

AN EXPERIMENTAL STUDY OF THE
HYDRODYNAMIC SUSPENSION OF SPHERES
AND SPHERE TRAINS IN A VERTICAL PIPE
USING WATER AND POLYMER SOLUTION

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USING WATER AND POLYMER SOLUTION

By

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TITLE: An Experimental Study of the Hydrodynamic Suspension of Spheres
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SCOPE AND CONTENTS:

This thesis describes an experimental study of hydrodynamically suspended spheres and sphere trains in a vertical pipe, using water and polymer solution as the suspending medium.

The experiments involved hydrodynamically suspending single spheres in a pipe for the sphere to pipe diameter ratios of 0.105 to 0.956. Drag coefficients were found from a force balance which involved measuring the average velocity of flow approaching the spheres while the pressure drops were found by direct measurement. The experiments on single steel and plastic spheres were carried out in both water and dilute aqueous polymer solution, while the tests on trains of spheres were carried out in water only on train lengths of up to twelve spheres.

From the correlations for drag coefficients and pressure drops of this data, comparison with other authors, especially with data obtained by McNown and Newlin⁽²⁾, Round and Kruyer⁽²¹⁾, and Tawo⁽²⁸⁾ were made.

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NOMENCLATURE

A	Cross sectional area of the sphere
B_1	Similarity law constant for polymer, see Granville ⁽¹⁹⁾
C	Characteristic polymer concentrations, see Granville ⁽¹⁹⁾
C_d^*	Drag coefficient in a bounded medium
C_d	Drag coefficient in an unbounded medium
C_f	Darcy-Weisbach friction factor
D	Diameter of pipe
GPM	Flowrate in Imperial Gallons per Minute
F_i	A force, such as gravity, buoyancy, or drag
$L = \lambda_1, \lambda_2 + nd$	Distance between pressure taps
L_c	Length of capsule
P	Polymer characteristic, dependant upon species and concentration, see Granville ⁽¹⁹⁾
P_i	An upstream or downstream pressure
PR1, PR2	A pressure ratio term, see Tawo ⁽²⁸⁾
ΔP	A pressure drop
ΔP_m	Actual pressure drop between pressure taps
ΔP_L	Pressure drop between taps due to liquid alone

$\Delta P'_L$	A pressure drop which when added to ΔP_L gives the pressure drop due to the liquid flowing at V_{AV} whose flow pattern is changed by the presence of the spheres
ΔP_S	The pressure drop associated with the support of the spheres but not including the end effects
ΔP_T	The pressure drop associated with the support of the sphere, but including the end effects
ΔP_E	A total "end effect" pressure term
ΔP_{Ei}	The end effect pressure drop terms for the leading and trailing ends of the trains
$(\frac{dP}{dZ})_T$	Pressure gradient along the sphere train
$(\frac{dP}{dZ})_L$	Pressure gradient due to liquid, with no sphere present
$(\frac{dP}{dZ})'_L$	Pressure gradient which when added to $(\frac{dP}{dZ})_L$ gives the gradient due to the liquid moving at V_{AV} whose flow pattern has been modified by the presence of the spheres
R_e	Reynolds number
R_{eN}	Apparent Reynolds number, flat plate polymer flows, see White ⁽²⁵⁾
R_{eX}	Flat plate Reynolds number for Newtonian fluid
T	Temperature
U	Free stream or centerline velocity

v_c	Velocity of capsule
v_{AV}	Average fluid velocity
\mathcal{U}	Volume of sphere
V	Velocity
W_{ppm}	Weight parts per million, a polymer concentration
$Z_i, \Delta Z$	An elevation
c	Capsule to pipe friction
d	Diameter of capsule or sphere
f	Fanning friction factor
g	Local acceleration due to gravity
g_c	Gravitational constant
h_m	Apparent manometer reading (cm. of manometer fluid)
h_{ACT}	Manometer reading, excluding thermal density effects (cm. of manometer fluid)
$h_0 = h_m - h_{ACT}$	Thermal density effects (cm. of manometer fluid)
$(h_m)_0$	Manometer reading at no flow
h_f	Head loss
k_c	Surface roughness of capsule
k_p	Surface roughness of pipe

