HEAT TRANSFER IN ANNULAR PASSAG

TURBULENT FORCED CONVECTION HEAT TRANSFER

IN

ANNULAR PASSAGES

By

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SCOPE AND CONTENTS:

An experimental study of turbulent forced convection heat transfer to water flowing in a vertical annular passage is reported in this paper. The study investigates the influence of eccentricity (ranging from 0% to 80%) and diameter ratio (ranging from 1.5 to 4.0) upon the heat transfer phenomena occurring at the inner boundary of the annular passage.

Dimensionless heat transfer parameters calculated from measurements made at the two locations corresponding to the maximum and minimum separation of the inner and outer boundaries of the annular passage are correlated in terms of the Reynolds number, the eccentricity and the diameter ratio. Analysis of the correlations indicates that eccentricity affects the heat transfer phenomena occurring at the two locations on the inner boundary of the annular passage in different fashions; increasing eccentricity causes the heat transfer to increase at the location corresponding to the maximum separation of the boundaries and causes the heat transfer to decrease at the location corresponding to the minimum separation of the boundaries. The magnitude of the increase or decrease in heat transfer is dependent upon the diameter ratio; at a particular level of eccentricity, the greater variations in heat transfer occur at the smaller diameter ratios. Ranges in which eccentricity does not influence heat transfer are found in connection with the larger diameter ratios.

Moody friction factors calculated from measurements made with concentric annular passages are correlated as a function of Reynolds number.

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TABLE OF CONTENTS

TEXT

- 1. Introduction
- 2. Literature Survey
- 3. Test Facility
 - 3.1 Test Rig
 - 3.2 Test Section
 - 3.3 Test Instrumentation
- 4. Experimental Procedure
- 5. Data Analysis
 - 5.1 Data Computation
 - 5.2 Data Correlation

6. Discussion

- 6.1 Accuracy of the Results
- 6.2 Heat Transfer in Concentric Annular Passages
- 6.3 Heat Transfer in Eccentric Annular Passages
- 6.4 Fluid Dynamics in Concentric Annular Passages
- 7. Conclusions
- 8. Nomenclature
- 9. References
- 10. Illustrations

APPENDIX

1. Test Results

(v)

- 1.1 Measured Values
- 1.2 Derived Results
- 1.3 Dimensionless Parameters
- 2. Theoretical Derivations

2.1 Temperature Drop in the Wall of a Stainless Steel Tube

- 2.2 Support Leg Lengths
- 3. Heat Transfer in an Eccentrically Arranged Single-Pass Shell and Tube Heat Exchanger

LIST OF FIGURES

- Figure 1 Test Facility
- Figure 2 Schematic Arrangement of Test Facility Components
- Figure 3 Test Section Assembly
- Figure 4 Location of Test Section Thermocouples
- Figure 5 Correlation of Experimental (Heat Transfer) Results: Eccentricity -0%
- Figure 6 Correlation of Experimental (Heat Transfer) Results: Eccentricity -0%
- Figure 7 Correlation of Experimental (Heat Transfer) Results and Effect of Eccentricity on Heat Transfer: Diameter Ratio -1.5
- Figure 8 Correlation of Experimental (Heat Transfer) Results and Effect of Eccentricity on Heat Transfer: Diameter Ratio -2.0
- Figure 9 Correlation of Experimental (Heat Transfer) Results and Effect of Eccentricity on Heat Transfer: Diameter Ratio -2.5
- Figure 10 Correlation of Experimental (Heat Transfer) Results and Effect of Eccentricity on Heat Transfer: Diameter Ratio -3.0

Figure 11 - Effect of Eccentricity on Heat Transfer

Figure 12 - Correlation of Experimental (Fluid Dynamics) Results: Eccentricity -0%



1. INTRODUCTION

Although convective heat transfer in annular passages has many applications in the design of industrial heat transfer equipment, the information available in the literature concerning heat transfer in such systems is relatively incomplete. There is little available information concerning the effect of eccentricity upon forced convection heat transfer, and the information which is available is not adequate to quantitatively assess the influence of diameter ratio upon forced convection heat transfer in annular passages. Those investigators who have studied forced convection heat transfer in eccentric annular passages have generally covered the complete range of eccentricities but have not explored the range of diameter ratios in sufficient detail.

The present paper describes an experimental study investigating the influence of eccentricity (ranging from 0% to 80%) and diameter ratio (ranging from 1.5 to 4.0) upon forced convection heat transfer to water at the inner boundary of a vertical annular passage. The experimental study was comprised of tests upon nineteen annular test configurations involving various combinations of five levels of eccentricity and six levels of diameter ratio. Heat transfer results were evaluated at the two locations corresponding to the maximum and minimum separation of the inner and outer boundaries of the annular passage.

Correlations are presented enabling the local heat transfer coefficients existing at the two locations on the inner boundary of the annular passage to be evaluated numerically. The results of other investigations have shown that average heat transfer coefficients in eccentric annular passages do not vary appreciably from average heat transfer coefficients in concentric annular passages and for this reason, average heat transfer coefficients are not presented. The singular function of the information presented is the prediction of local heat transfer coefficients on the inner boundary of annular passages. Heat transfer at the location corresponding to the minimum separation of the boundaries is of particular interest because this is the location where excessively high surface temperatures are liable to occur.

In addition, the present paper describes an experimental study investigating the influence of eccentricity (ranging from 0% to 80%) and diameter ratio (ranging from 1.5 to 2.5) upon pressure drop for turbulent flow in a vertical annular passage. A correlation is presented enabling the pressure drop in concentric annular passages to be evaluated numerically for the particular value of relative roughness involved.

2. LITERATURE SURVEY

The influence of diameter ratio upon the transfer of heat from the inner boundary of a concentric annular passage was first investigated by Foust and Christian (1). From the results of their experiments involving the transfer of heat to water flowing in ten different annular passages with diameter ratios varying from 1.20 to 2.36, Foust and Christian were able to prove the dependence of the heat transfer process upon diameter ratio. Subsequently, Monrad and Pelton (2) investigated the transfer of heat to water flowing in three annular passages with diameter ratios 1.65, 2.45 and 17 and derived the following correlation

 $Nu_B = 0.020 (Re_B)^{0.8} (Pr_B)^{1/3} (D_0/D_1)^{0.53}$

relating the heat transfer coefficients at the inner boundary of the annular passage to the flow conditions and fluid properties existing in the passage. For water flowing through a vertical annular passage with diameter ratio 1.33, Carpenter, Colburn, Schoenburn and Wurster (3) were able to derive an equivalent correlation involving the viscosity ratio (μ/μ_5) . Stein and Begell (4) thoroughly investigated the transfer of heat to water flowing in three annular passages with diameter ratios 1.25, 1.50 and 1.75 and derived the correlation

$$\operatorname{St}_{\mathbf{F}}(\operatorname{Pr}_{\mathbf{F}})^{2/3}(\operatorname{Re}_{\mathbf{F}})^{0.2}(\operatorname{D}_{\mathbf{0}}/\operatorname{D}_{\mathbf{1}})^{0.5} = 0.0200$$

which is essentially the correlation derived by Monrad and Pelton. Deissler and Taylor (5) have extended a previous theoretical analysis for turbulent velocity and temperature distributions in tubes to predict turbulent velocity and temperature distributions in an annular passage. Using the theoretical relationship derived, Deissler and Taylor have predicted the average heat transfer coefficient and the circumferential variation of the local heat transfer coefficient for air flowing through an annular passage with diameter ratio 3.5 and various eccentricities within the range 0% to 100%. The theoretical results presented by Deissler and Taylor indicate extreme variations in heat transfer coefficient around the inner boundary of the annular passage which are inconsistent with the variations measured by other investigators.

Heyda (6) has developed an analytical procedure based upon a continuous velocity distribution for turbulent flow near a smooth wall derived by Van Driest to determine the temperature field in an eccentric annular passage. Since Heyda has not applied the analytical procedure to solve a practical example, the validity of the theory is unknown.

Diskind (7) has reported the results of an experimental study performed at Columbia University in which the influence of eccentricity upon turbulent forced convection heat transfer and pressure drop in an annular passage with diameter ratio 1.5 was investigated. Water passed vertically upward through an annular passage in which the relative location of the inner and outer boundaries could be changed. The inner boundary of the annular passage was electrically heated. Heat transfer coefficients and friction factors were calculated from measurements of the resulting temperature and pressure distributions.

Diskind has presented average heat transfer coefficients with sufficient additional information to evaluate the circumferential variation in local heat transfer coefficients.

Faure (8) has reported the results of a similar study performed in France in which the influence of eccentricity upon turbulent forced convection heat transfer and pressure drop in three annular passages with diameter ratios 2.3, 3.3 and 5.4 was investigated. Air flowing vertically through an annular passage was heated by an electrically heated tube forming the inner boundary of the annular passage. The relative location of the inner and outer boundaries could be changed, enabling the eccentricity of the annular passage to be varied. Heat transfer coefficients and friction factors were calculated from measurements of the resulting temperature and pressure distributions. Faure has presented average heat transfer coefficients and the circumferential variation in local heat transfer coefficients for surface temperatures ranging from 80°C to 800°C. In support of these heat transfer results, Faure has presented velocity and temperature profiles measured within the annular passage for both concentric and eccentric arrangements of the boundaries of the annular passage.*

The experimental results presented by Diskind and Faure'are in general agreement; the dependence of heat transfer coefficient upon eccentricity in each case is similar, although a direct comparison cannot be made because of differences in diameter ratios. However,

^{*}Reference (9), an English translation of reference (8) can be obtained from the Department of Mechanical Engineering, McMaster University.

the theoretical results presented by Deissler and Taylor are not in agreement with the experimental results presented by either Diskind or Faure'in that the variation in theoretically calculated local heat transfer coefficients is several times greater than the variation in experimentally measured local heat transfer coefficients. The assumptions which Deissler and Taylor have employed in developing their theoretical relationship are therefore suspect.

