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4	Synchrotron tomographic quantification of the influence of
5	Zn concentration on dendritic growth in Mg-Zn alloys
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15	Abstract
16	Dendritic microstructural evolution during the solidification of Mg-Zn alloys was
17	investigated as a function of Zn concentration using <i>in situ</i> synchrotron X-ray
18	tomography. We reveal that increasing Zn content from 25 wt.% to 50 wt.% causes a
19	Dendrite Orientation Transition (DOT) from a six-fold snow-flake structure to a hyper-
20	branched morphology and then back to a six-fold structure. This transition was
21	the increase in Zn concentration Further doublen triplen and quadruplen tip enlitting
22	mechanisms were shown to be active in the Mg 38wt %7n allow creating a hyper
23	branched structure Using the synchrotron tomography datasets, we quantify for the
24 25	first time the evolution of grain structures during the solidification of these allows
25	including dendrite tip velocity in the mushy zone solid fraction and specific surface
20	area. The results are also compared to existing models. The results demonstrate the
28	complexity in dendritic pattern formation in hcp systems, providing critical input data
29	for the microstructural models used for integrated computational materials engineering
30	of Mg allovs.
31	
32	Keywords: magnesium alloys; zinc; 4D imaging; dendrite orientation transition;
33	morphology transition.

35 **1 Introduction**

36 As the lightest structural metal widely used for automotive and aerospace applications, Mg alloys have tremendous opportunity for lightweighting vehicles and improving fuel 37 efficiency[1][2][3]. Due to their excellent fluidity[2], most components made from Mg 38 are generally cast into a near-net-shape mould. At the scale of the microstructure, the 39 casting process refers to the formation of dendrites, eutectic, and precipitate 40 constituents as the metal evolves from the liquid to the solid state [4][5][6]. The 41 morphology and size distribution of these features significantly affects other 42 phenomena - micro-segregation, intermetallic precipitation, semisolid rheology, and 43 grain texture – and thus determines the in-service mechanical properties[7]. 44

45 The formation of dendrites during solidification is largely controlled by the underlying crystalline structure, diffusion (both heat and solute), and anisotropy in the 46 solid/liquid interfacial energy[4][8]. In metallic systems, a variety of dendritic 47 48 morphologies and growth patterns have been observed, from the expected cubic/hexagonal morphology to feathery and seaweed grains, hyperbranched structures, 49 and dendrite orientation transitions. These observations were made post-mortem, 50 historically in 2D (via metallography, scanning electron microscopy[9][10][11]) and 51 more recently in 3D (via serial sectioning and X-ray tomography[12][13][14]), on 52 samples quenched from the semi-solid regime to "freeze-in" the microstructure. In a 53 comprehensive study on Mg alloys, Yang et al.[15] performed post-mortem X-ray 54 tomography to examine the effect of solute content on dendrite morphology and 55 orientation selection using Sn, Ba, Al, Y, Gd, and Zn elements. In particular, for Mg-56

Zn, a dendrite orientation transition was observed in which seaweed-like α -Mg structures grew for Zn content between 20-45 wt.%, while 18-branch (<20wt.%Zn) and 12-branch (>45wt.%Zn) morphologies were observed outside this range. In a similar post-mortem X-ray tomography study, Shuai *et al.*[11] also observed a dendrite orientation transition, however the seaweed structure was not seen until 38 wt.%Zn. These studies showed the possibility to control the dendritic formation patterns of Mg alloys through alloy additions.

Recently, due to advances in high-speed synchrotron X-ray radiography and 64 tomography, in situ studies of microstructure evolution during the processing of 65 metallic materials have been reported [16] [17] [18] [19] [20] [21] [22] [23]. Real-time 66 radiographic experiments at ultrafast frame rates have been largely carried out on Al-67 68 based alloys (Al-Cu[24][25][26], Al-Ni[27], Al-Si[28][29]) with thin plate-like (100-200 µm) samples, in order to study solidification phenomena including dendrite 69 coarsening, columnar-to-equiaxed transition, crystal fragmentation [26], and 70 crystallographic misorientation [30]. In situ tomographic experiments, known as 4D 71 imaging, have also been performed on similar cubic alloy systems (but at a much slower 72 frame rate) to elucidate the corresponding 3D evolution in solidification 73 microstructure[9][31][32][33][34]. For the case of Mg, with hcp crystallography and 74 high affinity for oxygen, direct 2D and 3D observations of dendritic morphology 75 evolution during solidification are limited [19][35][36]. Using radiography, Wang et 76 al.[19] investigated the effect of cooling rate on dendritic growth dynamics of Mg-Gd 77 alloy in a fixed thermal gradient. Using tomography, Shuai et al.[35] quantified the 78

effect of the cooling rate on 3D dendritic morphology evolution in a Mg-Sn alloy while
Guo *et al.*[37] examined the influence of cooling rate and solute concentration on the
coarsening kinetics of Mg-Zn alloys.