k	Prandtl's mixing length constant
l_i	Characteristic polymer length, see Granville ⁽¹⁹⁾
m_i	Characteristic polymer mass, see Granville ⁽¹⁹⁾
t_i	Characteristic polymer time, see Granville ⁽¹⁹⁾
$l^* = \frac{u_* \rho}{\nu}$	Characteristic polymer length, see Granville ⁽¹⁹⁾
m	Total mass, water or polymer
\dot{m}_p	Mass flowrate of the polymer, not including water
n	Number of spheres in train
$u^+ = \frac{u}{u_{*0}}$	Law of the wall variable
u	Velocity at v in a positive x direction
$u_* = \sqrt{\frac{\tau}{\rho}}$	Friction velocity
$u_{*0} = \sqrt{\frac{\tau_0}{\rho}}$	Friction velocity at the wall
u'_{*0}	Threshold friction velocity, see White ⁽²⁵⁾
x	Distance
$y^+ = \frac{y u_{*0}}{\nu}$	Law of the wall variable
y	Distance normal to the wall
τ	Shearing stress
ρ	Density; not subscripted for solvent
σ	Density of spheres

δ	Boundary layer thickness
β	Law of the wall constant
ν	Kinematic viscosity
μ	Dynamic viscosity
α	Property of the polymer, see White ⁽²⁵⁾
θ	Angle of inclination
γ	Specific gravity

SUBSCRIPTS:

p	Polymer
W	Water
T	Total value
0	Value at the wall
AV	Average value
i	Discrete values, 1, 2, 3, etc.

I INTRODUCTION

The behaviour of a sphere moving through a viscous fluid has been the subject of research since 1851, when Stokes first considered a sphere settling in air at a very low Reynolds number. Following Stokes, there have been a succession of authors advancing and refining the theory of settling for both single and agglomerations of spheres.

Recently the need to transport material that cannot be contaminated by the transporting fluid of the pipeline has become apparent. These transportation systems enclose the material to be transported within a spherical or cylindrical capsule whose diameter approaches that of the pipe. The information presently available on the dynamics of dense fields of particles has permitted slurry pipelines to be designed, however this data is not sufficient for the design of capsule pipelines and research had to be carried out to determine what effect the constraining walls had on the motion of the capsules.

The earliest work carried out on this subject was an experimental study performed by McNown and Newlin⁽²⁾ in 1951 in which they measured the drag coefficient of a sphere rigidly fixed in a uniform flow field constrained within a tube. This work was further extended in 1967 by Round and Kruyer⁽²¹⁾ by an experimental study which determined the effect of specific gravity ratio and diameter ratio on spheres suspended in fully developed turbulent flow in inclined tubes. Other authors have studied related topics, such as the movement of capsules through pipelines and the pressure drop along sphere trains rigidly fixed to the pipe wall. Much remains to be done on these studies but an aspect that cannot be neglected is the effect of drag reducing compounds.

The behaviour of a sphere settling in an unbounded drag reducing fluid was studied by A. White^{(15), (24)} in 1966 and 1967, and by Chenard⁽¹⁹⁾ in 1967. The results of these experiments were consistent, and indicated that with a laminar boundary layer the drag on a sphere is reduced, but that with a turbulent boundary layer the drag was increased. This is approximately the reverse of what happens when a drag reducing solution flows through a pipe. In laminar pipe flow, polymer increases the drag while with turbulent flow the drag is reduced. The result of combining these two systems, that is a sphere suspended in a polymer solution within a cylindrical boundary, was studied by Stow and Elliot⁽³²⁾ in 1970, however, their results did not differ from water, and are questionable because of the experimental method used. More will be said regarding these experiments by Stow and Elliot later in chapter II.

The dilute aqueous polymer solution experiments were therefore conceived to determine what effect a drag reducing solution would have on a suspended sphere within cylindrical boundaries. The behaviour of single spheres fixed to the wall of a pipe, and also capsules moving through pipelines have been studied by other authors. To unify these experiments the behaviour of suspended trains of spheres in pure water was included in this study, although time did not permit the experiments to be extended to polymer solutions. In order to make comparison with others the apparatus and procedure had certain similarities to that of other workers.

II LITERATURE SURVEY

The initial part of this study was to obtain data on the flow of water past spheres and sphere trains in a vertical pipe. The earliest work that is related to this subject was that of McNown and Newlin⁽²⁾ who studied the drag coefficient variation of a sphere rigidly mounted in a tube, as a function of the sphere to tube diameter ratio. Their tests were carried out in air at a fixed Reynolds number and with a uniform velocity distribution across the test section upstream of the sphere, in order to relate their work to the extensive data available on the settling of spheres in an unbounded medium.