3. TEST FACILITY

A photograph of the test facility used in performing the experimental study is shown in Figure 1. The components comprising the test facility were arranged to form a closed system, such that the fluid upon which the heat transfer experiments were performed (water) circulated continuously through a pump section, a heater section, a flow meter section, a test section and a cooler section. The arrangement of the various components is shown schematically in Figure 2.

For purposes of description, the test facility may be considered to be comprised of two assemblies, the test rig and the test section. The function of the test rig was to provide the test section with water at a regulated flowrate and temperature; the function of the test section was to establish velocity and temperature distributions in the water for various annular test configurations and to evaluate the corresponding surface heat transfer coefficients.

3.1 Test Rig

A Worthington model 6GAU gear pump operating at 1750 revolutions/minute discharged water at a constant rate of 55 U.S. gallons/minute for any pressure up to 50 pounds/square inch which was the pressure at which the automatic relief valve within the pump opened. The portion of the flowrate in excess of that required for a particular test was recirculated through the pump by means of an

external pump bypass, enabling the rate of flow through the system to be controlled by the setting of a manually operated valve. This method of control proved to be quite adequate, as the flowrate responded quickly to changes in valve setting and fluctuations in flowrate were negligible.

Heat was added to the water in the system as it circulated through the heater section. The heat source was a Chromalox model TM612 flanged pipe heater comprised of six calrod elements, each having a rated 2000 watt heat output at 230 volts. The temperature of the water could be regulated by the manually operated heater controls which were so connected that the total heat output could be varied continuously from 0 watts to 12,000 watts. The operation of the heater section was typical of this type of heat transfer equipment in that relatively long periods of time were required to effect a change in temperature after a change in the control setting. However it proved possible to predict system heat requirements for particular test conditions, enabling the heater section to be operated satisfactorily.

The water flowrate was measured in a calibrated flow meter section employing an orifice plate designed in accordance with the British Standard Code for Flow Measurements (B.S. 1042:1943). The flow meter section, comprised of a length of straight pipe upstream of the orifice plate, the orifice plate and a length of straight pipe downstream of the orifice plate was calibrated twice during the experimental study. The range of flowrates which the flow meter section was required to measure induced differential pressures across

the orifice plate varying in magnitude by a factor of twenty. The inaccuracies associated with the measurement of the smaller differential pressures reduced the precision with which the smaller flowrates could be measured.

Heat was removed from the water as it circulated through the cooler section. The heat sink was a Heliflow model 9XF-16S heat exchanger in which heat was exchanged with mains water. The temperature of the water could be regulated by controlling the flow of mains water with two valves which were installed in parallel upstream of the cooler section for this purpose; the larger valve provided coarse control and the smaller valve provided fine control. This method of control proved to be quite satisfactory in that the rate of heat exchange could be precisely set and maintained. An orifice plate was installed upstream of the control valves, enabling the mains water flowrate to be measured so that particular test conditions could be re-established.

A 5 U. S. gallon capacity head tank was connected in the system upstream of the pump section to accommodate expansion of the water. The head tank was mounted higher than any other point in the system in order to keep the system flooded during operation and was vented at the top in order to establish atmospheric pressure in the system upstream of the pump section.

3.2 Test Section

The manner in which the components comprising the test section were assembled is illustrated in Figure 3. An annular passage through which the water circulated was formed between the inner tube assembly

and the outer tube assembly. The 0.50" O.D. inner tube assembly, which was common to all the configurations investigated formed the inner boundary of the annular passage; one of six outer tube assemblies having diameters ranging from 0.75" I.D. to 2.00" I.D. formed the outer boundary of the annular passage.

Inspection of Figure 3 will reveal that the inner tube assembly was mounted eccentrically in the housings and that the outer tube assembly was mounted eccentrically in the hubs. This offset, which was identical in each case, enabled the eccentricity of the annular passage to be varied. The hubs supporting the outer tube assembly could be rotated with respect to the housings, carrying the axis of the outer tube assembly around the circumference of a circle. As the outer surfaces of the hubs were concentrically mounted with respect to the true axes of the housings, the axis of the inner tube assembly intersected the circle representing the locus of the axis of the outer tube assembly. Consequently, any separation of the axes of the inner tube assembly and outer tube assembly could be achieved simply by rotating the hubs. When the hubs were so aligned that the axis of the outer tube assembly coincided with the axis of the inner tube assembly, concentricity was obtained.

The effective length of the inner tube assembly consisted of a stainless steel tube 0.50" O.D. x O.OlO" W.T. x 24" long which was heated by a heavy electric current. Tests performed upon similar pieces of tubing had indicated that the variations in wall thickness and resistivity of the stainless steel tube were small and consequently, the heat generation per unit surface area could be considered uniform.

Copper tubes 0.50" O.D. x 0.375" I.D. were silver brazed to the stainless steel tube in order to extend its length and to create an unheated length in which fully developed turbulent flow could be established. The copper tubes conducted the electric current to and from the effective length. The relative resistivities and cross sections of the tubes were such that heat generation in the copper tubes did not exceed 0.5% of the heat generation in the stainless steel tube.

The outer tube assemblies were fabricated from stock plastic tubes. Six sets of hubs, one for each outer tube assembly were machined from sheet plastic. The outer tube assemblies were mounted in the hubs on rubber "O" rings which enabled the outer tube assemblies to be rotated about their respective axes. Each outer tube assembly was fitted with two sets of diametrically opposed pressure taps which spanned the effective length and three dial indicator mountings located in line with the pressure taps.

In order to maintain the eccentricity uniform over the length of the test section, support legs were mounted on the inner tube assembly upstream and downstream of the effective length. The support legs consisted of lengths of 1/8" diameter plastic rod threaded into specially machined supporting rings which were soft soldered to the inner tube assembly. The plastic legs were machined to length in accordance with the particular outer tube assembly and separation being investigated in order to locate the inner tube assembly precisely with respect to the outer tube assembly^{*}.

•The theory derived for calculating support leg length is presented in Appendix 2.

In order to confirm the eccentricity of a particular configuration, measurements of the actual separation of the boundaries of the annular passage were made. A dial indicator with a 2" travel was mounted in turn in each of the three dial indicator mountings, clamped in place and rotated with the outer tube assembly about its axis. The stem of the dial indicator rode on the inner tube assembly and indicated a deflection equivalent to twice the separation of the axes of the inner tube assembly and outer tube assembly for one complete revolution. These measurements enabled the actual eccentricities to be calculated at three positions in the effective length.

The power supply for the test section was a Miller model SR 1000 Bl direct current welding transformer. The heat generation in the test section could be regulated by the control provided with the machine enabling stepless continuous variation in heat generation from 1 kilowatt to the specified value. The capacity of the welding transformer and the voltage-current characteristics of the stainless steel tube were such that a maximum heat generation of approximately 45 kilowatts (900 amperes at 50 volts) could have been obtained. However, the cables used limited the current, and as a consequence the heat generation in the experimental study did not exceed 14 kilowatts (520 amperes at 28 volts). The use of this welding transformer as a power source proved quite satisfactory in that any specified heat flux could be achieved simply by setting the control on the welding transformer.

3.3 Test Instrumentation

This section discusses at length the various instruments used in measuring the test conditions pertinent to the investigation of turbulent forced convection heat transfer in an annular passage.

The various temperatures in the test section were measured with eighteen thermocouples, three of which were stream thermocouples immersed in the water upstream of the effective length, twelve of which were surface thermocouples spotwelded to the inner surface of the stainless steel tube comprising the effective length and three of which were stream thermocouples immersed in the water downstream of the effective length. The twelve thermocouples spot welded to the inner surface of the stainless steel tube were positioned along the length of the tube in two diametrically opposite groups at four inch intervals spaced alternately. The location of the thermocouples in the test section is shown schematically in Figure 4.

The thermoelectric potentials of these eighteen thermocouples were recorded on a Philips model PR 3210 A/00 twelve point self balancing millivolt recorder. The thermoelectric potentials of the six stream thermocouples were recorded continuously; a switching circuit was arranged enabling the thermoelectric potentials of either group of surface thermocouples to be recorded depending upon the arbitrary setting of a switch. The thermoelectric potentials of all eighteen thermocouples were referenced to ice temperature.

The six stream thermocouples were formed from Thermoelectric "Ceramo" miniature sheathed thermocouple wire with inert oxide insulation. The type "J" iron-constantan pair contained by the sheath was welded together and grounded to the sheath at the hot junction. The twelve surface thermocouples were formed from Thermoelectric "Fibreglass-Fibreglass" thermocouple wire treated with high temperature varnish. The type "J" iron-constantan pair in the thermocouple wire was spotwelded together and then spotwelded in position using a specially developed fixture. The leads from the twelve surface thermocouples and the leads from the three stream thermocouples downstream of the effective length were brought out through the copper tube and terminated in a junction box at the downstream end of the test section; the leads from the three stream thermocouples upstream of the effective length were brought out through the copper tube and terminated in a junction box at the upstream end of the test section. The rated accuracy of the thermocouples used was $\pm 3/4$ of the temperature measurement, giving a possible $1.5^{\circ}F$ error in the difference of the measurements of the surface thermocouples and the stream thermocouples.

The bulk temperature of the water entering and leaving the test section was measured with two precision mercury-in-glass thermometers which could be read to $0.1^{\circ}F$. The thermometers, which were used in determining the rise in bulk temperature of the water circulating through the test section, were installed in thermometer wells located upstream and downstream of the test section. The precision with which the thermometers could be read produced a possible $0.2^{\circ}F$ error in the calculation of the bulk temperature rise.

