation of all attempted training paradigms is presented in Appendix A as well
as a full table outlining the results of the iterative testing (Appendix B, Table A.1). This sections presents a brief overview of the training paradigm of the CNN model.



Figure 4.2: Overall training paradigm. Contains two steps of training, once with each dataset to achieve some degree of 'transfer learning' between datasets. Additionally each step involves initial training with frozen VGG-16 weights to initialize training of input and classifier layers, followed by unfrozen training for all layers of the whole model [with very low learning rates].

The training consists of 2 steps as shown in Section 4.2:

Step 1: Training with Chapman dataset.

Datasets characteristics are presented in the section 3.1.1. The machine learning model training on the Chapman dataset had 2 steps with separate segments:

 In segment 1a, the parameters of all the layers of the VGG-16 CNN were kept 'frozen'. Meaning the weights of the neurons were untrainable. This was done to ensure that the input layer and the output dense (classifier) layers could be trained without changing the weights of the VGG-16 layers.

The imagenet [97] pre-trained weights were used as the starting weights of the VGG-16 layer. As shown in [106] the imagenet pre-trained weights led to significantly improved performance in classification tasks. Additionally, given the relatively small size of the Chapman and MITBIH datasets, using imagenet pre-training utilized the feature detection power from the pre-trained convolutional filter kernels [107].

2. In segment 1b, all the parameters were unfrozen to allow slight changes in the weights of the neurons in the VGG-16 CNN layers. To prevent massive fluctuations in the weights, the learning rate was reduced [107] and the momentum was increased to counterbalance the impact of the low learning rate [72].

Step 2: Training with the MITBIH dataset.

The full process of **Step 1** was repeated with the MITBIH dataset. Details of the datasets are presented in section 3.1.1. Only 30% of the data from the MITBIH dataset is used for training and validation purposes and 70% is retained for testing. This second step was only done with the MITBIH dataset because this is the testing Dataset, the entire Chapman dataset was used for training only (as shown in Step 1).

4.3 Model Parameters

This section presents the hyperparameters introduced in section 2.2.3. In this section more detail about how they were implemented is presented.

Hyperparameters that were optimized included:

1. Freezing/Unfreezing Training - The training happens in 2 segments. First, all the convolutional layer parameters are set to be 'frozen' (untrainable), so that the learned weights don't change for these layers as the training progresses. Only the Input and final Dense (classifier) layers will have changing weights. This initial training is followed by the second training segment, where all layer parameters are unfrozen (trainable) to allow changes in the weights of all parameters.

2. Loss function - The 'categorical cross-entropy' loss function is used because the task is a multi-classification task and according to [108] & [109] categorical crossentropy (log) loss function is the most commonly used loss function for a multi-class problem. Although more sophisticated loss functions exist [70], the simplicity of pre-existing keras implementation makes the log loss function the obvious choice .

3. **Optimizer** - The SGD (Stochastic Gradient Descent), this was the default optimizer implemented by Keras and recommended for a multi-classification problem [71].

4. Learning Rate - An initially high learning rate of 0.0001, to move the weights of the input layer and the dense (classifier) layer to the neighbourhood of the optimum weights quickly. In the second round the a much lower learning rate of 0.00001 is used to prevent massive fluctuations in trainable parameter weights.

5. Momentum - A low initial momentum of 0.5 for the first part (with frozen training layers), followed by an increased momentum of 0.9 when the learning rate

increases in the second cycle of training (with unfrozen training layers). The momentum is basically using an exponentially weighted average of the gradients used to determine the weights in each epoch, and utilizing this weighted gradient to determine the weights instead, which allows the neural network to arrive at the final weights quicker [72].

6. Test, Train, Validation Split - 100% of the Chapman data was used for training. 70% of the MITBIH dataset was set aside for testing. The remaining 30% of the overall dataset was used in the training stage and 10% out of the 30% training data was used for validation. Therefore 27% of the overall data was used for training and 3% for validation.

7. **Batch Size** - With larger batch sizes, greater computational resources are required and overall generalizability of the model decreases [110] but with smaller batch sizes

8. Learning Epochs - Based on preliminary testing, approximately 20 Epochs were determined to be long enough to see training and validation plateau and considered long enough to see if any further significant changes in gradient descent occur, resulting in further changes to the validation accuracy.

7. Early Stopping Parameters - The validation accuracy was the value that was monitored to implement early stopping. A minimum change or 'min_delta' of less than 1% in the value was the set point. As long as this set point didn't change more than the min_delta over a period or 'patience' of 5 consecutive epochs, the training was stopped. This method was implemented by the keras' 'EarlyStopping' method and is what helped determine the optimal cutoff of 20 epochs determined above [71].

Parameter	Segment	Value	Reference	
	1a, 2a	Frozen	[107]	
Freezing/Unfreezing	1b, 2b	Unfrozen	[107]	
Loss Function	All	Gategorical Cross-Entropy	[108, 109]	
Optimizer	All	Stochastic Gradient Descent	[71]	
L. D.	1a, 2a	0.0001	[107]	
Learning Rate	1b, 2b	0.00001	[107]	
	1a, 2a	0.5	[70, 111]	
Momentum	1b, 2b	0.9	[72, 111]	
	1a, 1b	100%,0%,0%		
lest, Irain, Val. Split	2a, 2b	70%, 27%, 3%	Experimental	
Batch Size	All	16	Experimental	
Epochs	All	20 (with Early stopping)	Experimental	
		Value - Validation Accuracy		
Early Stopping	All	Min_delta - 1%	[71]	
		Patience - 5		

Table 4.1: Model parameters used by the AI model for training purposes. These include parameters and hyperparameters that were optimized using values from cross validation and literature.

4.4 Training

The input images created from plotting the various lead combinations were of the size 500x500x1 pixels. The regular input of the VGG-16 is 224x224x3. To accommodate the difference size an input block was attached to the VGG-16 CNN layers to modify how the image features were extracted (see training paradigm in figure 4.2). New fully connected dense layers were added to process that increased number of parameters (as the input increased from 224x224x3 to 500x500x3). It also allowed the CNN to

redefine the number of classes from 1000 (normally for VGG-16) down to 4 for ECG classification in this thesis. A full layer by layer output is presented in Appendix B Model B.

The input images were modified from a single layer to a three layer image (500x500x1 to 500x500x3) as required by the VGG-16. This was done by broadcasting the array of images to increase the dimensional space. When the initial training was done with frozen parameters, only the CNN parameters were kept frozen (14,714,688 parameters frozen out of 118,492,676 total parameters).

There was a transfer learning effect created by training the VGG-16 model on the Chapman dataset in step 1 (figure 4.2), and in step 2 training with 30% of the MITBIH dataset. The impact of this potential transfer learning effect was evaluated and discussed in model performance section 4.6. In addition to these considerations, class weighting was implemented when training with the MITBIH dataset to offset the large dataset imbalance [112].

An important consideration for training paradigms, which is commonly overlooked in many medical decision making AI models. It is understanding the intersection of subject (patient) & records (ECG recordings of a patient) (figure 3.3) and how they impact learning in AI models [113]. According to [113] when records from the same subject are intermixed between training, validation and testing stages they often result in a massive improvement of the prediction accuracy of the model. This is effectively cheating, because during the testing phase the model has likely seen records very similar to the test set from the same patient during training or validation. The best method for dealing with multiple records from the same subject is to isolate all the records for a given subject for either training, validation or testing stage alone. This common oversight is very prevalent in literature with wearable sensors used to predict clinical outcomes.

Given the focus of this thesis' research was quantifying explainability in medical AI. The author acknowledges that no subject/record isolation was performed and that data leakage was not accounted when developing the model. As the goal of the thesis is to scrutinize model decision making at the the XAI explanation stage. An undeservedly-superior classifier may offer greater insight on how explanations are generated for an Neural Network's decision making paradigms.

To perform this task, a high accuracy model was beneficial to observe the best possible behaviour of the XAI methods. This particular consideration applied to the training done with the MITBIH dataset in step 2 of the training paradigm as shown in Figure 4.2. Having a model with high (artificially inflated) accuracy and a model with lower accuracy could have both been tested together to see their impact on the results of the XAI outputs, this could potentially have been used to gain insights on the stability of the XAI output with changing model accuracy. But this effect was not explored. If explainability is correlated to the accuracy of the model, as the accuracy changes, the similarity metric of explainability will likely change proportionally, but the within XAI method stability should most likely remain the same, and this may give additional insights on the value of the XAI methods.

4.5 Testing

The only dataset used for testing is the MITBIH dataset, 70% of the dataset (5190 records) was allocated for testing. As discussed before, the subjects seen in the training phase might be seen again in the testing phase, but the individual records

would be unique and never before seen.

Just as in the training, testing the performance of VGG-16 based CNN was done with the plotted images. A list of these files seen here was saved, to be given to the XAI methods in section 5.1.

4.6 Model Performance

Step 1 The results recorded here are of the performance of the model with the Chapman dataset only.



Figure 4.3: Training Step 1 - Performance (Accuracy vs. Epochs)

Step 2 The results recorded here are of the performance of the model with the MITHBIH dataset, after the model has already been previously trained on the Chapman dataset.



Figure 4.4: Training Step 1 - Performance (Accuracy vs. Epochs)

Results

Table 4.2 shows the accuracy, precision, recall and Area under the curve (AUC) values of the model during Training, Validation [step 2, segment 2b] and Testing. More detailed values shown in the Appendix A table A.1.

Table 4.2: Model Performance Results

	Train		Validatio	on		Test					
Train Acc.	Precision	recall	auc	Val Acc. Precision recall auc		Test Acc.	Precision	recall	auc		
0.985	0.97	0.97	0.9904	0.9787	0.9636	0.9507	0.9966	0.9718	0.9475	0.9391	0.9943

Confusion Matrix

The confusion matrix shown in table4.3 displays results of the Testing with 5190 records. Each quadrant with a Class (AFIB, SB, GSVT, SR) represents the results for that classification. In the rows in each quadrant, '1' represent an expected result of that classification and '0' represents an expected result of any classification other than that quadrant. The column '1' represents a correct classification and '0' represents an incorrect classification event.

AFIB	0	1	SB	0	1
0	4561	46	0	5065	3
1	11	572	1	4	118
GSVT	0	1	\mathbf{SR}	0	1
0	4869	115	0	785	126
1	121	85	1	154	4125

Table 4.3: Confusion matrix for test results, each class (AFIB, SB, GSVT, SR) is presented separately in a quadrant

4.7 Software Packages

The full flowchart of methodology and each .ipynb file in it is provided in Appendix B Figure A.6.

Command to get all the requirements.txt files for all the jupyter notebooks used:

```
jupyter nbconvert --output-dir="./reqs" --to script filename.ipynb
cd reqs
pipreqs
```

- 1. matplotlib==3.1.2
- 2. neurokit2==0.1.1
- 3. numpy==1.17.4
- 4. $opencv_contrib_python = 4.5.3.56$
- 5. pandas = 0.25.3
- 6. tensorflow==2.7.0
- 7. tensorflow_gpu==2.6.0
- 8. wfdb==3.3.0

Chapter 5

XAI Methodology

5.1 XAI Analysis



Figure 5.1: Visualization of overall Journey of the Thesis - Specifically dealing with the XAI methods in this section.

This section presents the implementation of specific XAI methods and the techniques used to provide: 1) a comparison between XAI methods, and 2) a comparison between XAI vs. SME.

5.1.1 Pseudocode of XAI output processing pipeline

The following steps were taken to perform the XAI analysis and the subsequent subsections expand on each step:

Step 1: MITBIH processed image output directory was sorted to identify testing images.

Step 2: XAI outputs were generated for each test image.

Step 3: XAI outputs were processed (thresholded, filtered, & masked).

Step 4: Properties for clusters of interest (centroids, & boundaries) were identified

Step 5: Comparisons of the processed XAI outputs were performed.

5.1.2 Step 1 - Sorting and Identification of MITBIH images

A directory of all MITBIH images used by the ECG classifier model were sorted to identify images used for testing, because they were originally randomly distributed using the test_train_split function. A list of indices used for testing were identified and only those plotted images were passed to the XAI method in step 2. Algorithm 1 outlines the logic discussed in this subsection.

```
Algorithm 1: Tracking indices of sorted files
  Input : Directory of all MITBIH plotted images
  Output: XAI input images
1 TestTrainSplitfunction(input) \leftarrow list_of\_test\_file\_indices
2 Sort(list_of_test_file_indices)
3 for input do
      if input is in list_of_test_file_indices then
\mathbf{4}
          Load(input) \leftarrow images
\mathbf{5}
          Preprocess_input(images) \leftarrow XAI_input_images
6
          XAI\_input\_images \leftarrow pass to XAI method
\mathbf{7}
      end
8
9 end
```

5.1.3 Step 2 - Generating XAI outputs

From step 1 an array of XAI input images was passed to one of four XAI methods: Vanilla Saliency, SmoothGrad, GradCAM, & GradCAM++. XAI methods were obtained from tf-Keras-vis¹ [114]. Attention maps were produced for each input image provided to the XAI methods. Used to visualize area of high interest to the ECG classifier model (VGG-16) in its decision making process.

Algorithm 2 references the XAI methods: Vanilla Saliency, SmoothGrad, Grad-CAM, & GradCAM++, these methods are discussed in more detail in section 2.3. The activation function of the last CNN layer was altered to be a linear function. The output became directly proportional to the input only modified by the weights of hidden layer neurons, and not a complex mapping of a non-linear function. This

¹https://keisen.github.io/tf-keras-vis-docs/

provided a linear combination of all the neuronal weights and biases represented by a Taylor series. Magnitudes of the weights relative to pixels of the original image created a mapping of importance of the pixels in determining the output score [114].

Al	gorithm 2: Generating XAI outputs
Ι	nput : XAI input images
C	Dutput: XAI method specific visualization of attention map
10 F	ReplaceToLinear modifies last Conv. layer activation function to
	linear
11 S	$Score_function \leftarrow score$ (links output of last Conv. layer to
	predicted classification)
12 f	or input do
13	$Vanilla_Saliency(input, score) \leftarrow vs_XAI_output$
14	$SmoothGrad(input, score) \leftarrow sg_XAI_output$
15	$GradCAM(input, score) \leftarrow gc_XAI_output$
16	$GradCAM + +(input, score) \leftarrow gc_XAI_output$
17 e	nd

18 XAL-outputs passed to post-processing

Figure 5.2 shows attention map outputs generated by each XAI method listed in Algorithm 2. These outputs were generated for the same arbitrary sample input.



Figure 5.2: Visualization of steps from Algorithm 2 - XAI generated attention map outputs from 4 different XAI methods [Vanilla Saliency, SmoothGrad, GradCAM & GradCAM++

5.1.4 Step 3 - Processing XAI outputs

The XAI output images generated in Algorithm 2 were passed to the next stage for processing before segmenting the image. The images were thresholded into binary images using Otsu thresholding (see Appendix A Figure A.6) to ensure uniform processing of the image regardless of the XAI method colour map.

To filter the image, first, a median filter was applied to reduce noise. Unlike low-pass filtering, commonly used to reduce grain noise, median filtering allowed smoothing over an area with drastic differences in pixel values [115]. Median filtering was done in two discrete stages with increasing footprint sizes to allow fine denoising (small filter footprint) followed by coarse denoising (larger filter footprint) [115].

This was followed by Gaussian filtering, used to blur (smoothen) the edges of the clusters of interest in the image. The gaussian filter kernel applied a heavier weighting to the central region of the cluster relative to the periphery, and smoothed its edges [116]. Multi-stage filtering was preferred over single stage filtering. This removed high frequency noise and reduced pepper noise, commonly observed in XAI outputs. It also allowed a fine control over preventing the segments of interest from growing too large [115] [116]. After filtering the remaining clusters were segmented. These segmented clusters were passed to step 4.

The Gaussian filter allowed blurring and consolidating clusters of interest close to one another but distant beyond a few pixels. Gaussian filtering was used to reduce the total number of clusters to be analyzed. In preliminary testing it was noted that the XAI outputs often appeared similar to the SME annotations, except they were scattered in many small clusters. These neighbouring clusters were consolidated using the Gaussian blur filter. Algorithm 3: Processing XAI outputs

Input : XAI method specific visualization of attention map

Output: Filtered and Segmented XAI output

- 19 Thresholding(Binary + Otsu) (thresholds the XAI attention map to unify filtering regardless of XAI method)
- 20 Median_filtering_1 ← fine_denoising (smoothes and consolidates regions of grainy noise)
- 21 Median_filtering_2 ← coarse_denoising (separates distant larger sections and removes excess noise)
- 22 $Gaussian_filtering \leftarrow smoothing_regions$ (groups nearby neighbouring sections)
- **23** $Masking \leftarrow segmented_XAI_output$ (creates masks on each distinct cluster)
- 24 for input do
- **25** $XAI_segmentation_function(input) \leftarrow$ $Filtered_and_Segmented_XAI_output$
- 26 end

27 XAL-outputs passed to identify contour data

Figure 5.3 below shows a visual representation of the outputs generated at each step of Algorithm 3. In the figure, a single vanilla saliency XAI output is chosen as an arbitrary example.