As a result of their work they developed the equation for C_d^* in the form;

$$C_d^* = \left[\frac{d/D}{1 - (d/D)^2} \right]^2 \quad (2.1)$$

which neglects the effects of viscosity but still correlates the data for $d/D > .82$ very well.

Closely related to the topic of spheres and sphere trains suspended in pipes is the subject of the transport of capsules through pipelines. An extensive study, ref. (3) to (10), and (20) on the subject of capsule pipelines was published between the years 1963 and 1967. This series began with a consideration of the concept of capsule pipelining and proceeded to develop and test analytical equations for the velocity and pressure gradient of capsules moving through pipelines.

This analysis brought out the importance of several parameters or

groups of parameters in pipeline flow that are similar or closely related to those found in the support of spheres in pipes. For capsule pipelines a dimensional analysis indicates that;

$$V_c/V_{AV} = [R_e, \frac{\sigma - \rho}{\rho}, \frac{d}{D}, \frac{L}{D}, \text{end shape}, C, \frac{k_c}{d}, \frac{k_p}{D}]$$

where

k_c = capsule surface roughness

k_p = pipe surface roughness

C = capsule to pipe friction

These are much the same groups that would be expected to influence the support velocity of a suspended sphere or sphere train. In addition to the above groups, the pipe Froude number $\frac{V_{AV}^2}{Dg}$, which is the ratio of the inertia forces to the gravity forces, could also be considered. While references (3) to (10) and (20) extensively investigated the above parameters it is difficult to relate their work directly to the present study in that they deal chiefly with capsules moving at a velocity in excess of the average fluid velocity, whereas for a suspended sphere the situation is the exact opposite.

The next work to be considered is that which was done by Round and Kruyer⁽²¹⁾, who studied the variation of the drag coefficient and the pressure drop across a sphere as a function of diameter ratio and specific gravity ratio in an inclined tube. It was found that when the quantity

$$\ln(\Delta P_m - \Delta P_L) / [D \sin \theta (\frac{\sigma - \rho}{\rho})]$$

was plotted as a function of $\ln(d/D)$ a straight line resulted.

Furthermore, the drag coefficients obtained by Round and Kruyer⁽²¹⁾ agreed with those of McNown and Newlin despite the differences in the experimental methods. Contrary to what might be expected, a sphere free to move in a fully developed turbulent flow does not exhibit very large drag coefficient differences to that of a rigidly mounted sphere in a uniform flow field. This subject will be further discussed in chapter VII.

References (3) to (10) and (20) and (21) have dealt with the pipeline flow of capsules and the flow around single spheres. The first consideration of flow around trains of spheres not moving with the liquid was done by Tawo⁽²⁸⁾, in his study of the pressure drops across a train of spheres fixed rigidly to the inside of a pipe. Pressure drop measurements were made as a function of diameter ratio and Reynolds number. Tawo also developed two pressure ratio terms by which the sphere train pressure drops can be related to those of the pipe free of the sphere train. These expressions were defined as;

$$PR1 = (\Delta P_S)/L / (\Delta P_L)/L$$

which does not include the end effects, and PR2 defined as;

$$PR2 = (\Delta P_S + \Delta P_E)/L / (\Delta P_S)/L$$

which does take into account the end effects.