The heat generated in the test section was calculated from measurements of the potential drop over the test section and the current flowing through the test section. A Metra model DLi No. 62262

variable range voltmeter with a rated accuracy of $\pm 1\%$ of the full scale value measured the potential drop over the test section; a Simpson model 29SC-No. 10028 ammeter-shunt combination with a rated accuracy of $\pm 1\%$ of the full scale value measured the current flowing through the test section. Using the measurements of these instruments, the maximum possible error in the calculation of the heat generated in the test section was approximately $\pm 5\%$.

The differential pressures induced by the flow through the orifice in the flow meter section and by the flow through the orifice in the mains water line were measured with 16" differential mercury manometers. The scales with which the manometers were fitted enabled differential pressures to be measured to \pm 0.05 inches of mercury. The maximum possible error in the corresponding flowrate measurement was approximately \pm 5%.

The pressure drop over the effective length of the test section was measured with two 36" differential mercury manometers. The differences in mercury columns could be measured to \pm 0.05 inches, giving a maximum possible error in the measurement of pressure drop of approximately \pm 10%.

The system pressure at the pump discharge was measured with a U. S. Gauge Company bourdon tube pressure gauge which was calibrated with a dead weight tester before being put into service. On the basis of this calibration, the maximum possible error associated with the use of this gauge to measure system pressure was assumed to be $\pm 10\%$.

The ambient temperature in the vicinity of the test facility was measured with a precision mercury in glass thermometer.

4. EXPERIMENTAL PROCEDURE

No special attempt was made to maintain the purity of the water circulating in the system. Prior to each test, the system was refilled with water from the mains. During filling, air trapped in the system was bled off at the test section and the heater section where bleed points for this purpose had been provided.

After the system had been filled, the water was circulated and a drain was opened permitting mains water to purge the system. It was found that air bubbles entrained in the water could be removed by operating in this fashion; much of the air dissolved in the water could be removed by operating with the heater section energized. Experimental measurements were accepted only after visual observation of the water circulating through the test section revealed it to be free of entrained air bubbles.

In establishing the conditions for a test, the water flowrate corresponding to the velocity which when multiplied by the equivalent diameter and divided by the kinematic viscosity would give the specified Reynolds number was set first. Mains water was started flowing in the cooler section and the heater section was energized; the respective controls were set so that the temperature of the water in the system rose at the approximate rate of 1°F per minute. The test section power supply was energized and the power generation in the test section was raised incrementally until the specified film temperature difference

indicated by the chart recorder was attained. Final adjustments bringing the temperature of the water in the system to equilibrium at the specified value were made by resetting the heater section controls.

When the temperature of the water in the system had attained equilibrium at the value specified for the particular test, five to ten minutes were allowed to elapse in which it was ensured that steady state heat transfer conditions existed in the test section. Then the following measurements were made with the appropriate instruments and recorded:

- (1) Temperature of the water upstream of the test section.
- (2) Temperature of the water downstream of the test section.
- (3) Surface temperatures on the stainless steel tube comprising the effective length.
- (4) Stream temperatures upstream and downstream of the effective length.
- (5) Flowrate of the water circulating through the system.
- (6) Potential drop over the test section length.
- (7) Current flowing through the test section.
- (8) Pressure differences over the effective length.
- (9) System pressure at the pump discharge.

(10) Ambient temperature in the vicinity of the test facility. The water flowrate was then reset and additional tests were performed in order to demonstrate the effect of flowrate on forced convection heat transfer.

5. DATA ANALYSIS

The results derived from the experimental study are tabulated in Appendix 1. The manner in which the results were analyzed is outlined in the following sections. The symbols used are defined in Section 8.

5.1 Data Computation

As mentioned previously, local heat transfer coefficients were calculated at the two locations on the inner boundary of the annular passage corresponding to the maximum and minimum separation of the boundaries. The relationship

$$h_{c} = \frac{(Q/A)}{(T_{s} - T_{B})} \quad B.T.U./hr.ft^{2} \ ^{o}F$$

was used to evaluate the local heat transfer coefficients. The heat flux (Q/A) and the mean film temperature difference $(T_S - T_B)$ were evaluated from measurements of the conditions existing in the region between 12" and 20" from the upstream end of the effective length wherein the heat transfer phenomenon was considered to be representative of fully developed turbulent forced convection heat transfer.

The heat flux (Q/A) was computed from electrical measurements of the heat generation in the test section and/or calorimetric measurements of the heat convection in the water circulating through the test section. The heat flux calculated from electrical measurements was computed by the relationship:

$$\frac{Q}{A} = 3.413 \left(\frac{B.T.U.}{watt-hr.}\right) \quad E \text{ (volts) I (amperes)} \left(\frac{1}{A_S}\right) \left(\frac{1}{ft^2}\right)$$
$$= 3.413 \frac{E I}{A_S} B.T.U./hr.ft^2.$$

The heat flux calculated from calorimetric measurements was computed by the relationship

$$\frac{Q}{A} = W (lb./hr.) C (B.T.U./lb.°F) (T_o - T_i) (°F) (\frac{1}{A_S}) (\frac{1}{ft^2})$$
$$= \frac{W C}{A_S} (T_o - T_i) B.T.U./hr.ft^2.*$$

The two independent computations of heat flux served to test the validity of the measurements as the experimental results were discarded if the computed values did not agree within approximately + 10%.

The mean film temperature difference $(T_S - T_B)$ was obtained by plotting the temperatures measured in the test section as a function of displacement from the upstream end of the effective length. Temperature profiles for the inner surface of the stainless steel tube were formed by drawing smooth curves through the points representing the surface temperature measurements at the locations corresponding to the maximum and minimum separation of the boundaries. The corresponding temperature profiles for the outer surface of the stainless steel tube were formed by drawing smooth curves through points obtained by

[•]The fluid property values used in all the calculations performed were obtained from graphs plotted from the values presented in "Thermodynamic Properties of Steam", by Keenan and Keyes, John Wiley and Sons Incorporated, 1936.

subtracting the temperature drop in the wall from the temperature profiles for the inner surface of the stainless steel tube^{*}. The temperature profile representing the uniform rise of water bulk temperature was formed by joining the points representing the bulk temperatures measured upstream and downstream of the test section by a straight line. Local film temperature differences in the region of fully developed turbulent forced convection heat transfer were evaluated by subtracting the local water bulk temperature from the local outer surface temperature; the mean film temperature difference characterizing the turbulent forced convection heat transfer at the particular location on the inner boundary of the annular passage was obtained by averaging the local film temperature differences.

Moody friction factors were calculated from the average of the measurements of pressure drop over the effective length. The relationship

$$f = (D_{e}/L) (2g/V^{2}) (\frac{ft}{\sec^{2}} \times \frac{\sec^{2}}{ft^{2}}) (P_{i} - P_{o}) (ft water)$$
$$= (D_{o} - D_{i})/L (2g/V^{2}) (P_{i} - P_{o}) (-)$$

was used to compute the friction factor.

In order to clarify the procedures used in computing the local heat transfer coefficients and friction factors, sample calculations are presented on the following two pages.

•The theory derived for calculating the temperature drop in the wall of the stainless steel tube is presented in Appendix 2.

THE FOLLOWING INFORMATION IS PERTINENT TO THE TEST DIAMETER RATIO -2.0 INNER DIAMETER-0.500" EFFECTIVE ECCENTRICITY - 2.9% OUTER DIAMETER-1.000" LENGTH-24" THICKNESS OF WALL OF STAINLESS STEEL TUBE -0.010" FLOWRATE - 12.0 U.S. GALLONS/MINUTE POTENTIAL DROP OVER TEST SECTION - 13.4 VOLTS CURRENT FLOWING THROUGH TEST SECTION - 265 AMPERES PRESSURE DIFFERENCE OVER EFFECTIVE LENGTH -0.78" MERCURY



NOTE: AT THE UPSTREAM END OF THE EFFECTIVE LENGTH WHERE HEATING COMMENCES, THE BULK TEMPERATURE & STREAM TEMPERATURES AGREE: AT THE DOWNSTREAM END OF THE EFFECTIVE LENGTH WHERE HEATING CEASES, THE BULK TEMPERATURE & STREAM TEMPERATURES DISAGREE. THE PROBABLE EXPLANATION IS THAT THE WATER IS NOT ADEQUATELY MIXED AT THE LOCATION WHERE THE STREAM TEMPERATURES ARE MEASURED AT THE DOWNSTREAM END OF THE EFFECTIVE LENGTH.