Vanilla Saliency XAI Output



Thresholded Image (Binary + Otsu)



Median Filtering (fine filtering)



Median Filtering (coarse filtering)



Gaussian Filtering (blurring)



Identifying Clusters of Attention



Generating Masks to Segment Clusters

Figure 5.3: Visualization of steps from Algorithm 3 - Sequence of thresholding, filtering and segmenting steps to generate clusters of attention from an XAI output (Vanilla Saliency shown here).

5.1.5 Step 4 - Identifying Properties of Interest

The centroid and boundary positions were determined for each segmented cluster. The X and Y coordinates of the centroid, as well as the coordinates of the left, right, top and bottom most extreme positions of each segmented cluster were taken relative to the origin position of the image (top left corner). The coordinates were stored in a data-frame, and the areas of attention determined by XAI outputs were compared against the SME determined areas of attention in the next step. Figure 5.4 shows a visual representation of centroids and boundary positions around clusters of attention. Any clusters with Y coordinates corresponding to a location on the ECG record with no ECG lead data (II, V1, V2, and V5) were ignored as noise from the XAI output method.



Identifying Cluster Centroids



Identifying Cluster Boundaries

Figure 5.4: Visualization of centroid and boundary positions of each segmented cluster identified in figure 5.3

5.1.6 Step 5 - Comparison of XAI Methods

After the properties of interest for each image output by each XAI method are identified. The XAI methods were evaluated in an objective & rigorous manner to quantify trustworthiness. Section 5.2 presents details of the comparisons of XAI methods.

5.2 Comparison of XAI Methods

As established earlier in Section 2.3.3, trustworthiness of XAI generated explanations is broken into constituent components of **similarity** & **stability** and if the XAI can identify when there is **novelty** and what was **overlooked** in what the AI model has learned, all relative to the golden standard, subject matter experts.

5.2.1 Similarity

To test similarity between XAI outputs and SME annotations for a given record, SME annotation timestamps were converted to X-axis pixel positions for each corresponding ECG record (500x500 pixel). This process was performed for all rhythm and beat annotations by the SME, and the annotations positions were recorded in an array.

An XAI identified cluster from step 5.1.5 and SME annotation were considered a positive match if the SME annotation was anywhere between the left and right boundaries of the cluster. All individual clusters were compared against all SME annotations for each record. An array of pairwise values of cluster centroids & matching SME annotations was generated. Clusters with no matching SME annotations were recorded with a value of 0 for the SME annotation and vice versa. Two distance metrics, Jaccard and Hamming, were applied to each pairwise array to provide a measure of similarity between the XAI output and the SME annotations for each record. These distance metrics were applied to outputs from all XAI methods (Vanilla Saliency, SmoothGrad, GradCAM, and GradCAM++) separately for each record. Equation 5.2.1 shows a visualization of the XAI output array (centroid \pm boundary), SME annotations and resultant pairwise array (XAI_output, SME_annotation).

$$\begin{aligned} XAI_output &= \begin{bmatrix} 5 \pm 2 & 26 \pm 5 & 151 \pm 6 & 225 \pm 3 & 350 \pm 10 \end{bmatrix} \\ SME_annotations &= \begin{bmatrix} 1 & 157 & 222 & 400 \end{bmatrix} \\ pairwise_array &= \begin{bmatrix} (0,1) & (5,0) & (26,0) & (151,157) & (225,222) & (350,0) & (0,400) \end{bmatrix} \\ (5.2.1) \end{aligned}$$

5.2.2 Stability

To test stability of an XAI output, the performance of each XAI output was compared with all other XAI outputs for each individual record, in a pairwise comparison. An array of clusters from one XAI method was compared to an array from a second XAI method. Each cluster from the first XAI method was compared against all other clusters from the second XAI method. A positive match was considered if the centroid x-axis position for a cluster was anywhere between the left and right boundaries of the cluster from the second array. An array of pairwise values of matching cluster centroids was generated. Clusters from one array with no matching cluster from the second array were recorded with a value of 0 for the second array. and vice versa. The Pearson correlation distance metric was applied to each pairwise array to provide a measure of stability between the pairs of XAI outputs.

Equation 5.2.2 shows a visualization of the XAI output arrays (centroid \pm boundary) from 2 XAI methods and resultant pairwise array (XAI_output, SME_annotation) for a single ECG record.

$$\begin{aligned} XAI_output_1 &= \begin{bmatrix} 5 \pm 2 & 26 \pm 5 & 151 \pm 6 & 225 \pm 3 & 350 \pm 10 \end{bmatrix} \\ XAI_output_2 &= \begin{bmatrix} 10 \pm 7 & 30 \pm 1 & 151 \pm 100 & 400 \pm 10 \end{bmatrix} \\ pairwise_array &= \begin{bmatrix} (5, 10) & (26, 30) & (151, 151) & (225, 151) & (350, 0) & (0, 400) \end{bmatrix} \end{aligned}$$

$$(5.2.2)$$

5.2.3 Novelty

XAI methods were used to identify novel and overlooked learning by the underlying AI; this provided insights about the AI's performance. These insights were acquired by evaluating individual features uniquely highlighted by or overlooked by the XAI output relative to the SME annotations.

Figure 5.5 demonstrates how all possible novel and overlooked features are determined. Overlapping features between the array of XAI outputs and SME annotations were removed. Two resultant arrays were generated; a novel features array and an overlooked features array. The novel features array was made from features unique to the XAI output and the overlooked features array was made from features unique to SME annotation array.

The TF-IDF method (see Section 2.3.3) was applied to the new resultant arrays for every record. A TF-IDF score was calculated for each individual feature for each record. If available, the most likely novel feature and the most important overlooked feature from each record were passed on to the SME for further validation.

A low TF-IDF score meant that feature occurred more commonly in the entire collection of records (all ECG records for a given classification). Thus a feature in the novel feature array with low TF-IDF score was very likely to be a real novel feature rather than noise because it appeared repeatedly in many ECG records for the same classification. If a record had multiple novel features, the feature with the lowest TF-IDF score was identified as the most likely novel feature.

A high TF-IDF score for a feature meant that it was a unique identifying feature for that particular record. Features with high TF-IDF scores identified the most important overlooked features, from the remaining features not yet learned by the AI. If a record had multiple overlooked features, the feature with the highest TF-IDF value in the record was identified as the most important overlooked feature.

In figure 5.5, visualization of inputs shows an ECG signal (labelled Expert Annotations). The SME annotations are marked on the ECG signal and represented below the image in an array. The image to the right (labelled XAI Outputs) shows the locations of all XAI identified clusters of interest. The array below that image is a representation of all XAI output clusters of interest.

Figure 5.5 then shows the two representative arrays are being subtracted from each other to remove any values common between the XAI output and the SME annotation. The two resultant arrays are then passed to the TF-IDF method.

Finally, visualizations of outputs shows an example of novel and overlooked features on overlays of the XAI output + ECG signal. Overlooked Features figure shows a green line to mark overlooked feature in the ECG signal that was never learned by the AI. Using TF-IDF it is identified as the most important overlooked feature for that record. Novel features figure shows a red line highlighting a novel feature identified by the XAI. It has the lowest TF-IDF score and most likely identifies a novel feature learned by the AI.



Figure 5.5: Visualization of how novel and overlooked features are determined. Arrays of features are subtracted from one another to remove all common features, remaining items in each array are evaluated using TF-IDF (shown in Figure 2.9) used to identify the significance of the possible novel and all overlooked features.

5.3 XAI Performance Results

This section presents the results of the comparisons of XAI methods with other XAI methods and SME annotations discussed in section 5.2. The results of evaluating XAI methods for similarity, stability and novelty are presented in the following section. Presented here are overviews and summaries of the results with more detailed tables and complete results available in the appendix A.

5.3.1 Similarity

The similarity XAI comparison method from section 5.2.1 compared the XAI output and the SME annotation to objectively quantify how accurately each XAI method captured and presented the underlying learning done by the AI model.

XAI	Metric	Correct	\mathbf{AFIB}_μ	\mathbf{GSVT}_μ	\mathbf{SB}_μ	\mathbf{SR}_μ	Average	Combined Avg.
	Hamming	Y	0.67862	0.55041	0.61465	0.70683	$0.69880 {\pm} 0.20444$	0 60470 0 20608
Vanilla Salianay	Hamming	Ν	0.69230	0.65855	0.84617	0.59571	$0.63031 {\pm} 0.22098$	0.09470 ± 0.20008
vanna Sanency	Issand	Y	0.63994	0.51625	0.56646	0.65951	$0.65267 {\pm} 0.19852$	0.64016 ± 0.10000
	Jaccaru	Ν	0.65270	0.61900	0.80953	0.56263	$0.59411 {\pm} 0.21301$	0.04910 ± 0.19990
	Hamming	Y	0.89149	0.92248	0.86749	0.92899	$0.92306 {\pm} 0.13738$	0 02105 0 12002
Smooth Grad		Ν	0.90207	0.91033	1.00000	0.86922	$0.88949 {\pm} 0.15964$	0.92103±0.13903
	Jaccard	Y	0.86558	0.89688	0.82027	0.90367	$0.89714 {\pm} 0.15448$	0 80502 0 15570
		Ν	0.87376	0.88262	1.00000	0.84084	$0.86166{\pm}0.17050$	0.89302±0.15570
	Hamming	Y	0.53191	0.56970	0.58998	0.65566	$0.63842 {\pm} 0.24863$	0.69710 + 0.95594
CredCAM		Ν	0.50086	0.54146	0.60897	0.36973	$0.45102{\pm}0.29102$	0.02719 ± 0.23524
GradCAM	Issand	Y	0.49715	0.52805	0.53929	0.60721	$0.59160 {\pm} 0.23444$	0 50195 1 0 94099
	Jaccard	Ν	0.46593	0.50082	0.53333	0.34553	$0.41889 {\pm} 0.27016$	0.38123 ± 0.24022
	Hamming	Y	0.50235	0.52619	0.64596	0.62432	$0.60921 {\pm} 0.28916$	0 60477 1 0 20052
GradCAM++	пашші	Ν	0.57985	0.61452	0.45513	0.46767	$0.53509{\pm}0.26967$	0.004 77±0.28855
	Income	Y	0.47083	0.49021	0.59750	0.58101	0.56725 ± 0.27473	0 56221 ±0 27200
	Jaccard	Ν	0.53875	0.57318	0.39047	0.43868	$0.49990 {\pm} 0.25431$	0.00321±0.27399

Table 5.1: Measuring Similarity Between XAI Output and Expert Annotation

Table 5.1 presents a summary of the outputs of each XAI method (Vanilla Saliency, SmoothGrad, GradCAM & GradCAM++) evaluated using the two metrics (Hamming and Jaccard) presented in Section 5.2.1. The 'correct' column separates test data by correct or incorrect classification decisions made by the underlying AI model. On the table 5.1 the highest combined average scores are highlighted in green, and the lowest scores are highlighted in red.



⁽a) Box-plot of all XAI outputs Hamming similarity scores for test ECG records.

(b) Box-plot of all XAI outputs Jaccard similarity scores for test ECG records.

Figure 5.6: Distribution of Similarity metrics of test ECG records

Figure 5.6 shows the performance of XAI methods combined over all classifications for each of the two similarity metrics. The BW plot shows the distribution of all test records and the red dots overlay the positions of only the incorrectly classified records.

The SmoothGrad XAI method had the highest Hamming and Jaccard combined average score across all classes (AFIB, GSVT, SB, SR), GradCAM++ has the lowest combined averaged scores. SmoothGrad also had the smallest standard deviations for each metric relative to all other XAI methods, and GradCAM++ had the largest standard deviations for each metric. Figures 5.7 and 5.8 visualize the scores of SmoothGrad and GradCAM++ in more detail via a BW plot.



(a) Box-plot of XAI output vs.SME annotation compared (b) Box-plot of XAI output vs.SME annotation compared with Hamming similarity metric for test ECG records.

Figure 5.7: Distribution of SmoothGrad similarity metrics of test ECG records vs. Classification labels

Figures 5.7a and 5.7b are the BW plots for Hamming and Jaccard similarity metrics respectively applied to Smooth Grad XAI method outputs. The upper whisker, 75th and the median values are near 1.0 for AFIB and GSVT. Exact values for the BW plots are available in a full detailed table in the appendix in Table A.3.





(a) Box-plot showing distribution of Hamming Similarity metric between the XAI output and the Expert annotation for each individual patient record in the test set.

(b) Box-plot showing distribution of Jaccard Similarity metric between the XAI output and the Expert annotation for each individual patient record in the test set.

Figure 5.8: GradCAM++ XAI output similarity metrics for each record plotted against True labels

Figures 5.8a and 5.8b are the BW plot for Hamming and Jaccard similarity metric respectively applied to GradCAM++ XAI method. The IQR range between similarity scores for GradCAM++ was large, similar to the large standard deviation seen in table 5.1.

The BW plots presented a comparison of accuracy of the two XAI methods (SmoothGrad and GradCAM++) by having the XAI methods output what they identified as the relevant learned features by the underlying AI and comparing that output with SME annotations. In figure 5.7 incorrect classifications by the AI (red points) were mostly below the median value and clustered around the 25th percentile or below in each BW plot. Whereas in figure 5.8 the incorrect classifications by the underlying AI model were evenly distributed throughout the BW plot. Many incorrect classifications had high similarity scores on Hamming and Jaccard metrics. The order of XAI methods from greatest similarity to the SME annotations to least similar:

Smooth Grad >Vanilla Saliency >GradCAM >GradCAM++.

5.3.2 Stability

To test stability of the four XAI methods (1-Vanilla Saliency, 2-SmoothGrad, 3-GradCAM, and 4-GradCAM++), pairwise comparisons between all XAI methods were performed for each individual record using pearson correlation (see section 5.2.2). The pearson correlation score (PCr) of each XAI method pairwise comparison was recorded in the table 5.2. For example PCr_1v2 refers to the pearson correlation coefficient between XAI method 1 (Vanilla Saliency) and XAI method 2 (Smooth Grad).

Table 5.2: Stability measure between XAI outputs, using Pearson Correlation

Record	Filename	y_True	y_Pred	Correct	PCr_1v2	PCr_1v3	PCr_1v4	PCr_2v3	PCr_2v4	PCr_3v4
0	file100x000	SR	SR	Y	1.00000	1.00000	1.00000	1.00000	0.68976	1.00000
1	file100x001	SR	SR	Υ	1.00000	0.99999	0.59985	1.00000	0.81734	0.36977
2	file100x002	SR	SR	Υ	1.00000	0.99999	0.51003	1.00000	0.44811	0.39226
3	file100x004	SR	SR	Υ	1.00000	0.88922	0.80477	0.81766	0.82795	0.99777
5185	file234x173	SR	SR	Y	1.00000	0.81143	0.77011	0.64923	0.74210	0.57380
5186	$file 234 \times 175$	SR	SR	Υ	1.00000	0.99981	0.52400	0.99846	0.56143	0.99854
5187	file 234 x 177	SR	SR	Υ	1.00000	0.90303	0.66749	0.83292	0.75267	0.00000
5188	file234x178	SR	SR	Y	1.00000	0.99973	0.99973	0.78991	0.99999	1.00000
5189	$file 234 \times 180$	SR	SR	Υ	1.00000	0.75627	0.99998	0.63928	0.86787	1.00000
Average					0.96660	0.81381	0.81031	0.79948	0.78724	0.77011
Std. De	v				0.09405	0.17844	0.20372	0.20174	0.23406	0.30996



Pearson Correlation Scores Vs. Classifications

Figure 5.9: PCr Scores of Each XAI Method Pairwise Comparison vs. Test Record Classification

After pairwise comparisons were made between the XAI outputs of individual test records, the PCr scores were averaged. For example, to determine the relative stability of XAI method 1 (Vanilla Saliency) compared to XAI method 2 (SmoothGrad), the individual scores of PCr_1v2 were averaged (0.96660 \pm 0.0945). Table 5.2 is a truncated table that shows the salient components used to determine the stability

scores.