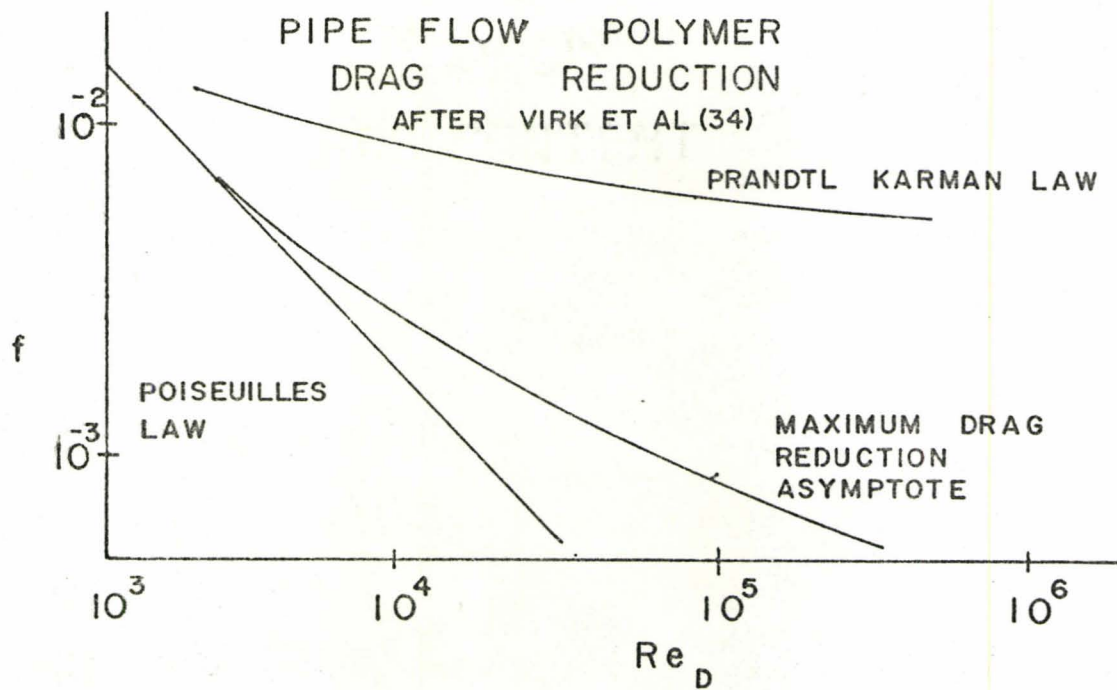
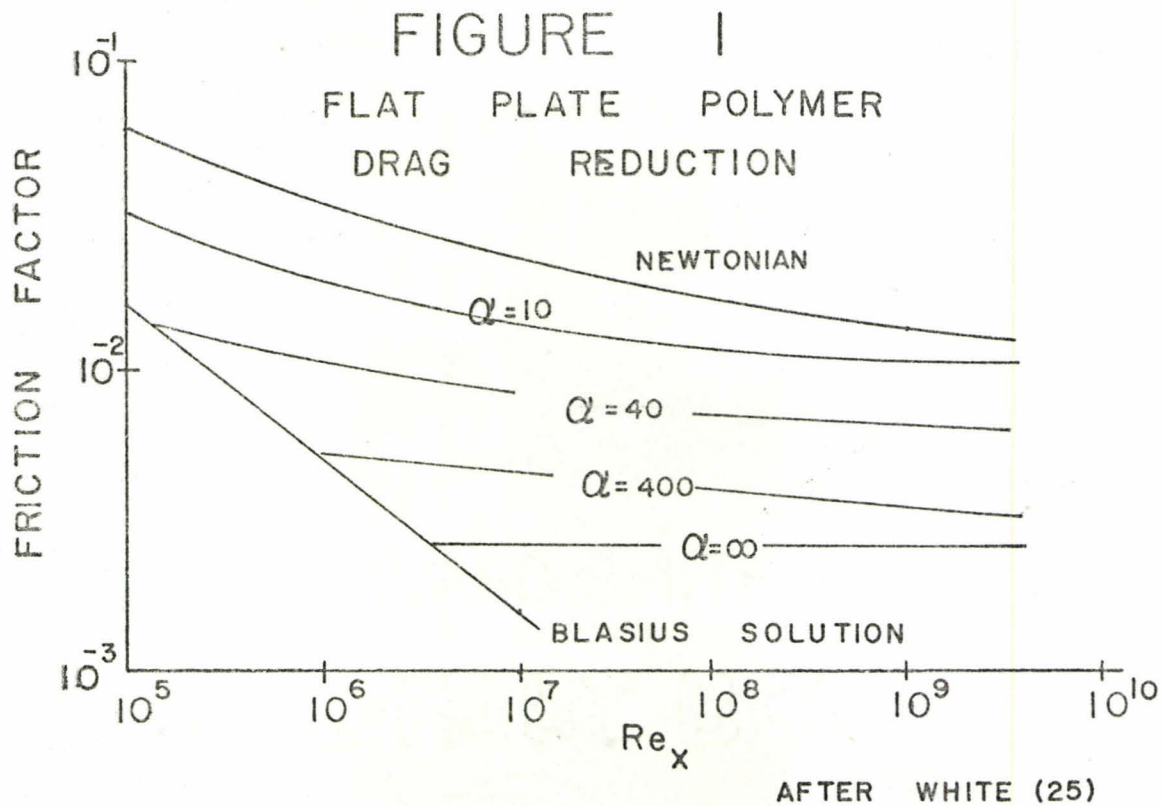
The phenomenon of drag reduction through the addition of trace amounts of long chain polymer molecules to turbulent flow past solid boundaries has been well established for twenty years or more. It has been found that amounts as small as 0.001% by weight or less, can in certain

cases reduce the drag by as much as 70%.