SURFACE AREA NORMAL TO THE FLOW OF HEAT A = $\pi \left(\frac{0.5}{12}\right)$ FT. $\left(\frac{24}{12}\right)$ FT. = 0.265 FT.²

HEAT FLUX CALCULATED FROM ELECTRICAL MEASUREMENTS

Q = 3.413 B.T.U. WATT-HR. X 13.4 VOLTS X 265 AMPERES (1 0.265) T.2 = 45,600 B.T.U. HR.-FT.2 HEAT FLUX CALCULATED FROM CALORIMETRIC MEASUREMENTS

TEMPERATURE DROP IN THE WALL OF A STAINLESS STEEL TUBE WITH INTERNAL HEAT GENERATION AND ADIABATIC INNER SURFACE $\Delta T = \left(\frac{0.25}{12}\right) FT. \left(\frac{1}{9.7}\right) \frac{HR-FT.^{\circ}F}{B.T.U.} \left[0.500 - \frac{(0.24)^2}{(0.25)^2 - (0.24)^2} \ln \left(\frac{0.25}{0.24}\right)\right]$ $X 45,600 \frac{B.T.U.}{HR.-FT.2} = 1.9^{\circ}F$

CONSEQUENTLY, THE OUTER SURFACE TEMPERATURE PROFILES ARE Obtained by subtracting 1.9°F from each of the inner surface Temperature profiles

MAXIMUM Separation

(T ₈ -	T _B) = 23.5 °F
(T ₈ -	T _B)=23.6°F
(T	T_)=23.6 *#
(T	T_)=23.7*F
(T_s-	T _B)=23.8°F

LOCAL H. T. COEFFICIENT h = 45,600 HR.FT.2(23.7) F = 1930 HR.-FT.2F MINIMUM SEPARATION 2'

 $(T_8 - T_B) = 25.3 \circ F$ $(T_8 - T_B) = 25.6 \circ F$ $(T_8 - T_B) = 25.6 \circ F$ $(T_8 - T_B) = 25.7 \circ F$ $(T_8 - T_B) = 25.9 \circ F$

LOCAL H.T. COEFFICIENT h = 45,600 B.T.U. HR.-FT.2(1258) + F = 1785 B.T.U. HR.-FT.2*F

SECTIONAL AREA NORMAL TO THE FLOW OF WATER A= $\frac{\pi}{4} \left[\left(\frac{1.00}{12} \right)^2 \left(\frac{0.50}{12} \right)^2 \right]$ =0.00409 FT.²

MEAN WATER VELOCITY IN THE ANNULAR PASSAGE

$$V = \left(\frac{12.0}{7.48\times60}\right) \frac{FT.^{3}}{SEC} \left(\frac{1}{0.00409}\right) \frac{1}{FT.2} = 6.55 \frac{FT.}{SEC}$$

EQUIVALENT DIAMETER

D = (1.00") - (0.50") = 0.50"

FRICTION FACTOR $f = (\frac{0.50}{24})(\frac{2X32.2}{6.55X6.55})(\frac{FT}{SEC} \times \frac{SEC^2}{FT}) \times 0.78$ MERCURY X1.124 **FT.WATER MERCURY**

=0.0272 (-)

5.2 Data Correlation

Graphical procedures were used to correlate the results of the experimental study. This method of correlation was considered most desirable as the trends resulting from the variation of eccentricity and diameter ratio could be visualized best in a graphical presentation.

In correlating the heat transfer results, a dimensionless heat transfer parameter $(Nu/Pr^{1/3})$ based upon the Nusselt number (Nu) and Prandtl number (Pr) was calculated for each test and plotted on logarithmic paper as a function of the corresponding Reynolds number (Re). This procedure, which assumes that the turbulent forced convection heat transfer is dependent upon $Pr^{1/3}$ was adopted since the actual dependence upon Prandtl number had not been investigated in the experimental study. However, this assumption introduced little error in the analysis of the influence of eccentricity and diameter ratio on turbulent forced convection heat transfer since all tests were performed under nearly the same temperature conditions. As a consequence, the Prandtl number varied little from test to test, and as only relative values were required to assess the trends resulting from the variation of eccentricity and diameter ratio, the Prandtl number variation had insignificant effect upon the final analysis.

The points corresponding to each individual test upon a particular configuration were correlated with a straight line. Examination of the pertinent graphs will reveal a high degree of correlation with a maximum ± 10% point scatter about the straight line. Figure 5 and Figure 6 illustrate the correlation of the heat transfer results derived from tests upon six concentric configurations and show the influence of diameter ratio upon turbulent forced convection heat transfer in concentric annular passages. The dimensionless parameters used in plotting Figure 5 and Figure 6 were calculated with fluid property values evaluated at the bulk temperature and film temperature respectively. Figure 7, Figure 8, Figure 9 and Figure 10 illustrate the correlation of the heat transfer results derived from tests upon various concentric and eccentric configurations having diameter ratios 1.5, 2.0, 2.5, and 3.0 respectively and show the influence of eccentricity upon turbulent forced convection heat transfer. The dimensionless parameters used in plotting Figure 7, Figure 8, Figure 8, Figure 9 and Figure 10 were calculated with fluid property values evaluated at the bulk temperature.

The influence of eccentricity upon turbulent forced convection heat transfer has been calculated numerically for one Reynolds number value but the correlations presented enable the analysis to be repeated for any other Reynolds number value. In order to assess the influence of eccentricity upon turbulent forced convection heat transfer numerically values of the heat transfer parameter corresponding to each level of eccentricity were evaluated at Reynolds number equal to fifty thousand. These numerical values were ratioed to the numerical value corresponding to concentricity, giving figures of merit indicating the trend resulting from the variation in eccentricity. The analysis was performed for each level of diameter ratio investigated and the figures of merit so derived were plotted as a function of eccentricity. Figure 7, Figure 8, Figure 9 and Figure 10 show the effect of eccentricity

upon turbulent forced convection heat transfer corresponding to the particular level of diameter ratio. This information is replotted in Figure 11 where the influence of both eccentricity and diameter ratio upon turbulent forced convection heat transfer is demonstrated.

In order to clarify the procedure used in computing the dimensionless parameters and evaluating the figure of merit, sample calculations are presented on the following page.

In correlating the fluid dynamics results, the friction factor (f) computed from the experimental measurements of each test was plotted on logarithmic paper as a function of Reynolds number (Re). Figure 12 illustrates the correlation between friction factor and Reynolds number for the three concentric configurations investigated. No attempt was made at showing the influence of eccentricity upon friction factor as the results did not warrant so detailed an analysis.

THE FOLLOWING INFORMATION IS PERTINENT TO THE TEST MEAN BULK TEMPERATURE IN THE REGION OF FULLY DEVELOPED TURBULENT FORCED CONVECTION HEAT TRANSFER T_B= 104.0°F

THERMAL CONDUCTIVITY

KINEMATIC VISCOSITY

2 0.708 X10 -5 FT. 2/SEC.

PRANDTL NUMBER

Pr = 4.33

NUSSELT NUMBER

$$Nu_{B}^{*} \frac{h_{C}D_{G}}{K_{B}} = \frac{h_{C}(D_{O}-D_{i})}{K_{B}} (\frac{B.T.U.}{HR.-FT.^{2}-F}) (\frac{HR.-FT.^{*}F}{B.T.U.})$$

100

MAXIMUM SEPARATION Nug= 1930 X 0.50 12 X 0.362 = 222 MINIMUM SEPARATION Nu = 1785 X0.50 B 12 X0.362 = 206

MINIMUM

SEPARATION

HEAT TRANSFER PARAMETER

= NuB / PrB

SEPARATION

5 = 222/1.630 = 136.2

3= 206/1.630= 126.4

REYNOLDS NUMBER

$$Re_{B} = \frac{V D_{0}}{V_{B}} = \frac{V(D_{0}-D_{i})}{V_{B}} = \frac{4}{\pi} \frac{Q}{(D_{0}^{2}-D_{i}^{2})} \times \frac{(D_{0}-D_{i})}{V_{B}} = \frac{4}{\pi} \frac{Q}{D_{0}+D_{i}} \times \frac{1}{V_{B}}$$

$$(\frac{FT.^{3}}{SEC.})(\frac{1}{FT.})(\frac{SEC.}{FT.^{2}}) = \frac{4}{\pi} (\frac{12.0}{7.48\times60})(\frac{12}{1.00+0.50})(\frac{10^{5}}{0.708}) = 38,400$$

HEAT TRANSFER PARAMETER CORRESPONDING TO CONCENTRICITY

2= 132.0

FIGURE OF MERIT

MAXIMUM SEPARATION MINIMUM SEPARATION

RATIO = 136.2/132.0=1.032 RATIO= 126.4/132.0=0.955

6. **DISCUSSION**

6.1 Accuracy of Results

This section concerns the analysis of error in the correlation of the experimental results. In performing the analysis, the maximum possible error involved in each measurement was used. As a consequence, the uncertainty in the correlation of the experimental results indicated by the analysis represents the maximum error resulting from the improbable combination of the maximum values of the individual errors. It is understood that the probable error is much smaller by a considerable factor.

The fluid property values used in calculating the dimensionless parameters were assumed to be those for pure water. Although small errors are undoubtedly involved in using these fluid property values, only the error associated with reading the numerical value of the fluid property from a graph has been considered in the error analysis.

The results of the error analysis which is presented in tabular form on the following two pages, indicate that the uncertainty in the correlation of the heat transfer results could be as great as \pm 21.5% and that the uncertainty in the correlation of the fluid dynamics results could be as great as \pm 49.5%, mainly as a result of the large possible error involved in the calculation of equivalent diameter.