The highest PCr (average over all test records) between two XAI methods was 0.96660 for PCr_1v2 (between XAI methods 1 & 2, Vanilla Saliency and SmoothGrad respectively), highlighted in green in table 5.2. The lowest individual pairwise stability score was 0.77011 for PCr_3v4 (between XAI methods 3 & 4, GradCAM and GradCAM++ respectively), highlighted in red.

Figure 5.9 is a visualization of PCr scores shown in table 5.2 separated by record classes (y_True in table 5.2). The PCr between XAI 1 & 2 was significantly higher compared to all other pairwise comparisons. PCr_1v2 also had a small standard deviation, meaning far less variance in the XAI outputs of the Vanilla Saliency and SmoothGrad methods relative to all other pairwise comparisons.

Table 5.3: Overall Stability Scores for Each XAI method

XAI	Avg. Pearson Corr. Coeff.	St. Dev
Vanilla Saliency	0.86357	± 0.18084
Smooth Grad	0.85111	± 0.20363
GradCAM	0.79447	± 0.23775
GradCAM++	0.78922	± 0.25374

The PCr scores for a single XAI method for all pairwise comparisons were combined and averaged. For example, all scores of PCr_1v2, PCr_1v3, and PCr_1v4 were combined and averaged to produce the score 0.86357 ± 0.18084 . The Table 5.3 shows the stability score of each individual XAI method relative to all other XAI methods. Green and red highlights show the highest and lowest stability scores of 0.86357 ± 0.18084 (Vanilla Saliency) & 0.78992 ± 0.25374 (GradCAM++) respectively.

Figure 5.10 is a BW visualization of the distribution of individual pairwise comparisons (PCr scores) for each XAI method. Each BW plot show a distribution of 15570 pairwise comparisons (XAI outputs of 5190 test records • 3 pairwise comparisons).



Figure 5.10: Visualization of Overall Stability Scores for Each XAI method - Box plot display the distribution statistics of the stability scores for each pairwise comparison (PCr score). The waterfall plot overlay, displays the relative density of PCr scores for each XAI method.

5.3.3 Novelty & Overlooked Learning

Comparing novel and overlooked features identified by the XAI methods provided insights into the performance of the underlying AI model and help determine its overall trustworthiness, as discussed in Section 5.2.3. TF-IDF scores were used to evaluate the utility of each individual feature.

Table 5.4 shows TF-IDF scores for novel features from a sample of records, for Vanilla Saliency XAI method only. Features are separated by classifications (SR, GSVT, AFIB, & SB) in columns and individual records in rows. Multiple features with different TF-IDF scores in the same record are grouped together. The feature with the lowest TF-IDF score for any given record is highlighted in red. In Table 5.4 class SB has no records with identified novel features, GSVT, AFIB and SR have 39, 541 and 3166 records with possible novel features identified respectively.

Table 5.4: Novel learned features according to Vanilla Saliency XAI - TF-IDF scores for each record with unique features identified by the XAI only, separated by true class labels for each record.

	\mathbf{SR}			GSVT			AFIB			\mathbf{SB}	
TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record
0.00000	0	0	0.02404	0	0	0.02947	0	0			
0.41448	13	0	0.00000	1	0	0.00000	1	0			
0.44928	37	0	0.49167	4	0	0.29287	44	0			
0.39364	112	0	0.41003	66	0	0.25937	83	0			
0.41954	125	0	0.36227	240	0	0.27090	105	0			
0.41783	170	0	0.05129	311	0	0.25426	181	0			
0.42669	205	0	0.46485	358	0	0.23692	213	0			
0.40355	262	0	0.55741	393	0	0.22629	277	0			
0.46667	447	0	0.41071	206	1	0.23319	321	0			
0.43841	492	0	0.37230	373	1	0.28474	391	0			
0.05757	0	3089	0.12371	172	32	0.72681	399	509			
0.20731	159	3109	0.07647	227	35	1.02178	167	516			
0.19427	217	3112	0.22318	247	35	1.18730	406	516			
0.31597	437	3155	0.12830	38	36	0.16823	495	520			
0.20289	142	3166	0.09018	349	36	0.36149	310	528			
0.32054	433	3166	0.20732	489	39	0.20867	215	541			

Table 5.5 shows the TF-IDF scores for overlooked features that were never learned from a sample of records, for Vanilla Saliency XAI method only. The feature with the highest TF-IDF score for any given record is highlighted in green. In Table 5.5 GSVT, AFIB, SB, and SR have 37, 77, 95 and 1237 records with overlooked features identified respectively for the the Vanilla Saliency XAI.

Full tables for all four XAI methods are in Appendix A starting from Table A.4.

To help visualize the information shown in Tables 5.4 and 5.5 an example record (File102x010) was selected to show an example of novel and overlooked learning. An overlay of the record's ECG signal with the segmented processed XAI output was generated as shown in figure 5.11. This figure shows the ECG signal and locations where the AI paid the most attention in attempting to classify the ECG signal according to the Vanilla Saliency XAI method.

	\mathbf{SR}			GSVT			AFIB			\mathbf{SB}	
TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record
0.55669	0	0	0.00000	0	0	0.01668	0	0	0.00000	0	0
0.00000	1	0	0.78358	92	0	0.00000	1	0	0.42316	25	0
0.69965	352	0	0.93825	300	0	0.52065	139	0	0.55256	84	0
0.61241	1	1	0.10473	332	0	0.01281	303	0	0.38928	151	0
0.33074	259	1	0.41360	410	0	0.44762	327	0	0.47092	273	0
0.59535	2	2	0.36584	421	0	0.01362	106	1	0.36300	311	0
0.44770	260	2	0.09750	164	1	0.31893	125	1	0.34822	496	0
1.51324	79	1191	0.37196	43	34	0.00647	118	64	0.21975	45	76
0.42267	213	1215	0.30568	382	34	1.10557	28	70	0.32337	365	78
0.50582	218	1220	0.24735	214	35	0.54806	32	74	0.80170	37	95
0.54750	53	1234	0.06690	92	37	0.01010	284	77	0.89217	73	95
0.36557	189	1237	0.22582	377	37	0.26672	304	77	0.64702	233	95

Table 5.5: Overlooked features according to Vanilla Saliency XAI - TF-IDF scores for each record with unique features identified by the SMEs only, separated by true class labels for each record.

File102x010 - Segmented XAI Output with ECG Overlay



Figure 5.11: Visualization of XAI Method Output with ECG signal overlaid (coloured segments are used to represent distinct clusters only)

Table 5.6 is a more detailed look at a single record (File102x010), from a list of records summarized in tables 5.4 & 5.5 and in Appendix A Tables A.4 & A.5. In addition to the details presented in other tables mentioned, the x-axis locations of the novel and overlooked features identified by the TF-IDF method are presented along with the filename for that record. The feature with the lowest TF-IDF score and overlooked feature with highest TF-IDF score were highlighted in red and green respectively, the colours are used to draw a visual connection to figures 5.12 & 5.13. Table 5.6: Vanilla Saliency XAI Output - SR Class - List of Novel and Overlooked Features, the filename for the record and X-axis position on the record, of the feature of interest.

		Nove	lty		Overlooked					
TF-IDF	Feature	Record	Feat_x-axis	Filename	TF-IDF	Feature	Record	Feat_x-axis	Filename	
0.35053	124	255	21	file102x010	0.14599	10	10	107	file102x010	
0.30658	187	255	267	$file 102 \times 010$	0.32728	134	10	219	file102x010	
0.34672	415	255	472	file102x010	0.33529	197	10	276	$file 102 \times 010$	
					0.32355	293	10	362	file102x010	
					0.29873	470	10	71	file102x010	

Figure 5.12 shows two parts, the figure on the left shows an ECG overlaid with Vanilla Saliency XAI segmented output and vertical lines marking the 3 novel features identified in table 5.6. The figure on the right only highlights the novel feature (red line) with the lowest TF-IDF score.



Figure 5.12: Visualization of Novel Features of Vanilla XAI Method Output Listed in Table 5.6. Image on the left presents all unique features, image on the right identifies feature with the lowest TF-IDF score (most useful novel feature).

Figure 5.13 also shows two parts, the figure on the left shows an ECG overlaid with Vanilla Saliency XAI segmented output and vertical lines marking the 5 overlooked features identified in table 5.6. The figure on the right only highlights the overlooked feature (green line) with the highest TF-IDF score.



Figure 5.13: Visualization of Overlooked Features of Vanilla XAI Method Output Listed in Table 5.6 Image on the left presents all overlooked features, image on the right identifies feature with the highest TF-IDF score (most useful important overlooked feature).

Chapter 6

Quantifying Trust

6.1 Trust Score



Figure 6.1: Visualization of overall Journey of the Thesis - The final step of identifying how trustworthy the XAI is, is determined in this section.

To improve user trustworthiness towards the AI, this thesis explores the impact of the explainability aspect of trust using a series of equations. This section implements quantification of trust using these equations.
6.2 Equations

The trust equations are reiterated in this section:

Overall trust equation:

$$T = \left(\left[\frac{\sum_{i} (w_x T_x)_i}{\sum_{i} w_i} \right] + w_v T_v + w_r T_r + w_f T_f \right) / \sum_n w_n$$
(2.4.1)

Explainability term from equation 2.4.1:

$$T_x = \frac{\sum (w_{sim} E_{sim}, w_{stab} E_{stab})}{\sum w}$$
(2.4.6)

Similarity & Stability terms from equation 2.4.6:

$$E_{sim} = \frac{\sum (0.5M_{Jaccard}, 0.5M_{Hamming})}{1} , \ 0 \le M \le 1$$
 (2.4.4)

$$E_{stab} = \frac{\sum (N_{PearsonCorr})}{1} , \ 0 \le N \le 1$$
(2.4.5)

Equations for Novel and Overlooked learning:

$$K_n = \frac{\Sigma(Record_n | XAI_{novelty})}{\Sigma(Record_n)}$$
(2.4.7)

$$R_u = \frac{\Sigma(Record_u | XAI_{overlooked})}{\Sigma(Record_u)}$$
(2.4.8)

Individual XAI's trustworthiness equation:

$$E_{XAI} = [T_x, K_n, R_u], \ 0 \le T, K, R \le 1$$
 (2.4.9)

6.3 Contribution to Trustworthiness

An example of the aforementioned equations as they apply to the Vanilla Saliency XAI method:

Vanilla Saliency:

$$E_{sim} = \frac{\sum (0.5 \cdot 0.64916, 0.5 \cdot 0.69470)}{1}$$

$$E_{sim} = 0.67193$$
(6.3.1)

$$E_{stab} = \frac{\sum (1 \cdot 0.86357)}{1}$$

$$E_{stab} = 0.86357$$
(6.3.2)

$$T_x = \frac{\sum (0.5 \cdot 0.67193, 0.5 \cdot 0.86357)}{1}$$

$$T_x = 0.76775$$
(6.3.3)

$$K_n = \frac{717 |XAI_{overlooked}}{5190}$$

$$K_n = 0.138$$
(6.3.4)

$$R_u = \frac{348 |XAI_{overlooked}}{5190}$$

$$R_u = 0.067$$
(6.3.5)

$$E_{XAI} = [0.76775, 0.138, 0.067]$$
 (6.3.6)

A vector of values was created as shown in equations 6.3.6 to provide insight on the individual utility and trustworthiness of the Vanilla Saliency XAI method. The T_x term provided the trustworthiness measure for the XAI method, built upon similarity (E_{sim}) and stability (E_{stab}) measures. K_n identified the novel Knowledge that the AI learned. R_u identified any recommendations the XAI had to improve the AI model by identifying important overlooked features.

Only the Vanilla Saliency XAI method was shown as a worked example. The full table of values for the trust equations from all XAI methods was calculated and presented in table 6.1.

Table 6.1: Trust Equation Values for XAI Methods - Presenting Similarity, Stability, Explainability (T_x), Novelty (K_n), & Overlooked (R_u) scores for all XAI methods, and E_xai XAI trustworthiness vector.

	Vanilla Saliency	${\bf SmoothGrad}$	GradCAM	GradCAM++
M_jaccard	0.64916	0.89502	0.58125	0.56321
M_hamming	0.69470	0.92105	0.62719	0.60477
E_similarity	0.67193	0.90803	0.60422	0.58399
27	0.00055	0.05111		0.00040
N_pearson	0.86357	0.85111	0.79447	0.80262
$E_stability$	0.86357	0.85111	0.79447	0.80262
Тх	0 768	0.879	0 699	0.693
K n	0.138	0.124	0.152	0.140
IX_11	0.156	0.124	0.152	0.143
$R_{-}u$	0.067	0.045	0.072	0.074
E_xai	[0.768, 0.138, 0.067]	[0.879, 0.124, 0.045]	[0.699, 0.152, 0.072]	[0.693, 0.149, 0.074]

Figure 6.2 shows the E_{xai} vector for each XAI method, with values taken from table 6.1 E_{xai} for each XAI method. The vectors present the XAI methods visualised relative to each other in terms of Explainability scores, as well as their novelty and overlooked learning scores. This presents insights into how XAI methods may related to each other in various dimensions.



Figure 6.2: Visualization of E_xai vectors for each XAI method - Shows a visual representation of each XAI method on axis of Explainability, Novelty and Overlooked learning.

Table 6.1 also shows the E_{xai} vector for each XAI method. A vector of values that provides insights about explainability, novel and overlooked learning for a given XAI method. The results show that SmoothGrad had the highest explainability (0.87957) score among all the tested XAI methods, and identified the least novel and overlooked features in XAI's underlying learning. GradCAM and GradCAM++ had low similarity and stability scores compared to Vanilla or SmoothGrad and thus had low overall explainability scores (0.699 and 0.693 respectively). GradCAM and GradCAM++ provided more insights on novel learning and on overlooked learning and performed relatively similar to each other.

Chapter 7

Discussion

This section presents a discussion on the results provided in previous sections as well as identifying the limitations of the methods and the results and what those limitations mean.

7.1 Quantifying Trust Equations

Equation 2.4.9 in section 6 provided insights about the explanations generated by the XAI methods. Similarity and stability scores were combined together to produce T_x . A simple metric to help quickly identify how closely an XAI generated explanation resembles one produced by SMEs and other XAI methods. The novelty and overlooked learning scores $K_n \& R_u$ respectively, are metrics to rate the ability of the XAI method to identify what new features the AI learned or known features it missed in its learning. There is a pattern in the performance of the XAI methods shown by E_{xai} vectors in table 6.1. As the T_x value decreases, the likelihood of finding a novel or overlooked feature increases. This feature can be used to identify the XAI method best suited for specific stakeholders under specific conditions.

Applications that analyze the AI's learning, will find XAI methods with high K_n and R_u scores more useful to provide insights about the learning process of the AI. Compared to applications requiring an accurate and consistent explanation, the XAI method with higher T_x scores would be more preferable.

There is a need for validation of the trust scores E_{xai} for all the XAI methods by SMEs to determine how congruent the XAI generated explanation perceived qualities are relative to their scores. Thus a limitation of this study is that until the validation is performed, this thesis only presents a novel framework to objectively evaluate explanations and only proposes a relative performance ranking between the explanations generated by each XAI method.

7.2 XAI Methodologies

In section 5.2.1 clusters corresponding to areas with no ECG signal were discarded. This biases the outcome of similarity comparison metrics in favour of higher similarity between the XAI and SME. The reason for discarding the clusters was that while some of these clusters might represent incorrectly learned patterns by the underlying AI. It would require a significant effort to distinguish which clusters are a result of noise, actual learning, or artifacts introduced by the XAI methodology itself. Discarding this data for now results in a significant reduction in computational complexity. Since all the individual records are processed the same way, any impacts to the similarity comparison will apply to all records, minimizing skewness in the results.

In section 5.2.1 equation 2.3.5. There was an issue regarding the use of Jaccard similarity as a measure of comparison between datasets that some datasets could

be arbitrarily larger or smaller relative to the paired dataset. There may be an arbitrarily large union between the two datasets, while the intersection may or may not be affected. Thus the results of the similarity comparison could be arbitrarily affected by the size of the compared datasets. This problem is overcome by ensuring that all pairs of dataset being compared are of identical sizes as shown in equation 5.2.1.

The individual features used as the cumulative feature vocabulary in section 5.2.3 are partially idealized. There is sometimes a shift at the starting point of the signal, as to what part of the ECG wave the signal starts from. This is due to the random nature of the sampling and stride windows and how they they randomly capture a sample from the overall record. This randomized shifting between records would result in desynchronized feature positions between samples. To minimize the impact of this shifting effect, the features were given a .5 pixel (50 samples) buffer around the feature position. This way the feature in the vocabulary for TF-IDF is idealized and comparable between records.