Collectively, these studies have greatly advanced our understanding of solidification microstructure evolution in complex hcp structures. In addition, they demonstrate the need for further research to reveal the dynamics of microstructural evolution and the underlying mechanisms by which solute elements alter the dendritic structures of hcp Mg alloys.

87 In the present study, the effect of Zn content on α -Mg dendritic growth patterns was investigated using 4D synchrotron X-ray tomography, X-ray diffraction (XRD) and 88 electron back-scatterred diffraction (EBSD). This research goes beyond the post-89 90 mortem tomography studies of Yang et al.[15] and Shuai et al.[11] to quantify in situ the evolution in solid fraction (f_s) , dendrite tip velocity in the mushy zone (V_{tip}) , and 91 specific surface area (S_v) in alloys having 25 to 50 wt.%Zn, and qualitatively capture 92 the influence of Zn on dendrite growth kinetics in hcp Mg alloys. By providing the first 93 quantitative kinetic data, the results both inform and validate numerical solidification 94 models of hcp metals. 95

96 2 Materials and experimental methods

97 Three hypoeutectic Mg-Zn alloys with 25, 38 and 50% weight percent of Zn were 98 selected for this study, to determine zinc's influence on the dendritic structure. The 99 solidification ranges of the three alloys are ~ 209°C (550-341°C), ~134°C (475-341°C) and ~59°C (400~341°C), respectively. The methodology for sample preparation and
encapsulation enabling 4D imaging of Mg alloy solidification is the same as that in
ref.[35]. Note that these are nominal alloy compositions, as evaporative loss may have
resulted in a reduction in the Zn content.

104 The X-ray tomography experiment was carried out at the Diamond-Manchester Beamline (I13), Diamond Light Source (DLS, UK). Each sample was heated to 30 °C 105 above the liquidus temperature, held for 30 min to ensure complete melting, and then 106 cooled at a rate of 3°C/min. During cooling, tomographic images were acquired 107 108 continuously until solidification was complete. The acquisition time was 14 s per tomogram at a voxel size of 1.6 μ m followed by a 22 s delay for system re-initialization, 109 giving a cycle time of 36 s. Subsequently, each set of 3D datasets was processed using 110 111 the Avizo software (ThermoFisher FEI) to visualize the process of solidification in Mg-Zn alloys and segment the solid and liquid phases. The experimental set-up, beam 112 parameters and image processing procedures are the same as those utilized 113 previously[35]. Please note that it was assumed that the melt temperature reached the 114 liquidus temperature in the tomogram prior to the one where the dendrites were first 115 observed irrespective of the thermocouple readout value. Further, based on the cycle 116 time and cooling rate, the temperature difference between each subsequent tomogram 117 was 1.8°C and thus this value was also assumed to be the uncertainty in temperature. 118

119 The XRD and EBSD specimens were prepared by heating cylindrical Mg-Zn alloys
120 to ~30°C above the melting point, cooled down at the same rate as the X-ray tomography
121 experiments to 30 °C below the liquidus, and then quenched into liquid metal coolant

(Ga-In-Sn). The XRD was conducted on a Bruker AXS-D8 Advance system (10° to 90°,
3°/min). For EBSD, metallography was then performed on a *Struers* automated
grinding and polish machine following the standard procedure. After final polish with
OP-S (0.04µm), the specimens were etched for 2-3s with a solution of 5ml nitric acid,
15ml acetic acid, 20ml distilled water and 60ml ethanol. The EBSD was conducted
using a Zeiss Crossbeam 540 equipped with NordlysMax2 detector and HKL Channel
5 data analysis system.