*	DESCRIPTION OF ERROR	MAXIMUM PERCENT ERROR	MAXIMUM ABSOLUTE ERROR
	HEAT		
	FLUX MEASUREMENT MEASUREMENT		A STATE
	-INSTRUMENT ERROR AT 1/2 SCALE	± 2.0%	-
	-VOLTAGE FLUCTUATIONS	±1.0%	1.000
2.	CURRENT MEASUREMENT		
	-INSTRUMENT ERROR AT 1/2 SCALE	± 2.0%	
3.	AREA = TT (DIAMETER)(LENGTH)	± 1.0%	
	- DIAMETER 0.500" ± 0.0025"	± 0.5%	
	- LENGTH 24" ± 0.125"	± 05%	
	ERROR IN HEAT FLUX CALCULATION	± 6.0%	
	FILM INNER WALL (TEMPERATURE) = (SURFACE)-(TEMPERATURE) DIFFERENCE TEMPERATURE DROP BULK -(FLUID)		
	- THERMOELECTRIC ERROR IN 130°F		± 1.0°F
-	- RECORDER INACCURACY		± 0.3°F
2.	WALL TEMPERATURE DROP		
	-ESTIMATED INACCURACY		± 0.1°F
3.	- THERMOMETER ERROR		±0.1°F
	ERROR IN FILM TEMPERATURE DIFFERENCE ERROR IN 30°F TEMPERATURE DIFFERENCE	± 5.0%	±1.5°F
	NUSSELT, HEAT HEAT NUMBER - (TRANSFER) (EQUIVALENT DIAMETER)		
1.	HEAT TRANSFER COEFFICIENT	+ 6 0%	
	- FILM TEMPERATURE DIFFERENCE	±5.0%	*
2.	EQUIVALENT DIAMETER = OUTER DIAMETER		
	- INNER DIAMETER		
	-OUTER DIAMETER		±0.0150
	- INNER DIAMETER	+7.5%	20.0025
3.	THERMAL CONDUCTIVITY		
	-READING ERROR ± 0.5%	±0.5%	
	ERROR IN NUSSELT NUMBER CALCULATION	±19.0%	
	HEAT (TRANSFER)=(NUSSELT)(PRANDTL)-1/3 PARAMETER		
1.	NUSSELT NUMBER		
2	-CALCULATION ERROR	±19.0%	
2.	- READING ERROR +3.0%	± 1.0%	
	ERROR IN HEAT TRANSFER PARAMETER	±20.0%	

CTION) = 29; EQUIVALENT DIAMETER) LENGTH X(PRESSURE DIFFERENCE) VELOCITY ² VELOCITY ² VELOCITY ² VIVALENT DIAMETER = OUTER DIAMETER -INNER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" SSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS OCITY = 4 VOLUMETRIO FLOWRATE OUTER INNER, OUTER INNER,	± 7.5% ± 0.5% ± 10.0%	±0.0150" ±0.0025"
LENGTH X(<u>PRESSURE DIFFERENCE</u>) VELOCITY ² VELOCITY ⁴ VELOCITY	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
VELOCITY ²) VELOCITY ²) VIVALENT DIAMETER = OUTER DIAMETER -INNER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" SSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS OCITY = 4 VOLUMETRIO FLOWRATE OUTER INNER, OUTER INNER,	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
VELOCITY ² VIVALENT DIAMETER = OUTER DIAMETER -INNER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER INNER, OUTER INNER,	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
-INNER DIAMETER = OUTER DIAMETER -INNER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIO FLOWRATE OUTER.INNER.OUTER INNER.	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
-INNER DIAMETER OUTER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER.INNER.OUTER INNER.	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
INNER DIAMETER INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER.INNER.OUTER INNER.	± 7.5% ±0.5% ±10.0%	±0.0150 ±0.0025
INNER DIAMETER ERROR IN 0.750"-0.500" IGTH ERROR IN 24" ±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER.INNER.OUTER INNER.	± 7.5% ±0.5% ±10.0%	± 0.0025
IGTH ERROR IN 24"±0.125" ISSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER.INNER.OUTER INNER.	± 7.5% ± 0.5% ± 10.0%	1 - 3 r
IGTH ERROR IN 24"±0.125" SSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER.INNER.OUTER INNER.	±0.5% ±10.0%	1-31
ERROR IN 24" ±0.125" SSURE DIFFERENCE INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER INNER. OUTER INNER.	±0.5% ±10.0%	
INSTRUMENT ERROR INSTRUMENT ERROR PRESSURE DIFFERENCE FLUCTUATIONS LOCITY = 4 VOLUMETRIC FLOWRATE OUTER INNER. OUTER INNER.	±10.0%	-
PRESSURE DIFFERENCE FLUCTUATIONS	£10.0%	
DCITY = 4 VOLUMETRIC FLOWRATE		- 1
OCITY = TOUTER INNER. OUTER INNER.	± 1.0%	1
DIAM. ' DIAM.' DIAM. DIAM.		
VOLUMETRIC FLOWRATE ± 6.0%		
OUTER DIAM. + INNER DIAM. ± 1.5%		
OUTER DIAM INNER DIAM. ± 7.5%		
ERROR IN VELOCITY ± 15.0%		
ERROR IN VELOCITY ²	±30.0%	
OR IN FRICTION FACTOR CALCULATION	±49.0%	
YNOLDS 4, VOLUMETRIC FLOWRATE)		
DIAM. + DIAM.	- 6	
X()		
JMETRIC FLOWRATE KINEMATIC VISCOSITY		
NSTRUMENT ERROR	± 5.0%	
LOWRATE FLUCTUATIONS	±1.0%	
ER DIAM. + INNER DIAM.		
UTER DIAMETER		+0.0150"
NNER DIAMETER		+0.0025
2000 IN 0750"- 0 500"	115%	200020
ENATIC VISCOSITY	£1.0 %	
READING ERROR ±0.5%	±0.5%	
	1.0.0%	
	OUTER DIAM.+ INNER DIAM. ± 1.5% OUTER DIAM INNER DIAM. ± 7.5% ERROR IN VELOCITY ± 15.0% ERROR IN VELOCITY 2 ROR IN FRICTION FACTOR CALCULATION CYNOLDS 4.VOLUMETRIC FLOWRATE UMBER = TO OUTER + INNER DIAM. + DIAM. UMETRIC FLOWRATE INSTRUMENT ERROR FLOWRATE FLUCTUATIONS TER DIAM. + INNER DIAM. OUTER DIAMETER INNER DIAMETER INNER DIAMETER ERROR IN 0.750"+ 0.500" EMATIC VISCOSITY READING ERROR ±0.5%	OUTER DIAM.+ INNER DIAM. $\pm 1.5\%$ OUTER DIAM INNER DIAM. $\pm 7.5\%$ ERROR IN VELOCITY $\pm 15.0\%$ ERROR IN VELOCITY ² $\pm 30.0\%$ ROR IN FRICTION FACTOR CALCULATION $\pm 49.0\%$ TYNOLD8 $4.VOLUMETRIC FLOWRATE$ UMBER = Π° OUTER + INNER DIAM. + DIAM.UMETRIC FLOWRATE $1000000000000000000000000000000000000$

Although these large uncertainties cast suspicion upon the validity of the correlations presented, it must be emphasized that these are extreme values which could only result from the improbable combination of the maximum values of the individual errors in connection with tests upon one particular annular test configuration. When considered in this manner, it would appear that the uncertainties in the correlations of most of the experimental results are no greater than those associated with any comparable experimental study.

6.2 Heat Transfer in Concentric Annular Passages

The results presented in Figure 5 and Figure 6 showing the influence of diameter ratio upon turbulent forced convection heat transfer in concentric annular passages are not in complete agreement with the results predicted by the correlations derived by Monrad and Pelton and Stein and Begell. The results presented appear to be dependent upon diameter ratio raised to the 1/4 power rather than diameter ratio raised to the 1/2 power as suggested by both Monrad and Pelton and Stein and Begell. However, the experimental evidence supporting this functional relationship is insufficient to justify another correlation for turbulent forced convection heat transfer in concentric annular passages.

In fairness to the results presented, it must be noted that the annular test configurations investigated in the experimental study were not identical dimensionally to the annular test configurations investigated by Monrad and Pelton and Stein and Begell. As it would

seem unreasonable to expect similar heat transfer phenomena to occur in annular passages of the same diameterratic but different dimensions, it is possible that the results of the experimental study are consistent with the correlations derived by Monrad and Pelton and Stein and Begell. Further investigation is required to resolve this point.

6.3 Heat Transfer in Eccentric Annular Passages

The results presented in Figure 7, Figure 8, Figure 9 and Figure 10 showing the influence of eccentricity upon turbulent forced convection heat transfer in eccentric annular passages are in general agreement with the results presented by Diskind and Faure. The results presented indicate that eccentricity and diameter ratio have a definite effect upon the heat transfer phenomenon and that the heat transfer from the two locations on the inner boundary of the annular passage is affected differently. Increasing eccentricity causes the heat transfer to increase at the location corresponding to the maximum separation of the inner and outer boundaries of the annular passage and to decrease at the location corresponding to the minimum separation of the inner and outer boundaries of the annular passage. Assuming a continuous variation in heat transfer around the inner boundary of the annular passage, it must be concluded that the average heat transfer decreases since the decrease in heat transfer in the vicinity of the location corresponding to the minimum separation of the boundaries is greater than the increase in heat transfer in the vicinity of the location corresponding to the maximum separation of the boundaries.

The results presented in Figure 11 showing the influence of diameter ratio upon turbulent forced convection heat transfer in eccentric annular passages are in general agreement with the results presented by Faure. At a particular level of eccentricity, the heat transfer varies in inverse proportion to the diameter ratio; the greater variations occur at the smaller diameter ratios. Ranges in which eccentricity does not influence heat transfer are found in connection with the larger diameter ratios.

The apparent explanation of the influence of eccentricity and diameter ratio upon turbulent forced convection heat transfer has been suggested by Faure. From a study of temperature profiles in eccentric annular passages, Faure was able to show that the heat transfer phenomenon was only affected by eccentricity and/or diameter ratio when the normal development of the thermal boundary layer at the inner boundary of the annular passage was disturbed by the presence of the outer boundary of the annular passage. It appears then, that the influence of eccentricity and diameter ratio upon turbulent forced convection heat transfer is derived from the development of a thermal boundary layer on the inner boundary of the annular passage. The fact that in certain annular passages, ranges in which eccentricity did not influence heat transfer were found is explained by postulating that the normal development of the thermal boundary layer was not disturbed until these ranges of eccentricity were exceeded. A mathematical solution of turbulent forced convection heat transfer in eccentric annular passages using boundary layer theory is required in order to verify this apparent explanation.