7.3 XAI Results

Similarity

In section 5.3.1 similarity metric results were plotted to visualize the differences between the performance of SmoothGrad XAI and GradCAM++ XAI. The expectation (see section 2.3.3) was that test records that are incorrectly classified by the underlying AI model will have lower similarity scores vs high similarity scores for correctly classified records. The assumption being that SME annotations are most likely dissimilar to what the AI actually paid attention to in incorrectly classified records. The XAI methods that can produce high similarity scores for correct classifications, and low similarity scores for incorrect classifications provide a measure of accuracy of the underlying AI. This measure of accuracy is one of the concerns for all stakeholders (section 2.1.3) that affects the overall trustworthiness of the underlying AI.

The SmoothGrad XAI method produced higher similarity scores on the Hamming and Jaccard metrics for correctly classified records relative to incorrectly classified records. Figure 5.6 a & b both show SmoothGrad method's median similarity score is close to 1.0, and the red dots depicting incorrect classifications are mostly well below the median similarity score.

Additionally, the SmoothGrad XAI method had high similarity scores averaged over all classes (see figure 5.7). This means that SmoothGrad method was able to identify more features the underlying AI had learn that were closer to the thought pattern of the SME. Since the SME is considered the gold standard in explaining the classification decision, SmoothGrad XAI outputs are the closest to the gold standard. GradCAM++ produced the lowest average similarity scores across any classification, thus this method was furthest from identifying the underlying learning of the AI relative to the SME gold standard. Additionally, the GradCAM++ method was bad at distinguishing the similarity of correctly classified records to SME annotations vs. dissimilarity between SME annotations and the AI learning behind incorrectly classified records.

The Hamming and Jaccard similarity metrics are consistent in the rankings they produce, further corroborating the results. With two separate methods of measuring similarity between the XAI outputs and SME annotations, XAI method rankings remained the same. The similarity scores effectively provide a measure of accuracy of the XAI methods. Some XAI methods depict the underlying learning of the AI model more closely what the human trainers might deem useful, some XAI methods may be depicting less informative components of the learned characteristics. The disparity in XAI methods' dissimilarity to the SME annotation, is more closely evaluated by looking at the similarity metrics of each individual record, as well as looking at the outputs for novelty and overlooked components in section 5.3.3, tables 5.4 & 5.5. But without looking at any other comparison methods like novelty, similarity begins to provide an objective form of evaluating the quality of an explanation generated by an XAI method.

Stability

Section 5.3.2 the XAI methods Vanilla Saliency and GradCAM were determined to be the most and least stable XAI methods respectively. On one hand the Vanilla Saliency score being the most stable makes somewhat sense, when considering the similarity scores. Since Vanilla Saliency was in the middle of the pack in the similarity rankings, it stands to reason that the score would be considered somewhat stable relative to the other XAI methods as well. What is counter intuitive is the fact that GradCAM which also gave a middling score in the similarity rankings somehow was the least stable method overall. Just from intuition, SmoothGrad (highest similarity score) or GradCAM++ (lowest similarity score) would have made a lot of sense as the least stable XAI method, but the data says otherwise.

This means that the stability of an XAI method's performance relative to all other XAI methods over any individual record is not a function of how closely the XAI method's output matches the SME annotation, rather it is a completely independent feature from the similarity score and thus noteworthy enough to be included in the overall trust measurements for a given XAI method.

In section 5.3.2 the XAI methods Vanilla Saliency and GradCAM were determined to be the most and least stable XAI methods respectively. Since Vanilla Saliency was in the middle of the pack in the similarity rankings, it would be reasonable to assume that the stability score should be higher relative to the other XAI methods as well. However, counter intuitively, GradCAM which also ranked middle of the pack in the similarity rankings, was the least stable method overall. Based on intuition alone, SmoothGrad (highest similarity score) and GradCAM++ (lowest similarity score) should have been the most and least stable XAI methods respectively, however the results of the stability metrics suggest otherwise.

Additionally, as seen in figure 5.9 the stability scores between Vanilla Saliency method generated outputs and SmoothGrad outputs was significantly higher than the rest of the pairwise comparisons for all classes. Subsequently, the overall stability scores for both Vanilla Saliency and SmoothGrad were relatively close together and higher than GradCAM and GradCAM++, which were also close to each other in value (see table 5.3). Given that SmoothGrad XAI method is a derivative of the Vanilla Saliency method and GradCAM++ is a derivative of GradCAM, these results are further support of the validity of the stability comparison method.

The stability of an XAI method's performance relative to all other XAI methods over any individual record is not a function of how closely the XAI method's output matches the SME annotation (similarity). Rather, it is a completely independent feature providing insight into the consistency of an XAI method's performance, and it affects the overall trustworthiness of the underlying AI.

Novelty

The TF-IDF methodology in section 5.2.3 applied to an individual record compares the importance of the features present in that record, using a full vocabulary of all features extracted from all the records. From section 5.3.3 when looking at the figure 5.12, the lowest scored TF-IDF feature (the least uniquely predictive feature) of that record (highlighted in red) is used to identify novel features.

In the common use of TF-IDF, a feature present in a record with a low TF-IDF score means it is not a unique enough feature to help identify that particular record; the feature is too common across all records. In the context of this thesis and identifying novel features, a low TF-IDF score means that this particular feature is present in many records which is interpreted to mean this feature is likely an actual novel feature identified by the underlying AI.

To demonstrate this in another terms, lets compare a series of arbitrary sentences:

"This is a unique sentence",

"That is a common example", and

"This is that example".

The vocabulary from these sentences is as follows:

('a', 'common', 'example', 'is', 'sentence', 'that', 'This', 'unique')

Based on this vocabulary and how frequently each word/feature is used in all the sentences using the TF-IDF equation 2.3.9. Looking at sentence 1; "This is a unique sentence"; to a human reader it becomes obvious that the features "This" and "is", are common among all the sentences. Which means they don't help uniquely identify

the sentence, but they are an important feature to all the sentences because they structure the semantic meaning of the sentence.

Therefore, if the SME didn't identify any of these individual features as important when annotating, but an AI algorithm did identify them as meaningful features in its decision making criteria. Then it would be worth determining if the features that AI identified are informative and offer further insight.

For the purposes of the ECG signal evaluation in this thesis; the more common and not uniquely predictive a feature is the more likely it is to be present in ECG records of that class. The importance a feature plays to a record is measured by TF-IDF, and that is used to determine the utility of that feature in classification (SR, SB, AFIB, & GSVT) by the AI. Based on the rationale presented here, a feature with a low score is most likely a novel feature. However, to improve certainty in identifying novel features, the proposed method requires the SME to re-examine the signal and feature to determine the importance of the new insights that the AI might have gleaned. This method of determining novel features learned by the AI provides a better understanding of how the AI is improving upon the performance in the normal workflow. It provides specific insights into what the AI may have improved upon compared to SMEs.

Overlooked Learning

Similarly, from Section 5.3.3 when looking at the figure 5.13, the most predictive feature of that record (highlighted in green) is used to identify most important overlooked features. As discussed with the arbitrary sentences example above, in the sentence 1; "This is a unique sentence"; the features "unique" and "sentence" are present in only that one sentence but are very important in identifying that particular sentence. These features would have the largest TF-IDF score according to the equations 2.3.10. Since the AI did not identify these features, but an SME annotation exists, the XAI method can be used to identify the features that remain overlooked by the AI. Then a TF-IDF analysis determines which features are next most important features that were overlooked by the AI during training. Similar to the novel feature, these overlooked features need to be validated by the SME to determine their predictive importance.

If SME annotations exist for individual features of interest and AI has missed some of these features, as identified by the XAI method. A recursive training method can be implemented, that goes back to optimize the training of the AI, to ensure some number of the most informative features are learned by the AI. This methodology can help provide some degree of manual control over what features an AI learns to optimize performance where needed.

Chapter 8

Conclusion

This section provides future directions to explore and a summary of research contributions made by this thesis.

8.1 Summary

The goal of this research was to gain insight into how deep learning models make decisions so that user trust can be increased how the model identified features contribute to decisions made by the AI. This thesis provides a framework to evaluate the trustworthiness of AI model in medical applications with respect to the needs of the stakeholders involved. The thesis identified Explainability as one of the main constituent elements of trustworthiness and explored it in detail. Similarity, stability and novelty were identified as components to allow objective evaluation of explainability. This thesis hypothesized that measuring these components will create a framework to objectively evaluate explanations.

8.1.1 Components of Explainability

This thesis used a few existing distance metrics (Jaccard, Hamming, and Pearson Correlation) to measure similarity and stability between the explanations generated by XAI methods and the SMEs. These metrics inform the stakeholder of the level of similarity and stability an XAI method has relative to SMEs and other XAI methods.

Additionally, novel and overlooked learning are determined using TF-IDF scores. The scores measuring the presence of novel and overlooked learning are then combined with an average score measuring the similarity and stability of the XAI methods. These components together provide the user a repeatable and testable value to measure explainability, and provide insights about the explanations generated.

One of the insights about explanations generated is that the similarity and stability scores combine together to produce an inverse score to the novelty and overlooked learning scores. As discussed this information can be used to identify the best type of XAI methodology for the use case.

8.2 Future Directions

The XAI analysis provided measures of similarity and stability that allowed an exploration of the explainability aspect of trust in the underlying AI model. The analysis also provided some insight into the novel and overlooked learning by the underlying AI.

The proposed metrics and subsequent trust equations provide a basic framework to objectively evaluate XAI methods. However, more validation needs to be performed to increase confidence in the utility of the specific metrics and their ability to provide the objective evaluation of the XAI method.

In the immediate short term, one way to achieve this validation for similarity, and stability metrics is to use a synthetic ECG generator with predetermined features of diagnostic importance. Then utilize the various XAI methods on the outputs of VGG-16 based classifier model trained on the synthetic data. To determine the relative similarity and stability values of the XAI methods in a more rigorously controlled experiment.

Additionally, the utility of the novel and overlooked learning needs to be determined by a cardiology SME. The results of the outputs generated in this thesis can be provided to SMEs. They can determine if there is true predictive and/ or diagnostic value in the novel and overlooked learning outputs determined by the XAI analysis. Similarly, a number of SMEs should be presented with outputs from the trust equations 2.4.1 & 2.4.9 to determine if and how their trust in an AI model is impacted by the use of the equations.

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Appendix A

Your Appendix

1 include a list of all snomed codes - look up the merged_diagnosis.csv



Figure A.1: Visualization of all paradigms for training the AI model used to identify the ideal training paradigm and accompanying parameters.



Figure A.2: Visualization of impact of data split between training, validation and testing used to identify the ideal data split.



Figure A.3: Visualization of Independent Variables vs. Accuracy for models tested with all paradigms for training the AI model used to identify the ideal training paradigm and accompanying parameters.
Table A.1: Raw Data to accompany Figure A.6, Independent Variables vs. Accuracy for models
tested with all paradigms for training the AI model used to identify the ideal training paradigm
and accompanying parameters.

Paradigm	Model Label	Pre-trained Model	Subj. Iso.	Rand. Iso.	Balancing	Data Split	Train Acc.	Val Acc.	Test Acc.
1	50_50	pretrained	No	No	No	45/5/50	0.9375	0.9596	0.9423
1	20_80	pretrained	No	No	No	18/2/80	0.8791	0.8523	0.9112
1	20_80	pretrained	Yes	No	Weighted	22.5/2.5/75	0.981	0.95	0.7659
1	20_80	pretrained	Yes	Yes	No	22.5/2.5/75	1	0.8635	0.8021
1	30_70	None	No	No	Weighted	27/3/70	1	0.955	0.9715
1	30_70	None	No	No	No	27/3/70	0.9669	0.965	0.9714
1	30_70	pretrained	No	No	Weighted	27/3/70	0.985	0.9787	0.9831
1	30_70	pretrained	No	No	No	27/3/70	0.985	0.9787	0.9718
1	30_70	pretrained	Yes	Yes	Weighted	27/3/70	0.901	0.9281	0.8994
1	30_70	pretrained	Yes	Yes	No	27/3/70	0.9569	0.9679	0.8676
2	30_70	None	Yes	Yes	No	27/3/70	0.9837	0.9801	0.9121
2	30_70	None	Yes	Yes	Weighted	27/3/70	0.9875	0.9956	0.9066
2	30_70	None	Yes	Yes	Weighted 2x	27/3/70	0.9931	0.9956	0.8974
2	70_30	None	Yes	Yes	No	63/7/30	0.9937	0.9859	0.8469
2	70_30	None	Yes	Yes	Weighted	63/7/30	0.9987	0.9806	0.8565
2	70_30	None	Yes	Yes	Weighted 2x	63/7/30	0.985	0.9772	0.8585
1	70_30	pretrained	No	No	No	63/7/30	0.9406	0.95	0.9479
3	New_trained	pretrained	No	No	No	0/0/100	-	-	0.2428
3	New_trained	pretrained	No	No	No	70/10/20	0.95	0.9218	0.9211



Figure A.4: Summary of the VGG-16 based deep learning model used for classification.



Figure A.5: Flowchart of the full methodology and order of implementation of accompanying files provided in the associated github for replicating work presented in this thesis.

AI Models	Tran.	AI Data Type	XAI Methods	Vis. Type	LO/GL	MA/MS	Source
Logistic Regression	IN		-	-	-	-	ref
Linear Regression	IN		-	-	-	-	ref
Decision Trees	IN		-	-	-	-	ref
K-NN	IN		-	-	-	-	ref
Rule Based Learners	IN		-	-	-	-	ref
General Additive Model	IN	TAB	GA2M	TAB	GL	MS	ref
Bayesian Model	IN	GRAPH, TAB, TEXT	iBCM	GRAPH, TAB,TEXT	GL	MS	ref
Ensemble Methods	рц	TAB	dofragTroos	TAB	CL	MS	rof
& Decision Trees	r 11	IAD	dellagilees	IAD	GL	IN1.5	Ter
Ensemble Methods	РН	TAB	inTrees	TAB	GL	MS	ref
& Decision Trees		1112		1112	01	1110	101
Random Forest	$_{\rm PH}$	TAB	Forest Floor	TAB, IMG	Both	MS	\mathbf{ref}
CNN, RNN,	РН	IMG TAB	SWAF (Stacking With TEXT		LO	MS	ref
LSTM, GRU	1 11	imo, inb	Auxiliary Features)	1 DA1	LO	MS	101
SVM	$_{\rm PH}$	TAB	hybrid Rule-Extraction	TAB	GL	MS	\mathbf{ref}
SVM	$_{\rm PH}$	TAB	Bayesian Method	TAB	GL	MS	\mathbf{ref}
SVM	$_{\rm PH}$	IMG	Contribution Propagation	IMG	LO	MS	ref
Linear SVM	$_{\rm PH}$	IMG, TAB	Heatmap coloring viewer	TAB, IMG	GL	MS	\mathbf{ref}
NN, ANN, FF	$_{\rm PH}$	TAB	RxREN (Rule Extraction by Reverese Engineering)	TAB	GL	MS	ref
NN, Perceptron,	рн	TAB	Tree Regularization	TAB	GL	MS	ref
RNN w/ GRU,		IND	The regularization	IND	GL	1410	161
NN, DCN,	$_{\rm PH}$	IMG	Distilling ensemble	IMG	GL	MS	\mathbf{ref}