129 **3 Results and discussion**

130 **3.1 Qualitative analysis**

131 **3.1.1 Dendritic morphology evolution during solidification**

Fig. 1 and supplementary videos V1, V2 and V3 show the dendritic morphology 132 133 evolution of three different Mg-Zn alloys at different temperatures within the mushy zone as 2D cross-sectional slices extracted from the middle of each tomogram. As can 134 be seen, distinctive dendritic morphologies were observed at each of the different Zn 135 contents. Specifically, a coarse and globular-like dendritic structure was obtained at 136 137 Mg-25wt.%Zn, a hyper-branched structure was obtained at Mg-38wt.%Zn, and a dendritic structure with branched arms around the trunk was obtained at Mg-50wt.%Zn. 138 For all the alloys, it appears that the majority of the grains nucleated on the sample 139 140 wall and grew towards the sample center. This is potentially due to the MgO skin on the surface acting as heterogeneous nucleation sites for the α -Mg grains[38][39]. With 141 increased solid fraction, an increase in the image contrast was observed. This was a 142

result of Zn being rejected from the growing dendrites to the liquid phase. Finally, for 143 the images b4 (Mg-38wt.%Zn) and c4 (Mg-50wt.%Zn), increased attenuation in the 144 145 interdendritic region was observed, suggesting that this region has solidified forming eutectic (i.e. the eutectic temperature was reached), showing as darker in the image due 146 to the solid's increased density and additional scattering of x-rays[25]. This final feature 147 is best seen in supplementary videos V1, V2 and V3. Note that the final ΔT in Fig. 1 148 (a4, b4, c4) does not correspond perfectly to the solidification range for the three alloys 149 from the phase diagram, but instead is ~15 °C less. This may be due to either evaporative 150 151 loss of Zn changing the composition during multiple melting/solidification experiments, and/or a change in the furnace temperature distribution resulting from latent heat 152 evolution. This inaccuracy in the solidification range does not affect the dendritic 153 154 growth observations, but may shift the Zn concentration at which they occur.



Fig. 1: 2D image sequence showing dendritic morphology evolution as a function of solid fraction and temperature in Mg-25wt.%Zn (a1-a4), Mg-38wt.%Zn (b1-b4) and

158 Mg-50wt.%Zn (c1-c4) alloys (ΔT indicates the temperature below T_{liquidus}). All the 159 figures share the same scale bar; the dark grey areas on the margin represent the gap 160 between the sample and graphite tube.



161

Fig. 2: 3D dendritic morphology evolution for Mg-25wt.%Zn (a1-a4), Mg-38wt.%Zn (b1-b4) and Mg-50wt.%Zn (c1-c4) alloys (ΔT indicates temperature below T_{liquidus} ; all the figures share the same scale bar).

To examine the 3D growth of dendrites during solidification, isolated 165 representative dendrites were extracted from each acquired tomogram. Fig. 2 and 166 167 supplementary videos V4, V5 and V6 show the morphological evolution of the three Mg-Zn alloys tested. From the earliest growth stage onwards, the microstructures of all 168 three alloys are seen to be dendritic from a 3D perspective[35]. For the case of Mg-169 25wt.%Zn, Fig. 2 (a1-a4), it would appear that dendritic growth and coarsening 170 occurred concurrently. For the cases of Mg-38wt.%Zn and Mg-50wt.%Zn, dendritic 171 growth is evident but coarsening is more difficult to clearly observe. As coarsening is a 172 173 time-dependent process, the decreasing solidification interval occurring with increasing Zn content results in shorter time for the structure to coarsen and thus its effects are 174

175 difficult to quantify. It can also be seen from Fig. 2 that, with an increasing Zn content, 176 the morphology of primary α -Mg grains became more complex with a higher number 177 of dendritic branches, and an increase in the number of secondary dendrite arms. In 178 other words, as the Zn concentration increases, dendrites in Mg-Zn alloys appear to 179 produce finer branches that split more frequently. This is best seen by comparing Figs. 180 2 al, bl, and cl.