6.4 Fluid Dynamics in Concentric Annular Passages

The results presented in Figure 12 showing the influence of diameter ratio upon friction factors for turbulent flow in concentric annular passages are in excellent agreement with the results presented by Diskind. The results presented indicate that the friction factors pertaining to the different levels of diameter ratio can be correlated satisfactorily by a single straight line which approximately represents the variation of friction factor with Reynolds number for flow in a tube with 0.0005 relative roughness. It would appear that the friction factors for turbulent flow in concentric annular passages can be satisfactorily predicted from published friction factors for turbulent flow in tubes.

7. CONCLUSIONS

An experimental study of turbulent forced convection heat transfer to water flowing in nineteen different annular test configurations has resulted in graphical correlations showing the influence of eccentricity and/or diameter ratio upon the heat transfer phenomenon occurring at the two locations on the inner boundary of the annular passage corresponding to the maximum and minimum separation of the inner and outer boundaries. The correlations derived generally confirm the results obtained by other investigators and extend the range of diameter ratios investigated. The results pertaining to heat transfer in concentric annular passages are not in complete agreement with the results predicted by the correlations derived by Monrad and Pelton and Stein and Begell in that the functional relationship between heat transfer and diameter ratio appears to be different than that predicted. The results pertaining to heat transfer in eccentric annular passages are in general agreement with the results published by Diskind and Faure' with respect to the influence of eccentricity and diameter ratio upon heat transfer.

An experimental study of the fluid dynamics of water flowing in three different annular test configurations has resulted in a graphical correlation showing the influence of diameter ratio upon friction factors for turbulent flow in concentric annular passages. The correlation derived indicates that the friction factors for turbulent flow in concentric annular passages can be satisfactorily predicted from published friction factors for turbulent flow in tubes.

8. NOMENCLATURE

Arabic Symbols	Description	Units
A	Area	ft ²
As	Surface area	ft ²
∧ _C	Cross section area	ft ²
С	Specific heat	B.T.U./1b ^o F
D	Diameter	ft
D	Equivalent diameter	
	$(D_0 = 4 \frac{Cross Section Area}{Wetted Perimeter} = D_0 - D_1)$	ft
Di	Inner diameter of annular passage	ft
D	Outer diameter of annular passage	ft
D _o /D _i	Diameter ratio $(D_0/D_1 = 2 R_0/2 R_1)$	-
E	Potential drop over test section	volts
ſ	Moody friction factor	-
g	Gravitational acceleration constant	ft./sec. ²
hc	Convective heat transfer coefficient	B.T.U./hr.ft ² o
I	Current flowing through test section	amperes
k	Thermal conductivity	B.T.U./hr.ft ^o F
L	Effective length	ft
P	Pressure	ft. water
P	Pressure upstream of effective length	ft. water

Po	Pressure downstream of effective length	ft. water
P ₁ -P _o	Pressure drop over effective length	ft. water
ę	Volumetric flowrate	U.S. gallons per minute
Q	Heat generation	B.T.U./hr.
Q!	Heat generation per unit length	B.T.U./hr.ft.
QII	Heat generation per unit area	B.T.U./hr.ft ²
Qu .	Heat generation per unit volume	B.T.U./hr.ft ³
r	Radius	ft
ri	Inner radius of tube	ft
ro	Outer radius of tube	ft
R	Inner radius of annular passage	ft
R	Outer radius of annular passage	ft
8	Length of shorter support leg	ft
S	Length of longer support leg	ft
T	Temperature	°F
TB	Bulk temperature	°F
Ti	Bulk temperature at test section inlet	°F
To	Bulk temperature at test section outlet	°F
TS	Surface temperature	°F
r-Ti	Bulk temperature rise	°F
rs-TB	Film temperature difference	°F
ΔT	Temperature drop in wall of tube	°F
U	Overall heat transfer coefficient	B.T.U./hr.ft ² °F
V	Mean flow velocity	ft/sec.
W	Mass flowrate	lb/hr.

eek	Symbols	Description	Units
	α	Angle	-
	β	Angle	-
	۲	Angle	-
	δ	Separation of axes	ft
	3	Eccentricity ($\varepsilon = \frac{\delta}{R_1 - R_2}$)	-
	٢	Heat transfer parameter $(\gamma = \frac{Nu}{Pr} \frac{1}{\sqrt{3}})$	-
	ŋ	Heat exchanger effectiveness	-
	λ	Constant of integration	-
	μ	Dynamic viscosity	lb/ft.sec.
	P	Kinematic viscosity	ft ² /sec

Dimensionless Parameters

L

Gre

Description

Units

Nu	Nusselt number (Nu = $\frac{h D}{c e}$)	-
Pr	Prandtl number ($Pr = \frac{\mu C}{V k_D}$)	-
Re	Reynolds number (Re = $\frac{1}{h^{\prime}}$)	-
St	Stanton number (St = $\frac{c}{\rho CV}$)	-

etter Subscripts	Description	Unita
В	Bulk temperature	-
F	Film temperature	-
C	Cross section	-
S	Surface	-
S.S.	Stainless steel	-
i	Inner or inlet	-
0	Outer or outlet	-

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10. ILLUSTRATIONS



TEST FACILITY





3 STREAM THERMOCOUPLES LOCATION OF TEST SECTION THERMOCOUPLES 12 SURFACE THERMOCOUPLES DOWNSTREAM **3 STREAM** THERMOCOUPLES SURFACE THERMOCOUPLES ARE POSITIONED ALONG THE STAINLESS STEEL TUBE IN TWO DIAMETRICALLY OPPOSITE GROUPS AT FOUR INCH INTERVALS SPACED ALTERNATELY.

FIGURE # 4

43

UPSTREAM











FIGURE #9

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FIGURE # 12

APPENDIX

I TEST RESULTS

IMPASURED VALUES			POTENTIAL	CURRENT PRESSURE		E BULK TEMPERATURE OF SURFACE TEMPERATURES MEASURED IN THE					
1111121.00	0	~	OVER	THROUGH	DIFFERENCE	WATER CIRCULATING REGION OF FULLY DEVELOPED TURBULENT					
DIAMETER	ECCENTRICIT)	FLOWRATE	TEST	TEST	EFFECTIVE	THROUGH T	ST SECTION	FORCED CO	NVECTION H	EAT TRANS	FER
HATIO	(%)	ILS GALLONS	VOLTE	SECTION	LENGTH	UPSTREAM	DOWNSTREAN	MAXIMUM S	EPARATION	MINIMUM SE	PARATION
		23.7	22 1	AMPERES	MERCURY	*F	•F	*F	TE	*F	°F
	3	148	192	387	25 50	98.3	1011	123.3	123 7	123.3	1240
		97	15 1	306	5 40	98.2	102.6	1293	125 0	125.0	1257
15		237	21 7	44	24 80	1032	106 0	127 0	126 7	127 3	1273
15	22	9.4	19 0	384	11 10	991	102 3	122 7	122 7	126 3	126 7
		21 3	20 3	408	20 40	102.0	104.0	125 3	125 3	129 7	129 7
	39	14 8	17.8	359	10 95	999	102 6	122 0	122 3	126 7	126 7
		97	14.4	292	5 05	985	101.4	1183	118 7	123 7	123 3
		186	16.1	381	4 00	1037	105.3	131 0	131 0	130 7	130 7
	3	120	142	282	0 76	1014	102 6	131 7	132.0	132.0	132 0
		67	10.8	215	0 34	1019	104 2	131.0	131 3	131 0	131 3
		18.3	19.6	389	3 70	103 1	104 8	132 0	132 0	132 3	133.0
	29	12 0	13.4	265	0 78	102 5	104 5	129 3	1297	135 3	135 3
20		6 5	107	214	0 32	101_0	103 1	1297	130 0	132 3	132 3
	1.28	318	192	386	3 85	100 5	102 2	128 0	128 0	1287	1293
	40	12.0	13.9	27.7	0 79	99.6	101 6	1307	130 7	131 7	1317
		6 7	110	215	0 33	100 0	102 2	1297	1297	136 0	1357
		31.5	18.8	376	3 76	103.2	104 9	129 0	1290	131 3	130 7
	5.9	185	166	267	0 75	102 1	104.0	131.3	131 3	134 3	134 0
		6 7	107	214	0 35	994	101 6	1280	1280	137 3	1367
2 5	5	38 0	173	344	1 17	103 7	104 8	132 3	132 3	131 3	1323
		22 0	14.4	303	0 50	102.8	104 1	133.3	134.0	132.0	133.0
		91	10.6	207	0 10	101 2	102.9	135 0	135 7	135.0	135.0
		37 0	16.9	336	1 23	102 4	103 5	1307	1307	130 0	130 3
	22	22.4	140	280	0.51	99 2	1004	1277	1277	128 0	1280
		83	103	205	0 29	99.0	1004	1340	1340	134 3	134 7
		36 6	176	347	1 09	103 3	104.4	(327	133 0	132.0	133.3
	4.4	220	14 4	285	0 44	102.4	1036	1307	1310	131 3	132 0
		135	115	228	0 21	102.0	1033	283	1293	130.5	130 7
		376	177	352	12	1034	1045	1323	132 7	133.3	133.3
	6.2	218	140	275	0.43	1020	1031	1290	1293	131.0	1310
	02	13.9	116	228	0 23	1007	1020	1277	1267	132.3	130.7
	74	37.0	92	344	32	1035	1047	1327	133 0	1347	134 0
		213	146	287	0 52	101.4	1027	1330	133 3	1353	135 3
		13.9	119	233	0 27	1024	1037	130 3	1307	1370	138.0
		89	95	295	013	1038	1045	133 3	133 3	1327	1333
		22.4	12 6	237		1045	1055	135 7	136 0	135.3	135 7
	3	14 6	109	20.4		1022	1032	1347	135 3	135.3	135 7
		83	83	156	_	992	1022	136.0	130 7	1297	130 3
		247	14.0	264		103 2	104 2	138 7	139 7	139 0	1390
	25	15.6	115	219	-	99 5	1006	135.0	135 7	1353	135.0
		10.8	9 6	180		999	0101	1330	1340	134 3	132.0
		42 0	15.8	249		1021	103.0	1337	133 7	1333	133 0
30	43	24.4	10.6	201		1002	101 1	1293	129 3	1297	130 0
		94	84	159		102.8	103 8	1327	132 7	135.7	136 7
		42.2	16 7	318			1020	135 3	136 0	136 7	137 7
	59	25.0	13 8	225		100 2	101 3	137 3	(30.3	141.0	142.3
	1.000	97	9 5	180		99 0	100 2	136 7	138	141.7	141 7
		40.4	15.0	285		1033	1041	129.0	1297	131 0	132.0
	76	244	120	22.8		101 5	1038	136 0	1377	141.0	141.0
		94	84	159	-	102 4	1034	131 0	132.7	136.0	137 0
		550	15 3	305		99.4	1001	1310	131 3	1293	129 7
3.5	2	30.8	12.4	246	-	973	97.8	1273	1273	1273	127 7
3.5	-	19.8	99	199	-	980	98.8	1343	1343	134.0	34 3
		117	12.8	253	-	100 2	1007	1287	1283	127.3	131 7
		32.0	10 6	211		1037	1042	1283	128.3	127.0	127.7
40	6	26.0	95	186		998	1003	133.7	133.0	1330	133 3
		125	77	190	and the second se		-				