AI models w	ith related	and com	patible	XAI	methods
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NN	$_{\rm PH}$			TAB	LO	MS	ref
DCN, CNN, MLP	$_{\rm PH}$	IMG	Assess Parameter Sensitivity	IMG	LO	MS	ref
NN, AE, FF,							
RNN, LSTM,	$_{\rm PH}$	TEXT	rcNN	TEXT	GL	MS	ref
GRU, CNN							
DCN	$_{\rm PH}$	IMG	DkNN (Deepest K-NN)	IMG, TEXT	Both	MS	ref
0111 B 011	DU	IMG, TAB,	CDEP (Contextual	TAB, IMG,			
CNN, DCN	РН	TEXT	Decomposition)	TEXT	GL	MS	ref
CNN, DCN	$_{\rm PH}$	IMG, TEXT	Sensitivity Analysis	IMG, TEXT	Both	MS	ref
CNN	PH	IMG	LRP	IMG	Both	MA	ref
RNN, LSTM	PH	TEXT	Auto Rule Extraction	TEXT	GL	MS	ref
BiRNN, LSTM, GRU	$_{\rm PH}$	TEXT	LRP for LSTM	TEXT	LO	MS	ref
RNN, LSTM, GRU	$_{\rm PH}$	TEXT	VisRNN	IMG,TEXT	$_{\rm GL}$	MS	ref
			RETAIN (REverse				
RNN, LSTM, GRU	PH	TAB	Time AttentIoN model)	TAB	GL	MS	ref
Reg., SVM,			QII (Quantitative				
Decision Tree, RF	PH	TAB	Input Influence)	TAB	LO	MA	ref
,			DSA (Data-based SA).				
NN, SVM,	$_{\rm PH}$	TAB	MSA (Monte-Carlo SA),	TAB	LO	MA	ref
Ensemble Methods			CSA (Cluster-based SA)				
DCN, CNN, NN	PH	IMG	DeedSHAP	IMG	LO	MA	ref
SVM. NN. RF	РН	TAB	ASTRID	TAB	LO	MA	ref
NN. Decision Trees.							
Clustering, Ensemble	$_{\rm PH}$	TAB	ALEplot (Accumulated	TAB	LO	MA	ref
Methods, Stat. Models			Local Effects)				
		IMG, TAB.		TAB, IMG,			
ANY, Classification	PH	TEXT	LIME	TEXT	Both	MA	ref
			LORE (Local Rule-				
ANY, Classification	PH	TAB	based Explanation)	TAB	LO	MA	ref
ANY, Decision Trees.							
Random Forest	PH	TAB	Prospector	TAB	LO	MA	ref
CNN, DCN, NN,	PH	IMG	Realtime Saliency	IMG	$_{\rm GL}$	MA	ref
ANY, Classification	PH	TAB, IMG	DarkSight	TAB. IMG	GL	MA	ref
MC. Classification		, -	Bayesian averaging	, -			
Trees	IN	TAB	over decision trees	TAB	GL	MS	ref
SVM Logistic			SPDA (Sparsed Penalized				
Regression, LDA	IN	TAB	Discriminant Analysis)	TEXT	GL	MS	ref
DBN. AE.							
DAE, BM, RBM	PH	IMG	Activation Maximization	IMG	LO	MA	ref
DCN, CNN, DBN, DN,	РН	IMG	Gradient-based Saliency Maps	IMG	LO	MA	ref
Classification		1.110		1	20		101
LDA. SVM	IN	ANY	BCM (Bayesian Case Model)	ANY	GL	MS	ref
DN	РН	IMG	DeConvolutional Nets	IMG	LO	MA	ref
CNN	PH	IMG	Guided Backprop	IMG	LO	MA	ref
BN. MCMC	IN	TAB	Bayes Bule Lists	TAB	GL	MS	ref
CNN	РН	IMG	CAM	IMG	LO	MA	ref
DCN.		TAB, IMG.	SHAP (SHapley	TAB, IMG.			101
Ensemble Methods	PH	TEXT	Additive exPlanations)	TEXT	Both	MA	ref
DCN. CNN	РН	IMG	Grad-CAM	IMG	LO	MA	ref
,		1.40					101

DCN	PH	IMG	PDA (Prediction	IMG	LO	МА	ref
			Difference Analysis)				
DCN, MLP	PH	IMG	Deep Taylor Decomposition	IMG	LO	MA	ref
DCN	РН	IMG	Sensitivity-n (Gradient-based	IMG	LO	MA	ref
			attribution method)				
Linear CNN, DN	PH	IMG	IG (Integrated Gradients)	IMG	LO	MA	ref
MLP. CNN. DCN	РН	IMG	PatternNet and	IMG	LO	MA	ref
,,			PatternAttribution				
Classification,	РН	IMG	TCAV (Testing with	IMG	GL	MA	ref
Regression		1110	Concept Activation Vectors)	1	01		101
CNN, DCN, Image	РН	IMG	BISE	IMG	LO	MA	ref
Classification NN		1110	1000	1	20		101
DCN, CNN	PH	IMG	Grad-CAM++	IMG	LO	MA	ref
			(IRT & OSFT) Interpretability				
DCN, CNN	$_{\rm PH}$	IMG	Randomization Test and	IMG	LO	MA	ref
			One-Shot Feature Testing				
DCN, CNN	$_{\rm PH}$	IMG	SR (Salient Relevance) map	IMG	LO	MA	ref
DCN, CNN	$_{\rm PH}$	IMG	Spectral Relevance Analysis	IMG	GL	MA	ref
CNN	рц	IMC	GAM (Global	IMC	CL	МА	rof
Olivity	1 11	inite	Attribution Mapping)	IMG	GL	MIA	Ter
			ACE (Automatic				
CNN	PH	TAB, IMG	Concept-based	IMG	GL	MA	ref
			Explanations)				
VAE AF DCN	рц	IMC	CaCE (Causal	IMC	CL	МА	rof
VAE, AE, DON	1 11	ING	Concept Effect)	IMG	GL	MIA	Ter
DON	IN	IMC	NAMs (Neural	IMC	CI	MC	
DON	111	110105	Additive Models)	IMG	GL	INLO	rei
CNN, DCN	$_{\rm PH}$	IMG	SG (SmoothGrad)	IMG	LO	MA	ref



XAI Vanilla Saliency Output

XAI OTSU Thresholded Image





Figure A.6: Visualization of Otsu binary thresholding (dashed line at 0.060543224), all pixels are .

OTSU threshold is determined by creating a histogram representation of pixel values for an image and then separating the histogram into two classes using a threshold to minimize intra-class intensity variance, or equivalently, by maximizing inter-class variance [117]. This method is an analogue of linear discriminant analysis (LDA) or equivalent to K-means clustering on the intensity histogram to determine the optimal threshold to create a binary image.

XAI	Metric	Cor.	AFIB	GSVT	\mathbf{SB}	\mathbf{SR}	Combined	
			count 562.000000	count 79.000000	$count \ 119.000000$	$count \ 4119.000000$	$count \ 4879.000000$	
			mean 0.678622	$mean \ 0.550406$	mean 0.614651	mean 0.706830	mean 0.698799	
			std 0.214634	std 0.229354	std 0.243665	std 0.199468	std 0.204438	
		v	min 0.000000	$\min 0.076900$	min 0.000000	$\min 0.000000$	min 0.000000	
	60	1	$25\% \ 0.538500$	$25\% \ 0.348450$	$25\% \ 0.454500$	$25\% \ 0.583300$	25% 0.571400	
<u>a</u>	nin		50% 0.699100	$50\% \ 0.555600$	$50\% \ 0.636400$	$50\% \ 0.736800$	$50\% \ 0.727300$	
lin	ami		$75\% \ 0.857100$	$75\% \ 0.750000$	$75\% \ 0.800000$	$75\% \ 0.857100$	$75\% \ 0.857100$	
Va	Ĥ		max 1.000000	$\max 0.952400$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	
			count 21.000000	count 127.000000	count 3.000000	$count \ 160.000000$	$count \ 311.000000$	
			mean 0.692305	mean 0.658554	mean 0.846167	mean 0.595713	mean 0.630313	
			std 0.249470	std 0.228517	std 0.153850	std 0.206086	std 0.220981	
		N	$\min \ 0.071400$	$\min 0.076900$	min 0.692300	$\min 0.105300$	$\min \ 0.071400$	
			$25\% \ 0.588200$	$25\% \ 0.500000$	$25\% \ 0.769250$	$25\% \ 0.473700$	$25\% \ 0.500000$	
			$50\% \ 0.714300$	50% 0.666700	$50\% \ 0.846200$	$50\% \ 0.631600$	$50\% \ 0.666700$	
			$75\% \ 0.857100$	$75\% \ 0.839750$	$75\% \ 0.923100$	$75\% \ 0.740100$	$75\% \ 0.789500$	
			$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	
			count 562.000000	$\operatorname{count}\ 79.000000$	count 119.000000	${\rm count}\ 4119.000000$	${\rm count}\ 4879.000000$	
				mean 0.639937	mean 0.516247	$mean \ 0.566463$	mean 0.659514	mean 0.652670
			std 0.207119	std 0.217078	std 0.234924	std 0.194258	std 0.198544	
		Y	min 0.000000	$\min \ 0.071400$	min 0.000000	$\min 0.000000$	$\min 0.000000$	
		-	$25\% \ 0.500000$	$25\% \ 0.324550$	$25\% \ 0.416700$	$25\% \ 0.538500$	$25\% \ 0.533300$	
	rd		50% 0.666700	$50\% \ 0.526300$	$50\% \ 0.583300$	$50\% \ 0.687500$	50% 0.666700	
	cca		$75\% \ 0.800000$	$75\% \ 0.692300$	$75\% \ 0.727300$	$75\% \ 0.800000$	$75\% \ 0.800000$	
	Ja		max 1.000000	$\max 0.909100$	$\max 1.000000$	max 1.000000	$\max 1.000000$	
			count 21.000000	$count \ 127.000000$	count 3.000000	$count \ 160.000000$	count 311.000000	
			mean 0.652705	mean 0.618998	$mean \ 0.809533$	mean 0.562634	mean 0.594114	
			std 0.245617	std 0.223707	std 0.179739	std 0.194924	std 0.213017	
		N	min 0.066700	$\min \ 0.071400$	min 0.642900	min 0.100000	min 0.066700	
			$25\% \ 0.555600$	$25\% \ 0.461500$	$25\% \ 0.714300$	$25\% \ 0.453375$	$25\% \ 0.464100$	
			50% 0.666700	$50\% \ 0.615400$	$50\% \ 0.785700$	50% 0.600000	$50\% \ 0.615400$	
			75% 0.800000	75% 0.789500	$75\% \ 0.892850$	75% 0.700000	75% 0.750000	
			$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	

Table A.3: Similarity Results - Full Dataset

			count 562.000000	count 79.000000	$count \ 119.000000$	$count \ 4119.000000$	$count \ 4879.000000$
			mean 0.678622	mean 0.550406	mean 0.614651	mean 0.706830	mean 0.923064
			std 0.214634	std 0.229354	std 0.243665	std 0.199468	std 0.137383
		3.7	min 0.000000	min 0.076900	min 0.000000	min 0.000000	min 0.055600
		Ŷ	25% 0.538500	25% 0.348450	$25\% \ 0.454500$	$25\% \ 0.583300$	25% 0.909100
ч	guin		50% 0.699100	50% 0.555600	50% 0.636400	50% 0.736800	50% 1.000000
oot	u u u		75% 0.857100	75% 0.750000	75% 0.800000	75% 0.857100	75% 1.000000
\mathbf{S} m	Hau		$\max 1.000000$	max 0.952400	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 21.000000	count 127.000000	count 3.000000	count 160.000000	count 311.000000
			mean 0 692305	mean 0 658554	mean 0.846167	mean 0 595713	mean 0 889486
			std 0 249470	std 0 228517	std 0 153850	std 0 206086	std 0 159640
			min 0.071400	min 0.076900	min 0.692300	min 0.105300	min 0.214300
		N	25% 0.588200	25% 0 500000	25% 0.760250	25% 0.472700	25% 0.846200
			50% 0.714200	2378 0.300000	20% 0.846200	2576 0.475700	2376 0.840200
			50% 0.714500	50% 0.886700	50% 0.846200	50% 0.651600	50% 0.944400
			1 000000	1 000000	1 000000	1000000	1000000
			max 1.000000	max 1.000000	max 1.000000	max 1.000000	max 1.000000
			count 562.000000	count 79.000000	count 119.000000	count 4119.000000	count 4879.000000
			mean 0.639937	mean 0.516247	mean 0.566463	mean 0.659514	mean 0.897143
			std 0.207119	std 0.217078	std 0.234924	std 0.194258	std 0.154479
		Y	min 0.000000	min 0.071400	min 0.000000	min 0.000000	min 0.052600
			$25\% \ 0.500000$	$25\% \ 0.324550$	$25\% \ 0.416700$	$25\% \ 0.538500$	$25\% \ 0.833300$
	pri		50% 0.666700	$50\% \ 0.526300$	$50\% \ 0.583300$	50% 0.687500	$50\% \ 1.000000$
	Iccar		75% 0.800000	$75\% \ 0.692300$	$75\% \ 0.727300$	$75\% \ 0.800000$	$75\% \ 1.000000$
	Ja		$\max 1.000000$	$\max 0.909100$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 21.000000	count 127.000000	$\operatorname{count} 3.000000$	$count \ 160.000000$	$count \ 311.000000$
		N	mean 0.652705	mean 0.618998	mean 0.809533	mean 0.562634	mean 0.861658
			std 0.245617	std 0.223707	std 0.179739	std 0.194924	std 0.170498
			min 0.066700	min 0.071400	min 0.642900	min 0.100000	min 0.200000
			Ν	25% 0.555600	$25\% \ 0.461500$	$25\% \ 0.714300$	$25\% \ 0.453375$
			50% 0.666700	$50\% \ 0.615400$	50% 0.785700	50% 0.600000	50% 0.894700
			$75\% \ 0.800000$	$75\% \ 0.789500$	$75\% \ 0.892850$	$75\% \ 0.700000$	$75\% \ 1.000000$
			max 1.000000	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 562.000000	count 79.000000	count 119.000000	count 4119.000000	count 4879.000000
			mean 0.678622	mean 0.550406	mean 0.614651	mean 0.706830	mean 0.698799
			std 0.214634	std 0.229354	std 0.243665	std 0.199468	std 0.204438
			min 0.000000	min 0.076900	min 0.000000	min 0.000000	min 0.000000
F		Y	25% 0.538500	25% 0.348450	25% 0.454500	25% 0.583300	25% 0.571400
AN	ing		50% 0 699100	50% 0 555600	50% 0 636400	50% 0 736800	50% 0 727300
Opi	E E		75% 0.857100	75% 0 750000	75% 0.800000	75% 0.857100	75% 0.857100
5 5	Har		max 1 000000	max 0.952400	max 1 000000	max 1 000000	max 1 000000
•			count 21 000000	count 127 000000	count 3 000000	count 160 000000	count 311 000000
			mean 0.692305	moan 0.658554	mean 0.846167	mean 0 595713	mean 0.630313
			std 0 240470	etd 0 228517	etd 0 153950	std 0 206086	std 0 220091
			min 0.071400	min = 0.076000	min 0.603200	min 0.105200	min 0.071400
		N	250% 0 500000	25% 0 500000	25% 0.760250	25% 0 472700	25% 0 500000
			2070 0.088200	2070 U.SUUUUU	2070 0.709200	2070 0.473700	20% 0.000000
			50% 0.714300	50% 0.666700	50% 0.846200	5U% 0.631600	5U% U.666700
			75% 0.857100	75% 0.839750	75% 0.923100	75% 0.740100	75% 0.789500
			$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$