In 1948, B. A. Toms⁽¹⁾ discovered that a solution of polymethyl methacrylate in monochlorobenzene gave drag reductions of up to 50% in turbulent flows through a 0.202 cm. diameter tube. In the ensuing interval the number of papers published on this phenomenon have become too numerous to allow individual mention, however, in general the experimental data fall within the range shown in figure 1. (See also reference (42)).

While experimental data are numerous, a complete explanation of the physical process causing the phenomenon is lacking. It is known that concentrated solutions of polymer are distinctly non-Newtonian, and for certain types of polymers, even dilute solutions exhibit non-Newtonian behaviour, but in general, weak solutions, such as 0.001% by weight, from a viscosity point of view are effectively Newtonian. Experiments by Gadd^{(13), (14)}, and White^{(15), (24)} have shown the polymer solutions have unequal normal stresses, in other words in a simple shear flow pressure does not act equally in all directions. Other experiments have shown that the effect of adding polymer is primarily concentrated in the buffer region, the region extending from $y^+ \approx 11.6$ to $y^+ \approx 70$. It has been observed by Corino and Brodkey⁽²⁶⁾ that the dissipation of energy takes place through the formation of small scale eddies in the region $11.6 < y^+ < 70$ and it has further been observed that the injection of polymer in the region $y^+ > 70$ produces negligible drag reduction until the polymer diffuses to the wall region. The addition of polymer appears to suppress these eddies resulting in a decrease in friction compared to that for a pure solvent.

Partial differential equations describing the momentum transfer of flow through a boundary layer have been developed, but cannot be solved because of their complexity. Existing mathematical solutions generally make use of a similarity variable which reduces the non linear partial differential



equations to ordinary ones. For velocity this new variable depends only on a single position parameter which characterises both distance from the wall and the distance in the direction of the flow. In this way the dimensionless velocity u^+ now depends only on the dimensionless distance y^+ .

Prandtl and von Karman were the first to develop such equations. For the turbulent flow of pure solvent Prandtl has determined a universal velocity defect law;

$$\frac{U - u}{u_{*0}} = \frac{1}{k} \ln \frac{\delta}{y} \quad (2.2)$$

and similarly the universal velocity distribution law;

$$u^+ = \frac{u}{u_{*0}} = \frac{1}{k} \ln \left(\frac{y u_{*0}}{U} \right) - \frac{1}{k} \ln \beta \quad (2.3)$$

for $y^+ = \frac{y u_{*0}}{U} > 11.6$

for $y^+ < 11.6$ $\frac{u}{u_{*0}} = \frac{y u_{*0}}{U}$ (2.4)

Equation 2.3 can be converted to a form containing the friction factor by letting;

$$C_f = \frac{8\tau_0}{\rho U^2} = 8 \left(\frac{u_{*0}}{U} \right)^2$$

therefore

$$\frac{1}{\sqrt{C_f}} = 0.868 \ln (\text{Re} \sqrt{C_f}) - 0.8 \quad (2.5)$$

The work of many authors has been directed towards obtaining an equation similar to equation 2.5, that is applicable to drag reducing solutions. It can be expected that equation 2.5 for a solvent must form the lower asymptote of drag reduction. Virk et. al.⁽³⁴⁾, have deduced the upper asymptote of drag reduction as;

$$\frac{1}{\sqrt{C_f}} = 4.125 \ln (\text{Re} \sqrt{C_f}) - 16.2 \quad (2.6)$$

Relationships such as the above must be used with caution, because for polymer flows the extent of drag reduction depends upon the thickness of the shear layer. If the shear layer is too thin, as in a pipe of very small diameter, the viscous sublayer and the interactive, or buffer layer remain, but the turbulent portion of the shear layer is either greatly reduced or non existent, and hence the flow becomes that for maximum drag reduction very easily. The result is that greater drag reduction is apparent at lower Reynolds numbers and lower concentrations of polymers than would normally occur where the shear layer is sufficiently thick.