1.2 DERIVE

	IL TO	HEAT FLUX	HEAT FLUX	TE MPERATI PO					
U RESU	JLIS	CALCULATED	CALCULATED	0900	MEAN	FILM	FORCED CON	VECTION HEAT	-
		FROM	FROM	UNOP	TEMPERATUR	E DIFFERENCE	TRANSFER	OFFEIGIENT	
		EL COTRUCK	C NOW	IN			LINE CHI C	OCFFICIENT	MOODY
DIAMETER	ECCENTRICITY	MEACHINE	CALORIMETRIC	STAINLESS	MAXIMUM	MINIMUM	MA Y INITIA	A LANDAU MAN	FRICTION
		MEASURE,	MEASURE	STEEL TUBE	SEPARATION	SEPARATION	SEDA BATION	MINIMUM	PACTOR
RATIO	(%)	BTU/HR-FT ²	BTU/HR-FT	15		DET HINATION	SCHARATION	SEPARATION	
		127500	127000				ВТИИН	R-FTZ-F	-
	3	95700	27.000	54		8.1	7.0	40	OIRO
	Ŭ	50,700	97,200	41	1	9.6	48	80	0231
		39,300	61,100	2.5		8.4	32	40	0251
		123,400	125,500	5.2	15.2	172	7520	7160	0252
1.5	22	93,800	93,400	4.0	175	213	63.70	7160	0193
		69,000	76,200	29	200	2 4 3	5570	4410	0222
		106,800	107,200	45	153	100	3450	2840	0248
	39	82,200	79,200	3.5	120	108	6380	5730	0197
		54,100	57,900	23	156	200	4840	4000	0219
		93,000	95,700	40		200	3470	2700	.0236
		67,000	64,500	29			42	00	.0195
		52,000	52,800	22		20	25	80	.0232
		29,900	32400	13		0	1.9	10	.0264
		98400	99000	4.2	276	2	11	40	.0384
		75.000	72100	32	236	243	4170	40.50	0193
	29	45700	47800	52	270	284	2790	2640	0236
1 C C C C C C C C C C C C C C C C C C C		29500	1,000	19	237	256	1930	1785	0272
2.0		95400	101200	13	259	287	1140	1030	0384
	A DESCRIPTION OF THE OWNER OF THE	72200	101,000	40	221	234	4320	4080	0193
	40	12,200	12,100	31	258	276	2800	2620	0234
	and the second se	49,600	48,000	21	248	295	2000	1680	0278
		30,500	31,000	13	269	333	1130	910	0372
	and the second second	90,900	101,000	39	217	238	4 90	3820	0 92
	59	_71,100	69,100	30	250	280	2840	2540	0234
	Construction of the	45,700	48,100	20	250	305	1820	1495	0264
		29,500	30,900	12	260	364	1 35	810	0395
		76,500	76,500	32	20	5	31	20	0100
		56,400	55,100	26	2	7.0	20	90	0244
	5	38,900	38,600	17	21	17		55	0266
		28,300	31.800	12	3	8	8	90	0200
		73200	75100	31	24	1	30	10	0283
	100	50500	51600	21	20	7	30	70	0210
	22	41500	38800	19	2		19	10	0238
		27100	25800				13	30	0352
		78400	23,800	3.7	0.5.7			10	0440
		60,400	14,400		253	258	3110	30 40	0190
2.5	44	32,800	50,500	22	253	264	2080	2000	0213
		33,800	34,900	14	242	264	1395	1280	0270
		23,500	26,300	10	254	285	9 25	825	0311
		80200	76,100	34	249	264	32 30	3040	0190
	62	49,500	46200	21	244	267	2030	1860	_0211
		34,100	35,800	1.4	248	280	1370	1215	0266
		21,500	22,500	09	247	303	875	710	0272
		76,800	82,500	33	252	277	30 4 0	27 70	0225
	74	53,900	5 3,50 0	23	284	328	1900	16 45	0267
	1.4	35,700	35,900	15	260	329	1380	1090	0314
	100 C	22,600	25,500	10	261	340	870	6 6 5	0385
		55,500	50,200	23	26	4	21	00	
		38,500	41,500	16	2.6	8	13	35	
	3	28,500	29,100	12	31	2	9	15	
		16,650	17.100	0.7	32	6	5	10	-
		61800	69400	2.6	2.8	0	22	10	_
		47500	46.200	20	33	2	14	30	
	25	32400	33800	14	- 11	9	9	55	-
		22300	24100	0.9	33	5	5	85	
		61000	60700	2.0		2	20	50	
		61,000	69,500	2,6	21	2		45	
30	43	42,200	41,900	1.8	21	9		95	
		27,300	28400	12	27	8	9	80	
		17,100	19,000	07	29	-	00.30	21.00	
		68,000	70,500	2.9	307	517	22 30	2160	
	59	47,000	47,900	20	318	336	1475	1400	
	33	34,400	34,100	14	396	355	970	870	
		22,000	2 3,600	09	369	409	595	5 3 5	
		55,000	59,900	2.3	266	279	2070	1970	
		35,200	37,300	1.5	258	285	1370	1240	-
	76	30,700	33,800	13	319	371	975	630	
		17100	19.200	07	279	329	615	520	-
		60100	67500	2.5	2.8	9	20	80	
		10200	40400	17	' 30	0	1.3	10	
3.5	2	35200	27000		28	8	8	80	
	-	25,400	27,000	0.8	15	0	5	55	
		19,350	19,000	10	25	6	1.6	30	-
		41700	49200	10	20	9	10	65	
00	6	28,700	29,900	12	20	7	10	50	
40		22600	24,800	10	26	1	8		
and the second second second		14800	12600	0.6	32	1	4	50	

DIMENSIONLESS			FLUID PROPERTIES EVALUATED AT								
	PARAME	TERS		BULK TEMP	ERATURE			FLUID PROPERTIES EVALUATED AT FILM TEMPERATURE			
	DIAME TER	ECCENTRICITY	REYNOLDS	NUSSELT	NUMBER	PRANDTL	REYNOLDS	NUSSELT	NUMBER	PRANDTI	
	RATIO	(%)	NUMBER	SEPARATION	SEPARATION	NUMBER	NUMBER	MAXIMUM	MINIMUM	NUMBER	
		3	55300	41	05	454	96,200	4 (01	408	
		, , , , , , , , , , , , , , , , , , ,	35,900		3.6	4.47	61,100	2	78	398	
			92,000	437	411	434	39,400		3 5	408	
	1.5	22	55,200	310	255	448					
			35,600	199	164	440					
		39	55400	402	327	435					
		00	35,900	200	231	447					
			104,200	41	104	454					
		3	57,600	2 :	9.8	450	67300	4	75	373	
			38,000	2 2	2 2	440	43,700	2	7	373	
2 0			21,500	1	3 1	434	24,000	12	2 9	383	
			58600	479	465	433					
		29	38400	222		435					
	20		20,500	131	118	442					
	20		99,200	497	469	446					
		40	57,400	322	302	447					
			38,100	229	193	438					
			20,700	130	105	447	100				
			58300	480	438	431					
		59	36,800	210	172	442					
			20,000	131	94	450					
		1	104,800	5 3	8	431	120000	52	8	371	
		5	6 0,2 0 0	3 5	59	435	71,100	35	5 5	370	
		3	37,500	2 :	34	441	43,500	23	30	373	
			24,500	1	54	442	28,800	15	50	368	
			58900	5	1 8	438					
		22	36500	2	30	456					
			21,800	1 4	40	457					
			100,300	536	522	434					
	2.5	44	59,800	360	345	438					
	6.9		36,600	242	221	440					
			24,300	160	142	447					
			103,700	556	523	433					
		62	37100	238	211	440					
			22,200	151	123	4.47					
			101,900	522	476	433					
		74	57,300	328	284	442				فلنستعال	
			3 8,000	238	188	438					
			24,600	149	115	430	107000			170	
			93,900	48	14	433	63000	41	4	362	
		3	34500	30	0	440	40,600	20	0.6	368	
			19500		7	445	22,900	11	6	370	
			96,700	50	9	457					
		25	59,100	32	8	435					
		25	36,000	22		454					
			24,800	15	8	453					
			99,600	51	6	442					
	30	43	37400		7	452	_				
			22300		4	436					
			99400	513	497	447					
			58,000	340	322	452					
		59	36,600	222	199	450					
			2 2,300	138	124	457					
			97400	477	453	434					
		76	57,300	316	285	437					
			22300	141	119	437					
			112200	60	0	457	131,300	51	8 8	380	
			61300	37	8	470	72,400	3	7 1	388	
	35	2	39,200	2 5	5	471	46,100	2 :	50	393	
			23,600	16	0	465	28,700	13	56	377	
			104000	56	3	452	70500	5	55	382	
	40	6	61,500	36	7	433	55300		89	386	
	40	0	48,000	29	5	455	27200		5 4	376	
			23,000	15	0		21,200				