			count 562.000000	count 79.000000	count 119.000000	count 4119.000000	count 4879.000000
			mean 0.639937	mean 0.516247	mean 0.566463	mean 0.659514	mean 0.652670
			std 0.207119	std 0.217078	std 0.234924	std 0.194258	std 0.198544
		v	min 0.000000	min 0.071400	min 0.000000	min 0.000000	min 0.000000
		I	$25\% \ 0.500000$	$25\% \ 0.324550$	$25\% \ 0.416700$	$25\% \ 0.538500$	$25\% \ 0.533300$
	ų		50% 0.666700	$50\% \ 0.526300$	$50\% \ 0.583300$	50% 0.687500	$50\% \ 0.666700$
	ccal		75% 0.800000	$75\% \ 0.692300$	$75\% \ 0.727300$	75% 0.800000	$75\% \ 0.800000$
	Ja		$\max 1.000000$	$\max 0.909100$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 21.000000	count 127.000000	count 3.000000	count 160.000000	count 311.000000
			mean 0.652705	mean 0.618998	mean 0.809533	mean 0.562634	mean 0.594114
			std 0.245617	std 0.223707	std 0.179739	std 0.194924	std 0.213017
		N	min 0.066700	$\min \ 0.071400$	min 0.642900	min 0.100000	min 0.066700
		IN	$25\% \ 0.555600$	$25\% \ 0.461500$	$25\% \ 0.714300$	$25\% \ 0.453375$	$25\% \ 0.464100$
			50% 0.666700	$50\% \ 0.615400$	$50\% \ 0.785700$	50% 0.600000	$50\% \ 0.615400$
			75% 0.800000	$75\% \ 0.789500$	$75\% \ 0.892850$	75% 0.700000	$75\% \ 0.750000$
			$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 562.000000	count 79.000000	count 119.000000	count 4119.000000	count 4879.000000
			mean 0.678622	$mean \ 0.550406$	mean 0.614651	mean 0.706830	mean 0.698799
			std 0.214634	std 0.229354	std 0.243665	std 0.199468	std 0.204438
		v	min 0.000000	min 0.076900	min 0.000000	min 0.000000	min 0.000000
	50	Y	$25\% \ 0.538500$	$25\% \ 0.348450$	$25\% \ 0.454500$	$25\% \ 0.583300$	$25\% \ 0.571400$
++	guin		50% 0.699100	50% 0.555600	$50\% \ 0.636400$	50% 0.736800	$50\% \ 0.727300$
ad-	u u		75% 0.857100	$75\% \ 0.750000$	$75\% \ 0.800000$	75% 0.857100	$75\% \ 0.857100$
C G	Ha		$\max 1.000000$	$\max 0.952400$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 21.000000	count 127.000000	count 3.000000	count 160.000000	count 311.000000
			mean 0.692305	mean 0.658554	mean 0.846167	mean 0.595713	mean 0.630313
			std 0.249470	std 0.228517	std 0.153850	std 0.206086	std 0.220981
		N	min 0.071400	min 0.076900	min 0.692300	min 0.105300	min 0.071400
		1	$25\% \ 0.588200$	$25\% \ 0.500000$	$25\% \ 0.769250$	$25\% \ 0.473700$	$25\% \ 0.500000$
			$50\% \ 0.714300$	50% 0.666700	$50\% \ 0.846200$	50% 0.631600	50% 0.666700
			75% 0.857100	75% 0.839750	$75\% \ 0.923100$	75% 0.740100	$75\% \ 0.789500$
			max 1.000000	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$
			count 562.000000	count 79.000000	count 119.000000	count 4119.000000	count 4879.000000
			mean 0.639937	mean 0.516247	mean 0.566463	mean 0.659514	mean 0.652670
			std 0.207119	std 0.217078	std 0.234924	std 0.194258	std 0.198544
		v	min 0.000000	$\min \ 0.071400$	$\min\ 0.000000$	$\min 0.000000$	min 0.000000
		-	$25\% \ 0.500000$	$25\% \ 0.324550$	$25\% \ 0.416700$	$25\% \ 0.538500$	$25\% \ 0.533300$
	rd		50% 0.666700	$50\% \ 0.526300$	$50\% \ 0.583300$	$50\% \ 0.687500$	$50\% \ 0.666700$
	cca		$75\% \ 0.800000$	$75\% \ 0.692300$	$75\% \ 0.727300$	$75\% \ 0.800000$	$75\% \ 0.800000$
	Ja		max 1.000000	$\max 0.909100$	$\max 1.000000$	$\max 1.000000$	max 1.000000
			count 21.000000	$count \ 127.000000$	$\operatorname{count} 3.000000$	$count \ 160.000000$	count 311.000000
			mean 0.652705	mean 0.618998	mean 0.809533	mean 0.562634	mean 0.594114
			std 0.245617	std 0.223707	std 0.179739	std 0.194924	std 0.213017
		N	min 0.066700	$\min \ 0.071400$	$\min 0.642900$	min 0.100000	$\min 0.066700$
			$25\% \ 0.555600$	$25\% \ 0.461500$	$25\% \ 0.714300$	$25\% \ 0.453375$	$25\% \ 0.464100$
			50% 0.666700	$50\% \ 0.615400$	$50\% \ 0.785700$	50% 0.600000	$50\% \ 0.615400$
			$75\% \ 0.800000$	$75\% \ 0.789500$	$75\% \ 0.892850$	$75\% \ 0.700000$	$75\% \ 0.750000$
			$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$	$\max 1.000000$

	\mathbf{SR}			GSVT			AFIB			\mathbf{SB}	
TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record
0.00000	0	0	0.02404	0	0	0.02947	0	0			
0.41448	13	0	0.00000	1	0	0.00000	1	0			
0.44928	37	0	0.49167	4	0	0.29287	44	0			
0.39364	112	0	0.41003	66	0	0.25937	83	0			
0.41954	125	0	0.36227	240	0	0.27090	105	0			
0.41783	170	0	0.05129	311	0	0.25426	181	0			
0.42669	205	0	0.46485	358	0	0.23692	213	0			
0.40355	262	0	0.55741	393	0	0.22629	277	0			
0.46667	447	0	0.41071	206	1	0.23319	321	0			
0.43841	492	0	0.37230	373	1	0.28474	391	0			
0.01573	0	1	0.36679	245	2	0.04501	496	0			
0.34367	25	1	0.43982	275	2	0.44725	57	1			
0.34506	71	1	0.29375	405	2	0.38102	75	1			
0.36037	117	1	0.32407	438	2	0.36783	182	1			
0.33962	161	1	0.03146	55	3	0.42374	217	1			
0.33831	249	1	0.42979	123	3	0.39609	263	1			
0.35708	294	1	0.53664	174	3	0.33598	360	1			
0.36733	343	1	0.64348	217	3	0.06585	492	1			
0.33575	388	1	0.05871	366	3	0.55746	84	2			
0.34792	477	1	0.30936	198	4	0.52935	165	2			
0.02414	0	2	0.22794	213	4	0.61996	282	2			
0.54314	97	2	0.25799	319	4	0.60527	408	2			
0.50236	143	2	0.02992	488	4	0.03166	488	2			
0.49221	191	2	0.21412	493	4	0.31458	32	3			
0.55563	462	2	0.17856	496	4	0.27311	57	3			
0.01723	0	3	0.13156	8	5	0.28453	82	3			
0.38433	31	3	0.15777	118	5	0.30585	101	3			
0.37952	77	3	0.01513	299	5	0.33590	119	3			
0.36241	122	3	0.17657	384	5	0.25872	230	3			
0.34352	166	3	0.20662	435	5	0.25048	348	3			
0.35368	223	3	0.04238	421	6	0.23961	383	3			
0.41509	300	3	0.27865	235	7	0.25449	430	3			
0.35857	393	3	0.33413	249	7	0.12290	484	3			
0.53617	105	4	0.19071	317	7	1.42059	245	4			
0.53172	152	4	0.22317	365	7	1.08151	365	4			
0.49719	197	4	0.24619	433	7	0.37422	102	5			
0.50592	242	4	0.01634	354	8	0.43484	214	5			
0.56372	285	4	0.02270	165	9	0.35071	368	5			
0.52531	374	4	0.19898	174	9	0.03419	476	5			
0.35087	3	5	0.15936	192	9	0.32191	23	6			
0.38105	45	5	0.23860	224	9	0.28946	53	6			
0.36554	90	5	0.13619	250	9	0.33035	90	6			
0.32621	132	5	0.01237	476	9	0.30091	124	6			
0.33205	176	5	0.18647	478	9	0.31428	190	6			
0.31167	225	5	0.21105	492	9	0.37740	226	6			
0.38540	402	5	0.25307	50	10	0.03717	472	6			

Table A.4: Novelty - Vanilla Saliency - Full Results

0.39659	11	6	0.16903	141	10	0.32066	41	7
0.37645	104	6	0.02921	287	10	0.31466	78	7
0.36505	151	6	0.30291	131	11	0.32711	112	7
0.37201	196	6	0.26763	149	11	0.30377	150	7
0.41285	241	6	0.36322	207	11	0.34994	224	7
0.37347	328	6	0.32839	42	12	0.33408	288	7
0.36641	373	6	0.24260	288	12	0.34165	369	7
0.39292	419	6	0.47413	225	13	0.38097	465	7
0.40642	466	6	1.20090	164	14	0.56809	93	8
0.02787	0	7	0.88485	176	14	0.59185	128	8
0.64759	90	7	1.00149	371	14	0.65436	167	8
0.58614	136	7	0.02725	275	15	0.69870	246	8
0.55217	180	7	0.20367	410	16	0.52102	330	8
0.61637	317	7	0.15007	420	16	0.02757	464	8
0.59483	362	7	0.16985	439	16	0.24779	492	8
0.02129	0	8	0.13603	148	17	0.25341	26	9
0.47700	102	8	0.01776	330	18	0.26636	49	9
0.44311	149	8	0.09593	452	19	0.22531	114	9
0.43855	194	8	0.39786	14	20	0.21482	202	9
0.45796	238	8	0.33180	79	20	0.23784	233	9
0.45280	280	8	0.04554	263	20	0.27396	311	9
0.43561	369	8	0.07505	74	21	0.25956	413	9
0.01340	0	9	0.19008	405	21	0.30732	2	10
0.32637	41	9	0.09909	196	22	0.26643	198	10
0.32101	57	9	0.06867	7	23	0.45074	397	10
0.28705	84	9	0.26573	75	23	0.36936	482	10
0.27227	129	9	0.29315	262	23	0.29409	146	11
0.27500	173	9	0.06330	440	24	0.29880	327	11
0.29389	218	9	0.04096	251	25	0.41369	126	12
0.29154	265	9	0.27024	271	25	0.38829	222	12
0.28490	310	9	0.03409	62	26	0.40453	338	12
0.29039	354	9	0.12634	495	27	0.57952	32	13
0.31764	396	9	0.31816	80	28	0.22923	6	15
0.29757	452	9	0.11421	306	28	0.22162	8	15
0.30413	496	9	0.08275	117	29	0.24263	159	15
0.38599	20	10	0.08885	428	29	0.23339	352	15
0.35488	194	10	0.20531	381	31	0.05032	436	15
0.38939	237	10	0.12371	172	32	0.42594	489	15
0.05201	0	11	0.07647	227	35	0.41834	35	16
1.13626	35	11	0.22318	247	35	0.41120	122	16
1.03687	171	11	0.12830	38	36	0.46247	285	16
0.01447	0	12	0.09018	349	36	0.04072	432	16
0.32005	14	12	0.20732	489	39	0.36594	471	16
0.33306	61	12				0.40458	499	16
0.31242	106	12				0.34467	69	17
0.30113	149	12				0.30817	125	17
0.33151	190	12				0.33274	161	17
0.28243	193	12				0.38332	225	17
0.31122	238	12				0.47065	265	17
0.31364	328	12				0.41731	342	17

0.28584	375	12	0.29098	90	18
0.32702	465	12	0.27860	131	18
0.03296	0	13	0.29805	339	18
0.67886	140	13	0.24668	391	18
0.66551	186	13	0.35125	472	18
0.73208	230	13	0.29498	78	20
0.75510	405	13	0.27944	98	20
0.35238	74	14	0.41025	166	21
0.30978	334	14	0.35911	371	21
0.33450	344	14	0.26321	76	22
0.43135	430	14	0.26800	185	22
0.01905	0	15	0.41732	345	22
0.41124	44	15	0.48611	464	22
0 44049	92	15	0.44279	50	23
0.39777	139	15	0 40447	88	23
0 44701	232	15	0.47370	160	23
0.41614	202	15	0.28420	201	20
0.41014	211	15	0.28429	417	24
0.42300	406	15	0.44936	417	24
0.43239	490	16	0.37423	195	20
0.34230	10	10	0.32214	200	20
0.33702	04 100	10	0.00052	207	20
0.31968	129	10	0.29253	107	20
0.32288	173	16	0.07789	392	26
0.33085	219	16	0.67191	168	27
0.32735	266	16	0.62609	263	27
0.36916	313	16	0.33977	444	28
0.36206	400	16	0.27487	137	29
0.54078	74	17	0.50622	324	29
0.49385	120	17	0.36181	109	31
0.53845	163	17	0.34066	271	31
0.50958	206	17	0.24306	141	34
0.54554	252	17	0.05705	360	34
0.51721	392	17	0.56683	398	34
0.52120	106	18	0.48289	440	34
0.55303	287	18	0.51269	31	35
0.35549	5	19	0.50200	194	35
0.37690	311	19	0.52431	257	35
0.35392	356	19	0.46132	171	36
0.67656	155	20	0.35611	218	36
0.68353	198	20	0.49677	0	38
0.69078	242	20	0.28258	348	38
0.72901	476	20	0.02191	340	39
0.60885	113	21	0.20629	343	39
0.57397	140	21	0.19283	364	39
0.56268	186	21	0.22459	373	39
0.68678	274	21	0.19694	411	39
0.60168	106	22	0.18903	442	39
0.59042	151	22	0.18549	496	39
0.54392	193	22	0.17907	72	40
1.13173	13	23	0.24184	123	40

1.10595	373	23	0.25329	269	40
0.67888	68	24	0.21169	302	40
0.57792	229	24	0.44448	394	40
0.67507	367	24	0.55110	192	41
0.61382	410	24	0.53703	220	41
0.49010	40	25	0.47427	321	41
0.42855	158	25	0.67494	56	42
0.44786	359	25	0.17614	396	42
0.46153	461	25	0.21774	436	42
0.62701	86	26	0.20140	123	43
0.64448	167	26	0.18218	207	43
0.58827	206	26	0.24950	416	43
0.57593	377	26	0.24505	488	43
0.69512	34	27	0.26489	15	44
0.65077	46	27	0.27747	162	44
0.68278	447	27	0.31272	256	44
0.07331	0	28	0.01899	320	44
1.51488	88	28	0.15024	322	44
0.32416	20	29	0.17877	323	44
0.30008	62	29	0.20148	350	44
0.31615	104	29	0.18346	376	44
0 30219	145	20	0 16075	400	44
0.29803	184	20	0.14796	400	44
0.31743	226	20	0.18869	448	44
0.33960	313	20	0.16382	473	44
0.28497	334	20	0.15510	410	44
0.20497	225	20	0.17067	50	44
0.51489	0	29	0.17707	59 66	45
0.02470	51	20	0.17454	144	45
0.45449	04	30	0.17404	2144	45
0.47294	120	30	0.02310	217	45
0.44467	139	30	0.18876	317	45
0.47096	350	30	0.22314	350	45
0.50225	400	30	0.20739	402	45
0.47908	178	31	0.18274	426	45
0.42190	225	31	0.19552	451	45
0.43416	353	31	0.21229	478	45
0.48120	395	31	0.21745	147	46
0.01167	0	32	0.23673	226	46
0.27662	19	32	0.24086	54	47
0.25594	24	32	0.30208	307	47
0.25389	58	32	0.21951	335	47
0.26251	97	32	0.15788	407	47
0.23869	138	32	0.39526	314	48
0.24540	177	32	0.25525	168	49
0.24030	216	32	0.02590	300	49
0.24196	254	32	0.25735	308	49
0.25914	293	32	0.21532	354	49
0.26025	330	32	0.21924	379	49
0.26606	401	32	0.27479	403	49
0.27113	409	32	0.23277	430	49

0.26367	479	32	0.	23804	474	49
0.31442	60	33	0.	25021	16	50
0.30277	100	33	0.	19332	164	50
0.26305	142	33	0.	31681	236	50
0.27593	184	33	0.	22791	250	50
0.29271	228	33	0.	24382	278	50
0.27317	353	33	0.	25880	477	53
0.31133	368	33	0.	35046	142	54
0.28179	445	33	0.	36280	268	54
0.46400	41	34	0.	49998	343	55
0.40966	164	34	0.	45222	370	55
0.40208	206	34	0.	39810	136	56
0.39919	382	34	0.	39206	239	56
0.37797	91	35	0.	28963	10	57
0.34140	180	35	0.	30429	279	58
0.38110	227	35	0.	21814	454	58
0.37058	397	35	0.	31870	287	59
0.57314	442	35	0.	46618	257	60
0.38270	457	35	0.	49210	246	61
0.32850	145	36	0.	20580	112	63
0.34938	324	36	0.	27054	61	65
0.37295	407	36	0.	20491	238	65
0.43435	141	37	0.	22342	389	65
0.37740	225	37	0.	19602	429	65
0.44480	235	37	0.	21165	465	65
0.39638	266	37	0.	28584	41	66
0.38837	353	37	0.	17322	232	66
0.43045	395	37	1.	52431	105	67
0.42486	468	37	0.	20180	116	68
0.50774	136	38	0.	02084	224	68
0.47831	180	38	0.	20711	236	68
0.53393	350	38	0.	20136	281	68
0.35017	144	39	0.	17033	287	68
0.41974	473	39	0.	19622	311	68
0.52790	28	40	0.	16491	334	68
0.42719	159	40	0.	16240	360	68
0.43707	223	40	0.	18733	384	68
0.49243	357	40	0.	17981	408	68
0.44005	377	40	0.	24093	485	68
0.40062	122	41	0.	18342	35	69
0.39500	165	41	0.	19157	87	69
0.45396	491	41	0.	17329	111	69
0.64142	130	42	0.	26805	159	70
0.61132	218	42	0.	22965	444	72
0 59708	392	42	0	22001	68	74
0.04034	0	43	0	39439	441	74
0.86105	103	43	0	30904	185	75
0.86431	231	43	0	26253	469	76
0.95153	466	43	0.	32530	336	78
0.72600	100	44	0.	32448	205	83
0.12000	109	1'I'	0.	02440	200	05