Granville^{(19), (35)} has investigated the limitations of similarity law type solutions applied to polymer flows, and bearing these in mind, several such solutions will be discussed briefly. F. M. White⁽²⁵⁾ combined the law of the wall developed by Meyer for polymer flows;

$$u^+ = \frac{1}{k} \ln y^+ + 5.5 + \alpha \ln \left(\frac{u^+}{u_{*0}'} \right) \quad (2.7)$$

where α is a property of the polymer and its concentration and u_{*0}' is a threshold friction velocity below which the flow behaves as a pure solvent would, with the two dimensional boundary layer equations to derive an

effective Reynolds number relationship for external flows;

$$R_{eN} \cong R_{eX} \left(\frac{u_*}{u_{*0}} \right)^{k\alpha} \quad (2.8)$$

The Reynolds number of the Newtonian fluid is calculated as before but it is then modified according to equation 2.8. Using this effective Reynolds number the friction factor can then be calculated from some Newtonian correlation such as;

$$C_f \text{ (NEWTONIAN)} = [2 \log (R_{eN}) - 0.65]^{-2.3}$$

Since the free stream velocity for a flat plate remains constant, the shear stress must decrease as the Reynolds number increases. Therefore, the term $u_* = \sqrt{\frac{\tau}{\rho}}$ must also decrease as the Reynolds number increases. The result is that for a flat plate, polymer addition reduces friction, starting at the threshold Reynolds number but proceeding with decreasing effectiveness as the Reynolds number increases.

Apart from Meyer, there have been many authors who have studied the similarity laws applicable to polymer flows, both theoretically, and experimentally. Granville^{(19), (35)} has published an interesting derivation of these similarity laws, along with a summary of their limitations.

Granville begins his analysis with a statement of the inner velocity law;

$$u = [\tau_0, \rho, \mu_0, y, \rho_p, l, l_1, l_2 \dots, \\ m, m_1, m_2, \dots, t, t_1, t_2, \dots.]$$

with the boundary conditions;

$$u = 0 \text{ at } y = 0$$

The variables are then grouped by a dimensional analysis and by considering the region of overlap between the outer velocity law and the inner velocity law, a functional form of the inner velocity law has been derived;

$$\frac{u}{u_*} = A \ln y^+ + B_1[\ell^*, C, P] \quad (2.9)$$

where

$$\ell^* = \frac{u_* \ell}{u_0}$$

is a non dimensional characteristic polymer length, and;

$$C = \left[\frac{\rho_p / \rho}{1 + \rho_p / \rho} \right]$$

ρ_p = polymer concentration (density units)

ρ = density of solvent

is a form of polymer concentration, where;

$$P = \frac{\ell}{\ell_1}, \frac{\ell_1}{\ell_2}, \dots, \frac{m}{\rho_0 \ell^3}, \frac{m}{m_1}, \frac{m_1}{m_2}, \dots$$

$$\frac{t u_0}{\ell^2}, \frac{t}{t_1}, \frac{t_1}{t_2}, \dots$$

These relationships indicate what the similarity laws for polymer must be like, unfortunately the exact form can only be determined by experiment.

While considerable data exists on the unhindered settling of spheres in air or water, the subject of unhindered settling in polymer has only recently been studied. In 1967, White⁽²⁴⁾ showed that the addition of polymer to the flow past a sphere in an unbounded medium caused the drag coefficient to decrease when the boundary layer was laminar and increase when it was turbulent.

This observation is somewhat unexpected because for internal flows in the laminar region the addition of polymer slightly increases the drag while in the turbulent region it produces a marked decrease in drag. White has attributed this occurrence in external flows to the delayed separation of the laminar boundary layer and a subsequent decrease in wake diameter. He postulated that the delay in separation is caused by the inequality of normal stresses in the shear flow, resulting in a higher pressure normal to the direction of shear than would be found in a flow of the pure solvent. This would then cause the boundary layer to adhere to the sphere longer than usual. The inequality of normal stresses was first suggested by Gadd⁽¹³⁾,⁽¹⁴⁾ and demonstrated by him by the impact of a free jet on an inclined plane.

In 1967, Chenard⁽¹⁶⁾ published a thesis reporting essentially the same results as White⁽²⁴⁾, however, when these results are compared with those of McNown and Newlin⁽²⁾ and others who did work on the flow around spheres in tubes, it can be seen that Chenard's drag coefficients should differ by as much as +10 to +15% when compared to those in a truly unbounded medium.