Fig. 3 plots the local mean curvature distribution for each of the three dendrites 181 shown in Fig. 2 at a time when the average solid fraction in the tomogram was 0.15. 182 Mean curvature, H, is defined as $(1/R_1 + 1/R_2)/2$, where $1/R_1$ and $1/R_2$ are the 183 two principal curvatures at any point on the dendrite. Along with the distribution, 184 images of the three dendrites are shown. In these images, a red colour indicates large 185 186 positive values of H, and thus local regions with large positive mean curvature / dendrite arms having the finest tip radii, while a green colour indicates neutral values 187 of H. As can be seen, with increasing Zn concentration, the dendritic surface area having 188 a large mean curvature also increases. This experimental result agrees well with the 189 experimental finding in succinonitrile-acetone alloys where an increase in dendrite tip 190 curvature was observed with an increase in acetone concentration [40]. 191



192

Fig. 3: Mean curvature (*H*) distribution of separated dendrites in Mg-25/38/50wt.%Zn alloys at a solid fraction of 0.15. The scale bar has a length of 300 μ m.

3.1.2 Dendritic morphology transition with increasing Zn concentration

Dendrites in Mg alloys generally evolve as a six-fold hcp symmetric snowflakelike structure[10][41][42][43]. However, due to the weak anisotropy between symmetric growth directions, the preferential growth orientations of α -Mg dendrite are influenced by many factors. These include alloying elements and solute concentrations, as well as imposed thermal conditions, resulting in a diversity of α -Mg dendrite morphologies possessing both six-fold symmetrical structures and those with abnormal structures formed during solidification[10][11][44][45][46].

As shown in Fig. 2, the dendritic morphologies in the studied alloys were found to transform from a six-fold snowflake-like structure in Mg-25wt.%Zn to a hyperbranched structure in Mg-38wt.%Zn and then subsequently back to a six-fold symmetry morphology in Mg-50wt.%Zn alloy. In Mg-25wt.%Zn a typical six-fold structure was present from the view of the basal plane. However, the dendritic arms were found to split on the basal plane and tended to grow along the direction of the prismatic plane. In contrast, while a six-fold structure was also observed in Mg-50wt.%Zn from the perspective of basal plane, only 4 branches were present on the prismatic plane, and the
branch arms on the basal plane disappeared and grew along a direction between the
basal plane and prismatic plane[11].

- In order to further confirm the dendrite orientation transition, XRD and EBSD 213 214 measurements were performed on the quenched samples. From the XRD patterns shown in Fig. 4, three different phase constituents, α -Mg (*P63/mmc*, a=b=3.209Å, 215 sc=5.211Å, c/a=1.624, $\alpha = \beta = 90^{\circ}$, $\gamma = 120^{\circ}$), Mg₇Zn₃ (*I*, a=b=c=14.170Å, $\alpha = \beta = \gamma = 90^{\circ}$), 216 Mg₂Zn₁₁ (*Pm3(200*), a=b=c=8.552Å, $\alpha=\beta=\gamma=90^{\circ}$) were observed and the <11 $\overline{2}$ 0> 217 direction of α-Mg on the basal plane can be observed in Mg-25wt.%Zn alloy, while in 218 Mg-50wt.%Zn, it is clear that $<11\overline{2}0>$ disappeared and only $<11\overline{2}1>$ was found. In Mg-219 38wt.%Zn, some anomalous diffraction peaks were observed. This is further clarified 220 221 by the EBSD results, shown in Fig. 5. Specifically, the preferred growth direction of α-Mg for Mg-25wt.%Zn was found to be $<11\overline{2}0>$ (Fig. 5 a2) and in Mg-50wt.%Zn alloy, 222 the preferential orientation was observed to be $<11\overline{2}1>$ (Fig. 5 c2). The results for Mg-223 38wt.%Zn (Fig. 5 b) show that the branching structure and growth orientation of these 224 dendrites were much more complicated than in either the Mg-25wt.%Zn and Mg-225 50wt.%Zn. 226
- 227





Fig. 4: XRD patterns of Mg-25/38/50wt.%Zn alloys showing the orientation selection
in these three alloys.



Fig. 5: EBSD measurement showing the preferential growth direction in: (a-a2) Mg-25wt.%Zn, (b-b3) Mg-38wt.%Zn, and (c-c2) Mg-50wt.%Zn

In general, the preferential growth direction of dendrites is known to be determined 236 by the anisotropy in interfacial free energy and thus the transition in dendrite growth 237 238 orientation can be attributed to changes in this quantity [4]. There are a variety of factors that might affect the anisotropy in solid-liquid interfacial free energy during the growth 239 of a dendrite: including (i) lattice defects (lattice distortions and/or stacking faults), (ii) 240 the formation of twin grains, (iii) fast cooling rates, and (iv) an increase in the 241 concentration of a solute element with high anisotropy in solid-liquid interfacial free 242 243 energy.