0.64911	334	44	0.43407	337	85
0.67430	369	44	0.39336	57	91
0.76226	423	45	0.28538	409	91
0.71725	489	45	0.45470	68	92
0.43636	39	46	0.31725	260	93
0.40810	84	46	0.32729	304	93
0.39230	216	46	0.35831	338	94
0.43523	6	47	0.53386	211	97
0.40237	47	47	0.09533	92	101
0.35609	88	47	0.47756	111	102
0.34245	217	47	0.19203	158	105
0.56822	220	48	0.20326	233	105
0.60642	459	48	0.26699	445	105
0.71327	8	49	0.22951	1	106
0.48781	26	50	0.34941	23	107
0.44948	243	50	0.06113	68	107
0.51019	289	50	0.36595	329	107
0.57993	131	51	0.51311	122	108
0.56088	175	51	0.54751	443	108
0.55048	375	51	0.49842	459	108
0.34095	147	52	0.30393	424	109
0.58155	21	53	0.15709	56	110
0.48900	195	53	0.17733	313	115
0.41285	253	54	0.24507	20	116
0.47495	3	55	0.05347	28	117
0 46521	228	55	0.61623	26	118
0.46335	459	55	0.75247	121	118
0 57534	27	56	0.71588	337	118
0.49889	112	56	0.73326	431	118
0.48742	199	56	0.08573	20	110
0.55827	245	56	0.10736	16	120
0.52955	483	56	0.07137	8	120
0.40656	255	57	0.23632	364	122
0.44262	494	57	0.34557	87	124
0.43133	105	58	0.02442	484	120
0.40794	225	58	0.25008	3	121
0.46901	371	58	0.20570	20	120
0.52741	35	59	0.23590	40	120
0.48128	171	50	0.21946	113	120
0.54800	262	50	0.21340	120	120
0.34800	205	60	0.21466	107	120
0.34903	195	60	0.19028	197	120
0.39114	321	60	0.19020	220	120
0.20226	ə(4 70	61	0.19319	292	128
0.39230	19	10	0.19955	ə28 490	128
0.32074	220	10	0.21065	430	128
0.37103	394	01	0.20301	443	128
0.50413	160	62	0.24263	83	130
0.52324	253	62	0.22988	228	130
0.71164	161	63	0.20818	205	131
0.74488	252	63	0.76627	161	137

0.70091	344	63	0.97702	287	137
0.72304	483	63	0.85675	354	137
0.38710	144	64	0.28134	137	138
0.48427	168	64	0.41828	21	141
0.39097	188	64	0.43175	287	151
0.42855	264	64	0.34069	411	152
0.72012	35	65	0.17074	452	161
0.65307	180	65	0.23249	274	162
0.42452	166	66	0.38727	267	167
0.50484	396	66	0.76121	347	168
0.53112	488	66	0.50559	97	169
0.38459	199	67	0.43200	49	172
1.60147	113	68	0.31260	81	173
0.43247	18	69	0.65933	7	174
0.38767	63	69	0.70001	178	174
0.35732	198	69	0.94723	392	177
0.36372	243	69	0.89743	86	178
0 40437	320	69	0.77903	128	178
0.41808	142	71	0.62959	215	193
0.42003	186	71	0.45133	68	197
0.43274	222	71	0.40100	451	210
0.43274	200	71	0.62235	159	210
0.47511	166	72	0.03020	261	210
0.37974	100	72	0.43835	107	221
0.42128	211	72	0.77394	127	229
0.37398	142	73	0.20044	37	243
0.35250	138	74	0.53816	208	247
0.36778	182	74	0.21823	0	248
0.39474	190	74	0.91738	304	248
0.38998	28	75	0.40816	415	252
0.34648	70	75	0.14374	420	267
0.31659	158	75	0.68542	257	268
0.39848	22	76	0.22308	101	271
0.35983	160	76	0.29937	331	274
0.49551	188	77	0.49157	236	280
0.51334	373	77	0.80696	453	286
0.42320	217	78	0.92094	123	287
0.45113	262	78	0.63651	309	295
0.49481	494	78	0.64756	267	296
0.32509	112	80	0.13605	260	307
0.42463	307	83	0.58162	338	307
0.32398	140	84	0.51571	381	307
0.31072	375	84	0.58466	494	312
0.40504	310	85	0.60524	224	313
0.37490	27	86	0.11208	236	313
0.46709	91	89	0.11460	232	314
0.49972	313	89	0.42967	93	351
0.58404	244	90	0.37559	328	381
0.59936	291	90	0.36054	351	394
0.46941	9	93	0.52028	19	395
0.59492	307	94	1.49426	385	417

0.37625	375	95
0.67135	21	97
0.61896	297	97
0.59261	475	97
0.51526	182	98
0.67411	431	98
0.78556	491	99
0.45973	372	101
0.41934	334	103
0.48337	345	103
0.54882	334	105
0.57203	155	106
0.62428	381	106
0.44625	383	107
0.35133	213	109
0.59145	17	110
0.50062	198	110
0.56653	329	110
0.48557	401	112
0.32276	111	113
0.32140	154	113
0.29312	195	113
0.30435	239	113
0.34132	282	113
0.30886	485	113
0.38320	23	115
0.32967	242	115
0.34036	375	116
0.49060	258	117
0.53444	18	119
0.51580	367	119
0.51871	473	119
0.28671	225	122
0.32848	263	122
0.31873	305	122
0.62979	100	123
0.58197	145	123
0.38214	159	124
0.92851	42	125
0.80933	159	125
0.86762	463	125
0.56941	389	128
0.36378	22	129
0.35871	73	129
0.34308	16	130
0.30546	114	130
0.35875	157	130
0.32557	264	130
0.33626	409	130
0.51919	164	132

1.55676	410	417
0.79829	353	419
0.55059	329	436
0.83889	383	439
0.74276	464	439
0.79255	431	444
0.25111	192	448
0.22443	204	449
0.25027	412	449
0.75421	28	455
0.49807	241	458
0.38083	499	470
0.60688	230	498
0.27747	332	504
0.72681	399	509
1.02178	167	516
1.18730	406	516
0.16823	495	520
0.36149	310	528
0.20867	215	541

0.59848	411	132
0.06448	0	133
0.44157	165	134
0.45621	210	134
0.58389	429	137
0.45638	57	139
0.32454	45	140
0.29632	93	140
0.27408	138	140
0.27051	186	140
0.31286	285	140
0.41559	436	140
0.40823	279	141
0.32180	138	143
0.47672	426	144
0.59086	433	146
1.25984	124	148
1.07482	380	148
0.51297	300	149
0.36790	56	150
0.29505	220	150
0.30771	275	150
0.39680	429	150
0.52170	402	152
0.65733	389	153
0.34790	162	156
0.40852	333	156
0.40040	494	156
0.56635	144	160
0.47398	142	161
0.58477	367	161
0.91575	183	162
0.89981	468	162
0.56097	409	163
0.65713	166	164
0.65509	217	164
0.68833	139	165
0.67206	247	165
0.60214	488	166
0.42979	146	167
0.33630	193	167
0.62160	209	170
0.54717	142	171
0.56451	195	171
0.45886	89	172
0.73837	20	174
0.68592	131	174
0.76594	250	174
0.51145	276	176
0.53786	6	177

0.69946	18	178
0.63261	352	178
0.63843	26	180
0.57011	138	180
0.42717	157	181
0.60403	319	182
0.43808	56	188
0.34679	175	188
0.36917	288	188
1.59509	13	189
1.53622	244	189
0.82254	353	192
0.94203	458	192
0.47222	28	195
0.70353	342	196
0.29408	144	197
0.31003	288	197
0.34488	339	197
0.66196	430	201
0.41066	487	204
1.12288	361	205
1.19147	471	205
0.44101	8	209
0.39993	56	210
0.31361	166	210
0.52324	442	210
0.38335	158	211
0.39481	425	212
0.33327	151	213
0.43926	431	214
0.46140	484	215
0.46292	438	217
0.47117	193	218
0.61787	482	218
0.37895	300	219
0.42216	402	226
0.45160	396	228
0.41739	367	233
0.38967	120	238
0.37511	334	238
0.48585	99	245
1.16005	163	250
1.10187	276	250
0.89599	105	251
0.83370	112	251
0.89224	156	251
1.20275	490	253
0.35053	124	255
0.30658	187	255
0.34672	415	255

1.04673	175	256
1.09388	219	256
0.33017	9	257
0.27978	139	257
0.34063	168	257
0.28926	185	257
0.28596	406	257
0.30837	462	257
0.30551	141	259
0.33215	157	259
0.27783	229	259
0.29883	314	259
0.55910	159	260
0.88492	91	264
0.82527	138	264
0.97721	367	264
0.47685	375	265
0.39734	6	266
0.35251	41	269
0.29905	88	269
0.31761	199	272
0.48752	482	277
0.28814	75	279
0.30983	256	279
0.32275	300	279
0.27139	456	279
0.36551	6	283
0.30326	242	283
0.30702	193	285
0 29702	155	286
0.31864	195	289
0 50749	487	200
0.83658	62	201
0.82805	155	202
0.48113	6	202
0.301/3	97	204
0.300143	325	299
0.33627	418	200
0.38766	72	200
0.38700	0	206
0.40201	0	300
0.20545	225	309
0.48431	139	310
0.70890	249	312
0.74159	295	312
0.43521	427	314
0.34568	159	315
0.33464	92	320
0.32998	401	320
0.32825	96	322
0.27880	143	322

0.36738	432	322
0.60977	6	330
0.04544	0	332
0.58807	41	332
0.55260	279	337
0.57234	19	344
0.38583	195	351
0.29124	175	352
0.48099	437	354
0.66418	339	356
0.31264	217	357
0.28849	166	359
0.36111	121	363
0.55049	401	365
0.47807	18	366
0.81715	157	372
0.77746	261	372
0.35453	96	378
0.33791	341	378
1.15513	457	382
0.04850	0	391
0.28281	181	391
0.25289	29	393
0.23558	162	393
0.24629	206	393
0.26982	245	393
0.27246	341	393
0.07870	0	396
0.03754	0	397
0.29510	70	397
0.31601	346	397
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0.08172	0	398
0.28063	82	398
0.24867	166	398
0.26329	208	398
0.28187	252	398
0.27941	412	398
0.25265	456	398
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0.29603	138	403
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0.25806	65	408
0.25491	104	408
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0.26486	183	408
0.24719	262	408
0.24811	386	408
0.26137	412	408

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0.63550	419	410
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0.26623	255	420
0.29420	296	420
0.27142	335	420
0.25777	380	420
0.28443	419	420
0.29217	186	421
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0.81452	162	422
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0.24452	340	429
0 25094	379	429
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0.28385	151	438
0 26149	193	440
0.31931	487	440
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0.25689	140	444
0.24713	180	444
0.26234	219	444
0.25348	215	444
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0.24563	334	444
0.24505	330	444
0.30384	473	444
0.30314	415	444
0.30214	149	444
0.30603	142	445
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0.27821	102	440
0.24344	199	440
0.20123	201	440
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0.34202	430	448
0.20840	490	448
0.02263	0	451
0.29471	6	451
0.25699	77	451

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0.23634	195	451
0.23790	247	451
0.29272	60	452
0.26826	249	452
0.28314	327	452
0.30559	17	453
0.26929	196	453
0.26425	276	453
0.25956	393	453
0.34830	431	453
0.28708	498	453
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0.26523	310	461
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0 24113	377	464
0 25432	247	465
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0 24042	24	467
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0.24100	212	467
0.20402	200	467
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0.34860	300	468
0.36310	83	460
0.02510	0	409
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0.27250	20	471
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0.27473	371	478
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0.25191	454	481

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0.24552	20	482
0.23945	113	482
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0.24446	314	482
0.22888	384	482
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0.31924	416	484
0.83801	168	486
0.25721	15	487
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0.23663	196	487
0.22573	271	487
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0.22808	376	487
0.24141	410	487
0.25346	423	487
0.22497	1	488
0.27684	6	488
0.25226	42	488
0.22347	220	488
0.25985	333	488
0.36193	433	490
0.26627	217	491
0.24638	375	493
0.30048	499	493
0.28754	9	494
0.23482	158	494
0.27382	417	494
0.28078	244	497
0.27956	241	499
0.03020	0	501
0.28586	17	506
0.28984	368	510
0.03628	0	511
0.33933	334	516
0.47978	217	517
0.69326	359	527
0.52699	426	530
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1.07853	132	534
0.87097	204	535
0.87438	319	535
0.85784	373	535
0.75163	134	538
0.26710	166	560

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0.74528	101	574
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0.38699	101	584
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0.04743	0	594
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0.06083	0	597
0.79844	45	600
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0.84245	160	605
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0.75864	38	654
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0.65402	15	697
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0.80294	41	714
0.55387	217	717
0.92417	33	720
0.84848	169	720
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0.26464	375	730

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0.40966	437	733
0.29126	458	734
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0.25852	282	735
0.24880	323	735
0.32254	438	735
0.34509	426	736
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0.25023	159	745
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0.31306	83	748
0.39291	439	748
0.26964	175	749
0.24789	217	751
0.36754	435	754
0.29103	422	757
0.42204	439	759
0.23047	375	762
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0.29863	482	769
0.28760	217	771
0.26384	334	772
0.36423	428	776
0.23118	180	779
0.26879	159	788
0.37291	318	793
0.30279	279	794
0.34336	438	794
0.24489	142	796
0.41488	442	798
0.52231	430	803
0.25184	162	804
0.40676	441	804
0.42061	375	808
0.31559	159	809
0.31994	430	816
0.37553	279	823
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0.71817	318	858
0.46080	101	867
0.81983	144	871
0.85468	151	879
0.53189	431	889
1.05695	129	901
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0.51783	428	918
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0.33831	142	956
0.46843	428	966
0.83085	194	971
0.98272	473	975
0.77354	232	980
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0.87784	150	991
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0.28412	142	1016
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0 40537	318	1184
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0.94673	246	1474
0.96145	491	1474
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0.23249	63	1972
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0.22310	361	1972
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0.23784	462	1972
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0.22772	193	1973
0.32281	427	1973
0.42585	438	1983
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0.64332	193	2005
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0.44564	442	2177
0.23189	217	2184
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0.48795	433	2214
0.06861	0	2247
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0.28052	416	2257
0.44731	443	2285
0.24690	6	2294
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0.21343	11	2479
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0.33998	433	2482
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0.21429	229	2492
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0.25018	416	2579
0.40008	444	2579
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0.20864	295	2585
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0.20596	470	2585
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0.38139	437	2591
0.84544	242	2627
0.64559	101	2655
1.45237	180	2774
0.66767	195	2791
0.90369	325	2821
0.79445	334	2821
0.93292	256	2836
0.79686	375	2836
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0.61794	443	2967
1.17015	178	2978
0.80176	217	2983
0.62210	318	2986
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1.74701	43	3028
0.28443	279	3043
0.26448	416	3053
0.39339	428	3062
0.05757	0	3089
0.20731	159	3109
0.19427	217	3112
0.31597	437	3155
0.20289	142	3166

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	\mathbf{SR}			GSVT			AFIB			$^{\mathrm{SB}}$	
TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record	TF-IDF	Feature	Record
0.55669	0	0	0.00000	0	0	0.01668	0	0	0.00000	0	0
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0.69965	352	0	0.93825	300	0	0.52065	139	0	0.55256	84	0
0.61241	1	1	0.10473	332	0	0.01281	303	0	0.38928	151	0
0.33074	259	1	0.41360	410	0	0.44762	327	0	0.47092	273	0
0.59535	2	2	0.36584	421	0	0.01362	106	1	0.36300	311	0
0.44770	260	2	0.09750	164	1	0.31893	125	1	0.34822	496	0
0.54492	3	3	0.46890	255	1	0.24802	143	1	0.37853	28	1
0.40432	46	3	0.56146	374	1	0.01904	409	1	0.49428	63	1
0.41243	267	3	0.41476	207	2	0.24529	105	2	0.42125	151	1
0.57406	5	5	0.33196	424	2	0.01175	212	2	0.25230	403	1
0.61626	58	5	0.08746	160	3	2.00366	384	2	0.34789	488	1
0.50648	295	6	0.47880	240	3	0.01390	15	3	0.28758	1	2
0.49974	84	7	0.54131	325	3	0.36622	91	3	0.40820	34	2
0.42807	8	8	0.64816	359	3	0.28480	148	3	0.31261	172	2
0.51746	53	8	0.10483	495	3	0.31485	165	3	0.27519	425	2
0.48164	96	8	0.12552	6	4	0.24694	284	3	0.32471	111	3
0.56656	259	8	0.08414	26	4	0.01733	318	3	0.26816	332	3
0.36935	188	9	0.09273	38	4	0.27408	481	3	0.22727	365	3
0.38103	410	9	0.00591	324	4	0.42998	20	4	0.34242	203	4
0.14599	10	10	0.11520	331	4	0.01704	121	4	0.44713	238	4
0.30144	18	10	0.07722	359	4	0.47099	211	4	0.31501	321	4
0.31999	61	10	0.08510	371	4	0.40492	306	4	0.38107	12	5
0.31018	105	10	0.09621	380	4	0.58204	481	4	0.27636	109	5
0.32728	134	10	0.06611	206	5	0.45264	82	5	0.30550	352	5
0.33529	197	10	0.07111	441	5	0.50040	274	5	0.27585	411	8
0.32355	293	10	0.20515	497	5	0.01757	30	6	0.20005	38	9
0.30716	314	10	0.17133	15	6	0.20778	67	6	0.22803	69	9
0.29873	470	10	0.13751	50	6	0.22970	228	6	0.24787	91	9
0.27246	11	11	0.15155	65	6	0.01654	333	6	0.18942	105	9
1.20506	186	11	0.11773	156	6	0.01066	136	7	0.21263	191	9
1.23706	320	11	0.04329	152	7	0.37459	340	7	0.32367	317	9
0.60234	12	12	0.44301	237	7	0.40490	428	7	0.23209	345	9
0.46625	445	12	0.32726	298	7	0.01481	242	8	0.32003	380	9
0.63029	362	13	0.36998	318	7	0.59241	422	8	0.24668	452	9
0.27415	17	14	0.25423	381	7	0.76176	433	8	0.28757	488	9
0.29009	62	14	0.10560	484	7	0.27419	83	9	0.26455	34	10
0.28718	111	14	0.15932	499	7	0.00975	348	9	0.29630	70	14
0.31443	155	14	0.18012	66	8	0.90097	374	9	0.24493	108	14
0.29627	160	14	0.21567	135	8	0.77459	413	9	0.34767	143	14
0.29311	200	14	0.08186	316	8	0.01310	454	10	0.21488	178	14
0.30663	246	14	0.31160	358	8	0.65986	498	10	0.26625	335	14