The final paper of immediate interest is one by Stow and Elliot⁽³²⁾ reporting their work on the measurement of drag forces and hence drag

coefficients on a tethered sphere in a polymer solution. The results they obtained indicates that the drag coefficient is not altered by the addition of polymer to the solvent. This disagrees with the results of the present study which indicates that the drag coefficient increases.

An examination of their experimental method suggests a possible explanation. The polymer used was Polyox WSR 301, a polymer that is highly susceptible to shear degradation, and rather than using an open circuit system they used a closed circuit in which the polymer was continually recirculated using a centrifugal pump. To obtain results at different concentrations this original polymer was then diluted. Because of the sensitivity of Polyox to shear degradation it is probable that over the period of the experiment the actual concentration was not accurately known and the polymer was totally degraded.

III THEORY

Referring to figure 2, when the sphere(s) are in stable equilibrium their weight is balanced by their buoyancy and the drag force exerted on them by the fluid. Assuming fully developed turbulent flow upstream of the spheres and neglecting the exact location or motion of the spheres, a drag coefficient can be postulated that encompasses all the effects encountered, and can be distinguished from the drag coefficient occurring in an unhindered configuration.

For the spheres at equilibrium we may write the force balance as, (referring to figure 2).

$$F_3 = F_1 + F_2$$

or

$$W = C_d^* \frac{A_S \rho V_{AV}^2}{2g_c} + n U_S \rho \frac{g}{g_c}$$

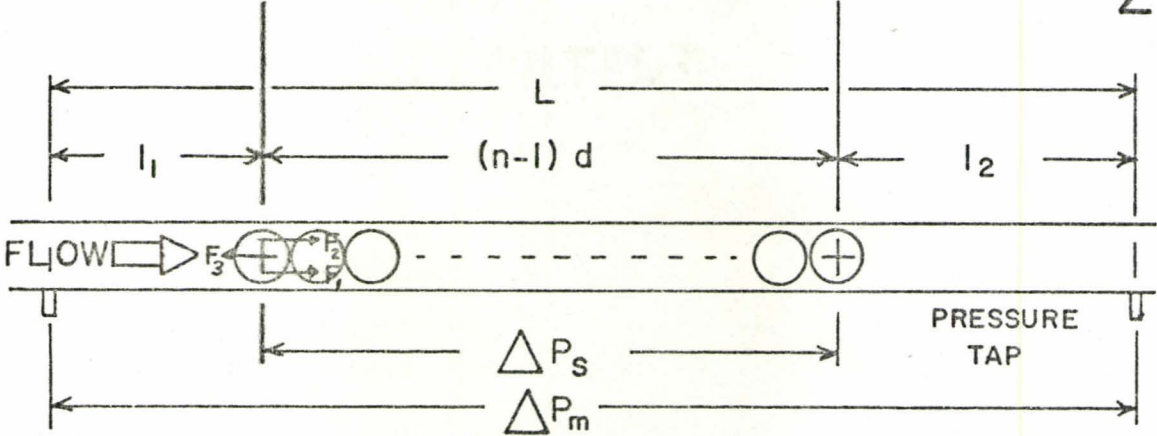
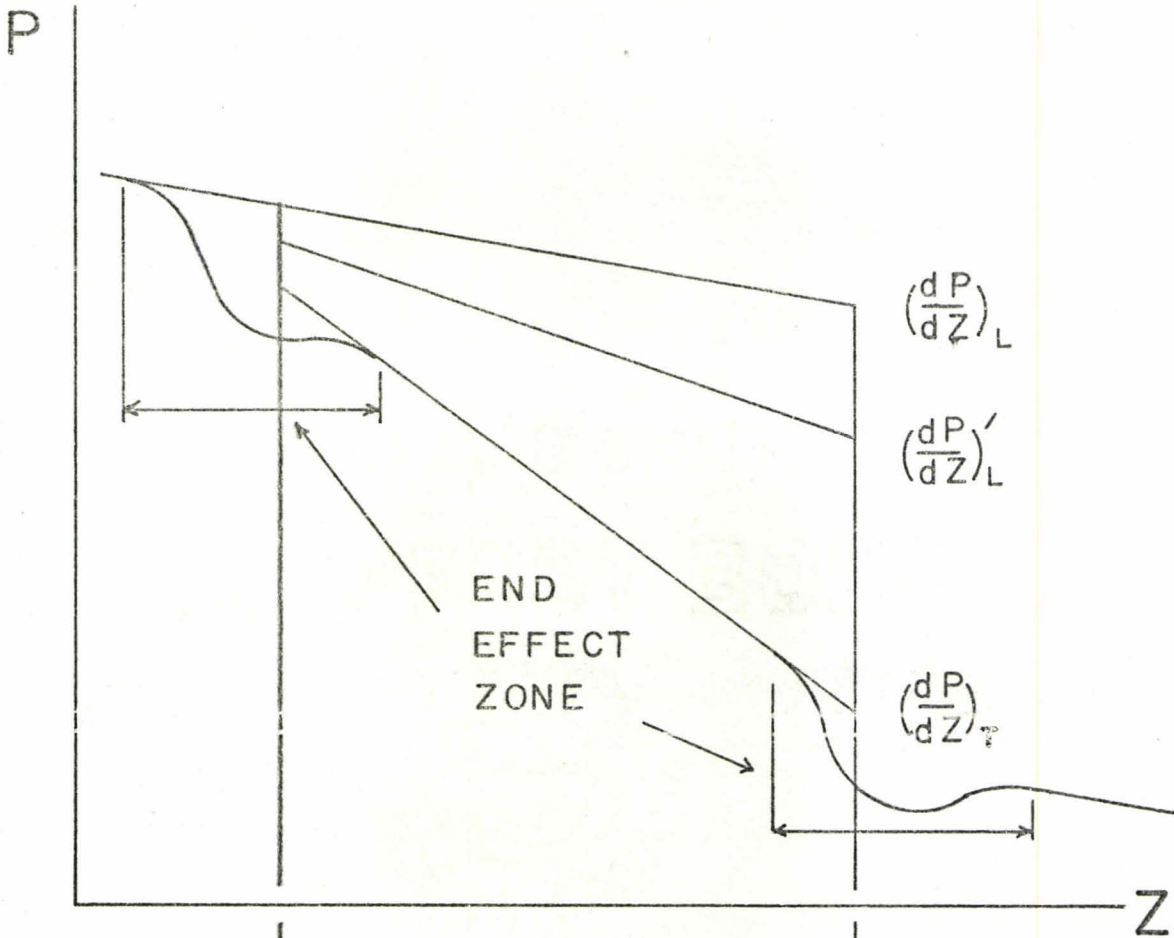
therefore