Of these, the first can be discounted in Mg-Zn because although lattice distortions and stacking faults are likely induced when Zn forms a solid solution in Mg, all three alloys are above the solid solubility limit. Hence, a similar number of lattice defects would be expected to form.

The second is seen as unlikely because the investigated system is binary while 248 twins are frequently seen in ternary systems. As reported by Kurtuldu et al. [46], a trace 249 addition of Cr (typically 200 to 1000 ppm) in Al-20wt.%Zn alloy was shown to 250 drastically modify the alpha-Al dendrite growth direction from <100> to <110>; this 251 was correlated in [46] to the formation of a surprisingly large number of twinned grains. 252 However, from the EBSD results shown in Fig. 5 and previous EBSD studies in Mg-253 Zn alloys[11][44][47], no obvious twin grains were observed to initiate this mechanism. 254 The third can be eliminated since similar hyperbranched/seaweed microstructure 255 was observed in Mg-Zn alloys when cooled under a range of cooling rates (3°C/min 256 (this study), 6°C/min[11] and quick quench[15]). 257

Thus, based on the results obtained in this study, it is likely that the observed dendrite orientation transition is caused by the increase in solute content as Zn is known to have a very strong anisotropy in solid/liquid interfacial energy. Because of the low solubility of Zn in Mg, we hypothesize that the structural changes occur on the liquid side, perhaps by a concentration-dependent atom cluster that forms adjacent to the dendrite growth front and changes continually the surface energy.

This hypothesis that Zn content is modifying the anisotropy in solid/liquid 264 interfacial energy in the Mg-Zn system to cause the change in growth directions is 265 266 supported by the molecular dynamics (MD) simulations of Sun et al.[45]. In these simulations, it was found that the anisotropy between different symmetric directions in 267 pure magnesium was rather small, therefore, the interface free energy anisotropy of α -268 269 Mg could be easily changed through the addition of a solute with high anisotropy. Due to present limitaions of MD calculations in binary systems[47], the community cannot 270 yet perform realistic simulations for the interfacial free energy anistropy in Mg-Zn 271 272 alloys. It is hoped that the present study and similar studies will encourage experts in MD to focus their attention on developing methods to help explain the phenomenon 273 observed in this work. 274

The dendrite morphologies presented in this study can be used to validate the numerical simulations, i.e. phase-field models, that are currently being used for predicting dendrite growth patterns in engineering metals. However, the phase-field simulation results will only match experimental results if the anisotropy function is properly accounted for. To give an example, although the Mg-Zn phase field simulations of Wang *et al.* [10] did show hyper-branched dendrite morphology at intermediate compositions, they used an anisotropy function having the preferred orientations of <1120> and <2245> based on [48]. These simulation results do not agree very well with the experimental results in this study where the dendrite orientation transitioned from <1120> to <1121>. Thus, in hcp systems, it is clear that a combination of simulations and experiments is needed to accurately quantify anisotropy in interfacial free energy.

287 3.1.3 3D evolution of hyper-branched structures in Mg-Zn alloy

Through analysis of the 3D datasets, it appears that three tip-splitting mechanisms 288 are responsible for the formation of hyper-branched structures at Mg-38wt.%Zn. These 289 are shown in Fig. 6: doublon (Fig. 6 al-a4 and dl-d4), triplon (Fig. 6 bl-b4) and 290 quadruplon (Fig. 6 c1-c4), respectively. These hyper-branched structures are similar to 291 ones displayed in succinonitrile-camphor under microgravity condition (Fig. 6 a1, b1, 292 c1) by Bergeon et al. [49]. However, only the final shapes (doublon, triplon or 293 quadruplon) were obtained in that study due to the limited temporal resolution of the 294 295 experiment; the evolution of seaweed structure and the tip splitting mechanisms were not captured. In the present study, the mechanisms of tip splitting were directly captured. 296 Specifically, (i) for the doubloon, the dendrite tip was observed to split in two parts 297 about its central axis with a narrow liquid groove in between (Fig. 6 a2-a4) and it is 298 similar to what was observed in directionally solidified Al-4wt.%Cu[50] and pure 299 Cu[51] metals in previous studies; (ii) for the triplon, the dendrite tip was observed to 300 split into three small tips simultaneously during growth (Fig. 6 b2-b4); (iii) for the 301

quadruplon, the tip dendrite was observed to first split into two tips (doubloon) and then
each doubloon split again into two tips making four tips in total (Fig. 6 c2-c4) through
a "doubling doublons" mechanism rather than quadruplon branches forming
simultaneously. It is worth noting that although the doublon structure was present in
both Mg-38wt.%Zn and Mg-50wt.%Zn alloy, triplon and quadruplon structures were
only observed in the Mg-38wt.%Zn alloy.