1.3

E

2. THEORETICAL DERIVATIONS

2. TEMPERATURE DROP IN THE WALL OF A STAINLESS STEEL TUBE

THE DIFFERENTIAL EQUATION

$$\frac{d^{2}T}{dr^{2}} + \frac{1}{r}\frac{dT}{dr} + \frac{Q''}{k} = 0 - (1)$$

IS POISSON'S EQUATION IN CYLINDRICAL CO-ORDINATES FOR STEADY STATE HEAT CONDUCTION IN A SOLID WITH HOMOGENEOUS INTERNAL HEAT GENERATION, EQUATION (I) CAN BE SOLVED BY SUBSTITUTING $\frac{dI}{dr} = T'$ AND $\frac{d2T}{dr^2} = \frac{dT}{dr}$.

$$\frac{dT'}{dr} + \frac{T'}{r} + \frac{Q'''}{k_{S.S.}} = 0 \qquad -(2)$$

EQUATION (2) HAS A CLASSICAL SOLUTION

$$\Gamma' = EXP \left(-\int \frac{dr}{r}\right) \left[\int -\frac{Q''}{k} EXP(+\int \frac{dr}{r}) dr + \lambda \right]$$

= EXP (- In r) $\left[\int -\frac{Q'''}{k} EXP(+ \ln r) dr + \lambda \right]$
= $\frac{1}{r} \left[\int -\frac{Q'''}{k} r dr + \lambda \right] = -\frac{Q'''}{k} x \frac{r}{2} + \frac{\lambda}{r} - (3)$

FOR A HOLLOW CYLINDER WITH AN ADIABATIC INNER SURFACE, T'=O WHEN $r = r_i$. APPLYING THIS CONDITION, GIVES

$$0 = -\frac{Q'''}{k} \times \frac{r}{2}i + \frac{\lambda}{r_i} \text{ AND } \lambda = +\frac{Q'''}{k} \times \frac{r^2}{2}i \qquad -(4)$$

CONSEQUENTLY,

B

$$r' = -\frac{Q''}{2k_{SS}} [r - \frac{r^2}{r^1}]$$
 -(5)

INTEGRATING EQUATION (5) AND APPLYING THE CONDITIONS THAT T=T, WHEN r=r, AND THAT T=T, WHEN r=r, GIVES

$$\begin{bmatrix} T \end{bmatrix}_{T_{i}}^{T_{0}} = -\frac{Q^{"'}}{2k} \begin{bmatrix} \frac{r^{2}}{2} - r_{i}^{2} \ln r \end{bmatrix}_{r_{i}}^{T_{0}}$$

$$T_{i} - T_{0} = +\frac{Q^{"}}{2k} (r_{0}^{2} - r_{i}^{2}) \begin{bmatrix} \frac{1}{2} - \frac{r_{i}^{2}}{r_{0}^{2} - r_{i}^{2}} \ln \frac{r_{0}}{r_{i}} \end{bmatrix} -(6)$$

$$UT \quad Q^{"'} = \frac{Q}{A} \times \frac{SURFACE \ AREA}{VOLUME} = \frac{Q}{A} \times \frac{2\pi r_{0}L}{\pi (r_{0}^{2} - r_{i}^{2})L}$$

$$= 2 - \frac{r_{0}}{L} \times \frac{Q}{L} - (7)$$

THEREFORE, SUBSTITUTING EQUATION (7) INTO EQUATION (6) $T_{I} - T_{0} = + \frac{r_{0}}{k} \left[\frac{1}{2} - \frac{r_{1}^{2}}{(r_{0}^{2} - r_{1}^{2})} \ln \frac{r_{0}}{r_{I}} \right] \times \frac{Q}{A} - (8)$

 $=2(r_0^2 - r_1^2)^{A}$

2.2 SUPPORT LEG LENGTHS



 $S+s+2R_{i} < 2R_{0}$

3. HEAT TRANSFER IN AN ECCENTRICALLY ARRANGED SINGLE-PASS SHELL-AND-TUBE HEAT EXCHANGER

Statement

A single-pass counter flow shell and tube heat exchanger with 4 square feet of heat transfer surface area is comprised of an inner tube 0.50" 0.D. \times 0.020" W.T. eccentrically located within an outer tube 1.25" 0.D. \times 0.125" W.T. The arrangement of the tubes is such that the eccentricity of the assembly is 60%. Oil at 155°F which flows through the inner tube at the rate of 32,000 lb/hr exchanges heat with water at 90°F which flows through the annular passage between the inner tube and outer tube at the rate of 8,000 lb/hr. Neglecting the thermal resistance of the wall of the inner tube, calculate

- (a) The rate at which heat is exchanged.
- (b) The approximate circumferential temperature variation in the wall of the inner tube at a plane midway between the ends of the heat exchanger.

Solution

(a) The solution of this problem is obtained through the use of plots of heat exchanger effectiveness η as a function of the hourly heat capacity ratio $\frac{(WC)}{(WC)} \max$ and the number of transfer units $\left(\frac{AU}{WC}\right) \min$. Such a plot for a single-pass counter flow heat exchanger is presented below.







By definition, the rate at which heat is exchanged

$$Q = \gamma (WC)_{min} (T_{oil})_i - (T_{water})_i$$

011water
$$(WC) = 32,000 \times 0.5 = 16,000 \frac{B.T.U}{hr^0 f}$$
 $(WO) = 8,000 \times 1.0 = 8,000 \frac{B.T.U}{hr^0 f}$ The heat transfer coefficient at
the inner surface of the tubeThe heat transfer coefficient at
the outer surface of the tubeseparating the oil and water is
computed byseparating the oil and water is
separating the oil and water is
computed byNu = 0.023 (Re) $^{0.8}$ (Pr) $^{0.4}$
using fluid propertiesseparating the oil and water is
separating fluid propertiesevaluated at 150°F. Thus
Re = $\frac{4}{\pi} \times \frac{32,000}{54,553500} \times \frac{12}{0.460} \times \frac{10^5}{9.3}$
= 55,400 $Re = \frac{4}{\pi} \times \frac{8,000}{60,5050} \times \frac{12}{1.50} \times \frac{10^5}{0.74}$
= 50,000Pr = 122
h_1 = 0.023 $\times \frac{0.075512}{0.460} \times$
(55,400) $^{0.8}$ (122) $^{0.4}$
= 1920 $\frac{B.7.U}{hr.ft^{20}F}$ Prom Figure 8
Maximum
SeparationNote: It was assumed that $\mathcal{I}(50,000$
2.0, 60%) was the numerical average
of $\frac{1}{7}$ evaluated at the locations of
maximum and minimum separation.
Hence $\mathcal{J}(50,000, 2.0, 60\%) =$ Maximum
 $\frac{B.7.U}{hr.ft^{20}f}$ $\frac{172 + 138}{2} = 155$ 172 $\frac{1.7.U}{hr.ft^{20}f}$

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$$\frac{(WC)\min}{(WC)\max} = \frac{8,000}{16,000} = 0.5$$

$$\frac{UA}{(WC)\min} = \frac{4}{8,000} \left[\frac{1}{\frac{r_o}{r_ih_i} + \frac{1}{h_o}} \right] = \frac{1}{2000} \left[\frac{1}{\frac{0.25}{0.23 \times 1920} + \frac{1}{2230}} \right]$$

n

$$= \frac{1}{2,000} \left[\frac{1,000}{0.565 + 0.446} \right] = 0.5$$

= 36.2% and Q = 0.362 x 8,000 (155) - (90) = 188,000 $\frac{B.T.U.}{hr}$

The solution of the simultaneous linear differential equations governing the performance of the heat exchanger yields the temperature distributions shown below. The actual temperatures in the plane midway between the ends of the heat exchanger indicate that the temperatures chosen to evaluate the fluid properties were reasonable.



(b) The average temperature in the wall of the inner tube $T_{av} = 102.3 + \left[\frac{0.446}{0.565 + 0.446}\right] (149.5 - 102.3) = 123.1^{\circ}F$

The maximum temperature in the wall of the inner tube occurring at the location corresponding to the minimum separation of the boundaries of the annular passage

$$T_{max} = 102.3 + \left[\frac{0.446 \times \frac{122}{138}}{0.565 + 0.446 \times \frac{155}{138}}\right] (149.5 - 102.3) = 124.5^{\circ}F$$

The minimum temperature in the wall of the inner tube occurring at the location corresponding to the maximum separation of the boundaries of the annular passage

$$T_{min} = 102.3 + \left[\frac{0.446 \times \frac{122}{172}}{0.565 + 0.446 \times \frac{155}{172}}\right] (149.5 - 102.3) = 121.9^{\circ}F$$