Table A.5: Unlearned - Vanilla Saliency - Full Results

0.31867	377	14	0.26023	8	9	0.44495	223	11	0.22839	429	14
0.28439	424	14	0.06869	148	9	0.01262	60	12	0.29374	331	16
0.27909	445	14	0.49524	274	9	0.36967	230	12	0.37551	88	17
0.27658	474	14	0.10345	480	9	0.33439	313	12	0.26167	145	23
0.07019	15	15	0.20887	42	10	0.01525	363	12	0.24894	275	23
0.33306	19	15	0.28107	335	10	0.01777	166	13	0.20906	365	25
0.29956	47	15	0.22559	407	10	0.00834	469	13	0.34152	59	30
0.26952	87	15	0.33655	431	10	0.01834	272	14	0.23187	296	32
0.30301	139	15	0.24862	471	10	0.28246	364	14	0.25804	333	32
0.32795	240	15	0.07020	144	11	0.01724	378	15	0.19890	204	33
0.41228	16	16	0.23019	159	11	0.25756	68	16	0.19356	55	34
0.36448	173	16	0.40075	480	11	0.23298	131	16	0.55382	192	51
0.35577	224	16	0.33469	497	11	0.21554	143	16	0.47508	331	51
0.32474	284	16	0.29604	174	12	0.00885	181	16	0.50948	405	51
0.39750	490	16	0.26862	193	12	0.29312	275	16	0.44697	429	51
0.11854	17	17	0.06206	308	12	0.34094	287	16	0.53389	335	61
0.25010	46	17	0.08319	140	13	0.21732	344	16	0.47974	427	61
0.25527	88	17	0.24033	156	13	0.01622	287	17	0.38719	438	61
0.25263	125	17	0.20071	216	13	0.85755	46	18	0.44133	239	62
0.23875	134	17	0.16110	235	13	0.39554	190	18	0.62644	457	63
0.23092	179	17	0.17754	284	13	0.30761	248	18	0.41153	490	63
0.24532	223	17	0.21289	494	13	0.34006	335	18	0.61633	433	70
0.29005	262	17	0.18830	126	14	0.31759	413	18	0.72317	75	71
0.24305	270	17	0.14628	140	14	0.33886	97	19	0.21975	45	76
0.24086	477	17	0.17086	214	14	0.01439	302	20	0.32337	365	78
0.38401	18	18	0.09292	304	14	0.26514	350	20	0.80170	37	95
0.48159	252	18	0.11722	147	15	0.01681	105	21	0.89217	73	95
0.48733	294	18	0.15869	161	15	0.01822	408	21	0.64702	233	95
0.47611	382	18	0.10637	171	15	0.41876	104	22			
0.42835	427	18	0.13253	181	15	1.42162	218	22			
0.30425	41	19	0.09106	365	15	1.22222	467	22			
0.31332	221	19	0.13075	300	16	0.37100	177	23			
0.33118	267	19	0.11627	132	17	0.01853	317	23			
0.34904	405	19	0.37634	413	17	0.21792	390	23			
0.35421	452	19	0.11789	296	18	0.25347	25	24			
0.29110	494	19	0.27026	376	18	0.65491	340	25			
0.08241	20	20	0.36586	67	19	0.48556	389	25			
0.33719	115	20	0.07258	128	19	0.01538	332	26			
0.34415	159	20	0.17882	21	21	0.00529	135	27			
0.32768	202	20	0.19233	77	21	0.70067	139	27			
0.34785	248	20	0.01727	124	21	0.01861	438	27			
0.37416	293	20	0.19314	292	21	0.39248	261	28			
0.34060	339	20	0.04479	288	22	0.01874	44	29			
0.31132	386	20	0.04813	120	23	0.28994	64	29			
0.36002	476	20	0.28420	349	23	0.01794	150	30			
0.26088	58	21	0.08082	448	25	0.47475	346	30			
0.28560	77	21	0.30554	491	25	0.01886	256	31			
0.26703	173	21	0.20995	177	26	0.01034	271	34			
0.23670	191	21	0.07932	280	26	0.36628	111	35			
0.27383	280	21	0.24523	292	27	0.29959	420	35			
				-			-				

0.26388	370	21	0.02880	108	29	0.01407	498	39
0.29610	266	22	0.20773	385	33	0.01428	104	41
0.35973	400	22	0.03325	432	33	0.35108	479	42
0.28871	446	22	0.37196	43	34	0.01086	225	45
0.26730	447	23	0.30568	382	34	0.30936	96	47
0.12647	24	24	0.24735	214	35	0.56731	252	48
0.27288	62	24	0.06690	92	37	0.00761	43	49
0.26225	106	24	0.22582	377	37	0.00215	346	49
0.31007	151	24				0.23343	9	50
0.25749	171	24				0.26348	111	50
0.27582	276	24				1.10270	173	52
0.27889	322	24				0.51317	77	55
0.28900	372	24				0.28458	356	58
0.29273	419	24				0.94802	415	58
0.28210	436	24				0.00647	118	64
0.38970	43	25				1.10557	28	70
0.38527	85	25				0.54806	32	74
0.45133	130	25				0.01010	284	77
0.37308	219	25				0.26672	304	77
0.37697	263	25						
0.35258	307	25						
0.39435	355	25						
0.36575	377	25						
0.38976	29	26						
0.40829	153	27						
0.44134	0	28						
0.57531	39	28						
0.62312	354	29						
0.60789	30	30						
0.54914	32	32						
0.26736	247	32						
0.25523	335	32						
0.41845	33	33						
0.42121	149	33						
0.43080	416	33						
0.49556	34	34						
0.24237	198	34						
0.23264	306	34						
0.26069	327	34						
0.23731	448	34						
0.30531	469	36						
0.27007	55	38						
0.75437	91	39						
0.59113	40	40						
0.51762	41	41						
0.35172	151	41						
0.51048	42	42						
0.49397	480	42						
0.51242	3	43						
0.53001	43	43						
0.43572	446	43						
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0.52935	35	44						
0.11155	44	44						
0.46586	82	44						
0.45199	108	44						
0.46105	284	44						
0.43958	379	44						
0.45643	388	44						
0.41810	416	44						
0.19005	45	45						
0.41673	73	45						
0.40048	166	45						
0.39679	298	45						
0.42589	335	45						
0.17267	46	46						
0.34662	181	46						
0.41562	209	46						
0.39924	433	46						
0.35487	47	47						
0.33390	101	47						
0.48380	49	49						
0.45306	88	49						
0.38003	137	49						
0.34827	50	50						
0.39322	321	50						
0.44704	2	51						
0.35941	51	51						
0.28169	309	51						
0.58628	52	52						
0.60012	24	53						
0.90200	91	54						
0.88259	184	54						
0.81153	189	54						
0.84036	422	54						
0.46642	55	55						
0.40439	229	56						
0.43522	58	58						
0.29356	94	58						
0.31659	497	58						
0.31867	59	59						
0.36228	440	59						
0.40984	466	59						
0.43594	308	60						
0.54655	482	60						
0.32988	61	61						
0.42177	280	64						
0.35894	411	64						
0.42835	50	65						
	53	05						
0.24848	53 65	65						

67

164

0.59736

0 50000	0.01	00
0.50288	321	68
0.53383	123	72
0.44513	74	74
0.34101	73	75
0.53977	390	75
0.45945	99	76
0.69302	365	77
0.35571	229	78
0.67446	82	79
0.71368	363	79
0.68044	39	80
0.81940	71	80
0.64720	272	80
0.68662	59	81
0.60970	350	81
0.23105	101	85
0.22851	138	85
0.22374	153	85
0.20617	173	85
0.22150	211	85
0.24925	248	85
0.21934	283	85
0.23371	318	85
0.21332	351	85
0.23943	456	85
0.24579	492	85
0.24506	113	86
0.25395	145	86
0.22831	178	86
0.27246	213	86
0.21691	248	86
0.22234	283	86
0.23979	310	86
0.24788	319	86
0.23044	353	86
0.23493	386	86
0.25723	488	86
0.25084	79	87
0.27034	146	87
0.23471	222	87
0.25801	251	87
0.24766	285	87
0.29483	429	88
0.22910	460	88
0.28143	58	89
0.25091	162	90
0.25983	392	90
0.28546	432	90
0.23939	45	91

0.31177	227	91
0.27752	454	91
0.30086	170	92
0.26476	290	92
0.29668	22	94
0.25304	399	94
0.24885	18	95
0.32071	426	97
0.31518	28	104
0.24685	107	109
0.24491	301	109
0.22427	118	115
0.22048	187	115
0.32671	221	116
0.23279	207	119
0.32316	211	128
0.26515	290	128
0.31043	468	137
0.27180	319	149
0.35789	99	178
0.26437	279	201
0.21520	394	202
0.06534	205	205
0.25713	161	207
0.34448	37	209
0.33855	52	212
0.47087	406	212
0.33962	53	210
0.28639	219	221
0.36918	80	222
0.34419	11	223
0.28413	416	220
0.23413	339	224
0.36566	68	221
0.26307	420	220
0.20307	420	220
0.31644	145	230
0.32188	354	237
0.32100	200	231
0.33103	403	230
0.21294	152	240
0.07581	255	255
0.07561	409	200
0.38303	492	207
0.21113	241 144	201
1 59716	144	323
1 47450	9440	220
1.47409	∠40 460	220
0.92327	409	338
0.98747	271	339
0.57025	242	340

0.52270	260	341
0.55934	161	342
0.50757	277	343
0.94678	246	345
0.21134	345	345
0.83279	492	345
0.86473	126	346
0.45082	346	346
0.45502	077	250
0.55249	465	252
0.58055	405	252
0.06119	201	201
0.06112	381	381
0.38443	333	412
0.38666	50	415
0.35093	304	416
0.22626	237	470
0.52815	475	473
0.54598	133	474
0.38642	406	475
0.60341	423	476
0.70653	486	477
0.77358	133	478
0.79505	168	478
0.50255	480	480
0.63781	96	483
0.65405	430	486
0.58594	248	487
1.54121	337	488
0.64572	87	489
0.56536	296	489
0.34956	424	493
0.72889	411	497
0.84819	204	499
0.81839	306	499
0.56620	0	501
0.42484	428	505
0.49338	462	505
0.56898	141	506
0.51362	328	506
0.43198	327	507
0.44357	486	507
0.48132	68	512
0.49892	116	512
0.40868	467	513
0.43541	497	524
0.37697	394	529
0 47352	278	534
0 38317	445	537
0.37401	415	537
0.57401	410	544
0.03807	403	563

0.34378	485	587
0.41203	478	590
0.53486	49	596
0.23802	98	599
0.30160	102	603
0.09979	105	606
0.47017	111	612
1.16288	159	623
1.11483	184	623
0.45420	123	624
0.48973	323	627
0.33780	127	628
0.48563	351	631
0.72113	121	633
0.82548	377	634
0.89208	121	635
0.42142	0	636
0.67221	241	636
0.78400	175	637
0.49835	99	639
1.17627	300	640
1.12611	59	641
1.15010	96	641
0.55601	64	642
0.55154	141	644
0.47401	339	648
0.71655	477	649
0.54720	23	653
0.57420	65	660
0.91238	177	660
0.58229	238	661
0.25407	161	662
0.30562	405	683
0.30191	163	710
0.46042	351	716
0.30887	88	718
0.33833	103	733
0.33070	204	751
0.40446	79	752
0.18388	262	763
0.28922	266	767
0.30820	268	769
0.22388	281	782
0.33479	203	783
0.13553	283	784
0.19665	286	787
0.15821	288	789
0.54036	306	807
0.62203	307	808
0.58066	316	817

0.01000	010	000
0.61933	319	820
0.21164	343	824
0.20748	366	824
0.24299	384	824
0.20952	402	824
0.22648	124	825
0.20362	170	825
0.24700	297	825
0.21615	319	825
0.22608	356	829
0.21726	421	829
0.20963	25	830
0.25294	59	830
0.21526	130	830
0.24252	228	830
0.22393	294	841
0.23650	473	843
0.26569	171	844
0.29374	347	848
0.28708	75	854
0.05742	353	854
0.21867	280	858
0.28181	186	859
0.27695	284	861
0.26828	86	863
0.30000	211	884
0.16276	384	885
0.34370	395	896
0.40240	398	899
0.49826	402	903
0.22107	422	905
0.23577	482	905
0.20551	166	906
0.25133	226	906
0.22940	289	906
0.36526	405	906
0.40799	407	908
0.52094	427	928
0.35799	98	964
0.73699	319	1047
0.45136	475	1055
0.61616	66	1068
0.28629	77	1079
0.21145	61	1080
0 76372	3	1088
0.68215	150	1096
0.59091	120	1107
0 74547	302	1114
1 10030	300	1115
1 09251	420	1115
1.00001		1110

1.07366	12	1119
0.66286	426	1119
0.93472	270	1173
0.53793	174	1176
1.51324	79	1191
0.42267	213	1215
0.50582	218	1220
0.54750	53	1234
0.36557	189	1237

Appendix B

Long Tables

Model: "model"

Layer (type)	Output Shape	Param #
<pre>input_1 (InputLayer)</pre>	[(None, 500, 500, 3)]	0
block1_conv1 (Conv2D)	(None, 500, 500, 64)	1792
block1_conv2 (Conv2D)	(None, 500, 500, 64)	36928
block1_pool (MaxPooling2D)	(None, 250, 250, 64)	0
block2_conv1 (Conv2D)	(None, 250, 250, 128)	73856
block2_conv2 (Conv2D)	(None, 250, 250, 128)	147584

block2_pool (MaxPooling2D)	(None, 125, 125, 128)	0
block3_conv1 (Conv2D)	(None, 125, 125, 256)	295168
block3_conv2 (Conv2D)	(None, 125, 125, 256)	590080
block3_conv3 (Conv2D)	(None, 125, 125, 256)	590080
block3_pool (MaxPooling2D)	(None, 62, 62, 256)	0
block4_conv1 (Conv2D)	(None, 62, 62, 512)	1180160
block4_conv2 (Conv2D)	(None, 62, 62, 512)	2359808
block4_conv3 (Conv2D)	(None, 62, 62, 512)	2359808
block4_pool (MaxPooling2D)	(None, 31, 31, 512)	0
block5_conv1 (Conv2D)	(None, 31, 31, 512)	2359808
block5_conv2 (Conv2D)	(None, 31, 31, 512)	2359808
block5_conv3 (Conv2D)	(None, 31, 31, 512)	2359808

block5_pool (MaxPooling2D)	(None, 15, 15, 512)	0			
flatten (Flatten)	(None, 115200)	0			
dense (Dense)	(None, 1024)	117965824			
dense_1 (Dense)	(None, 512)	524800			
dense_2 (Dense)	(None, 4)	2052			
Total params: 133,207,364 Trainable params: 118,492,676 Non-trainable params: 14,714,688					