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Fig. 6: Dendrite tip splitting mechanisms during the solidification of (a1, b1, c1) bulk
transparent (succinonitrile–camphor) alloy (after ref.[9]), (a2-a4, b2-b4, c2-c4) Mg38wt.% alloy and (d1-d4) Mg-50wt.%. (ΔT indicates the temperature below liquidus.
Figures (a2-a4, b2-b4, c2-c4, d1-d4) share the same scale bar. Note no scale bar was
given in reference[9] after which images a1, b1 and c1 were taken).

314 Seaweed-like microstructures usually form under various situations like isotropic

or weakly anisotropic conditions or with increased undercooling[52][53]. In the current 315 study, the sample was solidified under a relatively low cooling rate, and it is unlikely 316 317 that the hyper-brached structures resulted from large undercooling. Instead, we hypothesize that the formation of seaweed-like hyper-branched microstructure is a 318 result of the Zn addition and the corresponding modification of the interfacial free 319 energy anisotropy of α -Mg dendrites. This phenomenon correlates well to that observed 320 in Al-(10~90)wt.%Zn alloys where a dendritic orientation transition occurred with an 321 increase in Zn content and a hyper-branched structure formed at interim Zn 322 323 concentration (e.g. Al-55wt.%Zn)[4]. Abnormal and complex dendritic growth morphologies were also previously observed in a number of transparent systems[51][54] 324 and metallic alloys[4][45][50]; the observations of dendrite growth in Figure 4 help to 325 326 explain the development of such structures.

327 **3.2 Quantitative analysis**

328 **3.2.1** Evolution of dendrite solid fraction with temperature

The overall evolution in volume fraction of primary α -Mg dendrites with 329 temperature was calculated from the 3D datasets, and is shown in Fig. 7 along with the 330 corresponding lever rule and Scheil predictions. For the Scheil equation, the partition 331 coefficient was assumed to be constant with a value of $k_0=0.146[55]$. As can be seen, 332 the measured results for all three alloy systems, except during the later stages, were 333 generally in agreement with the Lever rule and far from the Scheil model. In the case 334 of Mg-50wt.%Zn, the the rapid increase in solid fraction at ~360°C is a result of eutectic 335 solidification and thus the Lever rule no longer applies. Although it is widely 336

recognized that the partition coefficient varies with solutal concentration in a binary 337 system, varying k_0 for the three alloys did not provide any meaningful difference in the 338 position of the Scheil model fraction solid relative to the experimentally-collected data. 339 Interestingly, in the previous work for Mg-15wt.%Sn alloys under the similar 340 cooling rate[35], the measured evolution in solid fraction matched the Scheil 341 predictions and not the Lever rule. The difference in the solid fraction evolution with 342 temperature between Mg-Zn and Mg-Sn alloys may result from the underlying 343 thermodynamic parameters of the alloying elements (solute diffusion and solute 344 345 partition coefficient) as either analytic curve can be shifted to fit the experimental data depending on these values. Note that the dendrite morphology will also influence the 346 distribution of solute concentration during solidification and hence influence the 347 348 evolution of solid fraction.



Fig. 7: Measured evolution of solid fraction together with values determined via the
lever rule and Scheil Equation. (Note, change from filled to hollow symbols
denotes in the cooling rate near the end of experiment.)

353 3.2.2 Influence of zinc on dendrite tip velocity in the mushy zone during 354 solidification

The evolution in dendrite tip velocity (V_{tip}) in the mushy zone was characterized in 355 each of the three alloys in order to provide insight into the effect of solute concentration 356 on dendrite growth kinetics. This was carried out by segmenting several representative 357 equiaxed dendrites and then measuring the evolving dendrite arm length (L) during the 358 solidification process. As can be seen in Fig. 8, V_{tip} in the mushy zone was observed in 359 all three alloys to decrease continuously with time and then arrest at the end of 360 solidification. The gradual decrease of dendrite tip growth rate was mainly ascribed to 361 the rejection of solute ahead of the growing grains, hindering the growth of dendrite 362 arms. As demonstrated in an Al-Cu alloy by Bogno et al.[24] (Fig. 4a and b) the 363 decelerating regime emerges when the far-field solute concentration ahead of the 364 dendrite tip starts to increase because of an overlap between the solute fields of adjacent 365 grains. It must be stated that the initial accelerating growth stage of dendrites are not 366 captured due to a limited temporal resolution between tomograms; this phenomenon 367 can only be captured using ultrafast 2D radiography which which will be on the order 368 of 1000 times faster than tomography[56]. 369

Fig. 8 also shows that all three curves reach a plateau at about 220s after the initial solidification. The duration of the decelerating growth stage as a fraction of total solidification time for each of the Mg-25/38/50wt.%Zn alloys is estimated to be about 5%, 11% and 20%, respectively. This indicates that the dendrite morphology evolution was dominated by tip growth only at the early stage of solidification and then solidification occurred through lengthening and thickening of secondary arms.

As plotted in Fig. 8, the fraction of the dendrite tip growth period with respect to 376 the total solidification time increases continuously with increasing Zn content. The 377 experimental results therefore indicate that the amount of Zn influences dendritic 378 growth kinetics during solidification. This effect can be considered in terms of growth 379 restriction factor (GRF)[57]. Specifically, the addition of solute elements generates 380 constitutional undercooling within a diffusion layer ahead of the solid/liquid interface, 381 restricting dendritic growth and thus limiting the overall growth rate. As suggested by 382 383 Lipton et al.[40], the dendrite tip growth velocity in the mushy zone was closely related to solute concentration and dendrite morphology (tip radius). The tip radius in Mg-Zn 384 alloys was demonstrated to decrease with the increasing zinc concentration, as shown 385 386 in Fig. 3. The difference of dendrite tip velocity in the mushy zone might also be attributed to the diversity of dendrite morphologies and growth orientations. 387



Fig. 8 Average dendrite tip velocity in the mushy zone as a function of solidification time for Mg-25/38/50wt.%Zn alloys. A few dendrites were measured for each composition. The error bars in the figure indicate the standard deviation of the measured values.

393 **3.2.3** Effect of solute concentration on specific surface area evolution

The microstructure evolution during dendritic growth and coarsening can be 394 assessed through analysis of the change in specific surface area (S_{ν}) with solidification 395 time or solid volume fraction. Voorhees et al.[13] reported that the inverse of specific 396 surface area usually follows a $S_v^{-1} \sim t^{1/3}$ power law during isothermal coarsening of both 397 equiaxed and directionally solidified dendrites. Further research has shown that the 398 temporal exponent is not exactly 1/3 but varies based on solidification conditions[59]. 399 A more general law is thus, $\frac{S_v}{S_{v_0}} = [1 + k \times (S_{v_0})^n \times t]^{-1/n}$ 400 (Eq. 2) or $S_v^{-n} - S_{v_0}^{-n} = kt$ (Eq. 3) where S_{v_0} is the initial value of S_v (1/µm), t is the 401 solidification time, and n and k are fitting parameters. $k (\mu m^n/s)$ is generally known as 402 the coarsening rate constant. Although Equation (3) was derived for isothermal 403 conditions with constant values of interfacial energy and diffusion coefficient, it will 404 also provide a good fit during non-isothermal conditions if one assumes that the 405 temperature variation in the interfacial energy and diffusion coefficient are small[60]. 406 Researchers are working to overcome this limitation, as recently demonstrated by 407 408 Beckermann et al. [61] who proposed a more general equation for specific surface evolution during solidification. 409

Fig. 9 shows the plots of $S_{\nu}/S_{\nu 0}$ as a function of time for the three Mg-Zn alloys, along with the fitted curves at the early growth stage. As can be seen in the figure, the specific surface area for all three alloys decreases continuously with solidification time, as expected. The specific surface area at the final stage of solidification is also seen to increase with increased Zn content. As the lines show, Eq. (3) provides a reasonable fit to the experimental data, assuming different fitting parameters are used. With increasing Zn concentration, the exponent *n* increases slightly, while the coarsening rate *k* decreases dramatically. The increasing *n* and decreasing *k* indicate a slower coarsening process. This is consistent with the qualitative results shown in Figure 2, where coarsening was clearly evident in the Mg-25wt.%Zn alloy, but hardly visible in the Mg-50wt%Zn alloy. The results are also consistent with results of isothermal coarsening experiments conducted on this alloy system [37].

To comprehensively reveal the evolution of a specific surface area, especially in 422 423 relation to growing dendrites during solidification, it is imperative to quantify the specific surface area of dendrites by temperature or solid fraction, as described in a 424 model proposed by Cahn[62] and further developed by Rath[63]. This model links the 425 426 specific surface area (S_v) of the dendrite, to its solid fraction (f_s) during solidification and is expressed as follows: $S_v = K \times (f_s)^m \times (1 - f_s)^n$ (Eq. 4) 427 where K, m and n are constants, f_s is the volume fraction of solid phase and m=n=2/3428 429 according to [62] or 0 < (m, n) < 1 based on the fitting value from results described in [63]. Fig. 10 illustrates the variations of S_{ν} with solid fraction (f_s), along with the fitted 430 curves. As can be seen, the curves are able to match the experimental data although m431 and K must both be taken as fitting parameters. Interestingly, the exponent m has a 432 negative value. Cahn and Rath's model assumes the initial grain shape is globular, 433 hence the specific surface area initially increases with solid fraction and then 434 continually decreases when f_s exceeded ~0.5. However, in this study, as Figs. 1-3 show, 435

436 the initial growing grains are already dendritic-like with hierarchical branches.

Therefore, due to the interaction of solute rejected by adjacent solidifying dendrites and the limitation and restriction of solute diffusion at higher solid fraction, it is reasonable that the coarsening process tends to decelerate with increasing solid fraction, causing the value of m to be negative, i.e. we are not capturing the very initial stages of spherical growth and it's degeneration, which is happening on a very fine scale and/or a very short time period.



443

Fig. 9 Normalised specific surface area evolution as a function of solidification time in
Mg-25/38/50wt.%Zn alloys. Fitting curves using the model proposed by Poirier in
ref.[59] (Eq. 2) are also plotted. (Note, change from filled to hollow symbols denotes
an increased cooling rate; hollow data was not used for fitting.)



Fig. 10 Specific surface area evolution as a function of solid fraction, and fitted curvesusing modified Rath and Cahn's model.

451 4 Conclusions

Using 4D synchrotron X-ray tomography, the dendritic growth dynamics of primary α-Mg grains during the solidification of Mg-Zn alloys with various Zn concentrations was investigated both qualitatively and quantitatively. These *in situ* observations demonstrate conclusively that a dendritic morphology transition occurs in Mg-Zn alloys. This finding, along with prior similar findings in fcc Al, strongly supports the hypothesis that Zn modifies the anisotropy in interfacial energy in alloy systems that have inherenly weak anisotropy in interfacial energy (e.g. Mg, Al).

459 Synchrotron tomography revealed the mechanisms by which hyper-branched 460 structures form, i.e. via doublon, triplon and quardrulon (or doubling doublons). The 461 dynamic formation of these structures was captured and quantified, revealing new tip-462 splitting mechanisms.

Analysis of the time resolved 3D images allowed the first quantification of the 463 microstructural evolution of Mg-Zn alloys during solidification, including: solid 464 fraction (f_s), dendrite tip growth velocity (V_{tip}), and specific surface area (S_v). The f_s 465 variations with temperature were found to correlate well with lever rule. Dendrite tip 466 growth was found to decelerate continuously with solidification time, and dendrite tip 467 growth as a mechanism of dendrite morphology evolution was found to dominate only 468 at a very early stage of solidification. The evolution of S_{ν} during dendritic growth 469 compared well with Poirer's model[59], demonstrating the rate of dendritic coarsening 470 471 decreases with increasing Zn concentration. The data was also fit to Cahn and Rath's equation to reveal the evolution of S_v with f_s during solidification. 472

These 4D observations provide both the first quantification of dendritic growth dynamics during the solidification of these magnesium alloys, providing a method for both informing and validating numerical models of microstructural evolution, e.g. phase field simulations and cellular automata methods.

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486 Data statement

Representative samples of the research data are given in the figures and supplementary
data. Other datasets generated and/or analysed during this study are not publicly
available due to their large size but are available from the corresponding authors on
reasonable request.

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