$$\frac{n \pi d^3}{6} \sigma \frac{g}{g_c} = C_d^* \frac{\pi d^2}{4} \rho \frac{V_{AV}^2}{2g_c} + \frac{n \pi d^3}{6} \rho \frac{g}{g_c}$$

collecting terms and transposing we have,

$$\frac{C_d^*}{n} = \frac{4}{3} \left(\frac{\sigma - \rho}{\rho} \right) \frac{gd}{V_{AV}^2} \quad (3.1)$$

FIGURE 2



$F_3 =$ WEIGHT
 $F_2 =$ BUOYANCY
 $F_1 =$ DRAG

Hence for a given fluid and sphere material

$$\frac{C_d^*}{n} \propto \frac{gd}{V_{AV}^2} \quad (3.2)$$

In order to understand better the phenomenon and how the variables relate to each other, a dimensional analysis, using Buckingham's π theorem has been performed for the system.

It may be assumed that the variables involved may be written:

$$\Delta P = f(d, D, \rho, \sigma, \nu, V_{AV}, g_c) \quad (3.3)$$

The units are;

$$\Delta P = FL^{-2}$$

$$d = L$$

$$D = L$$

$$\rho = ML^{-3}$$

$$\sigma = ML^{-3}$$

$$\nu = L^2T^{-1}$$

$$V_{AV} = L^2T^{-1}$$

$$g_c = MLF^{-1}T^{-2}$$

Arranging these into four dimensionless groups;

$$\pi_1 = V_{AV}^a D^b \rho^c g_c^d \Delta P$$

$$\pi_2 = V_{AV}^a D^b \rho^c g_c^d d$$

$$\pi_3 = V_{AV}^a D^b \rho^c g_c^d \sigma$$

$$\pi_4 = V_{AV}^a D^b \rho^c g_c^d \nu$$

By satisfying the requirement of dimensional homogeneity for each π group we can solve for a, b, c and d. Hence;

$$\pi_1 = \frac{\Delta P g_c}{V_{AV}^2 \rho} \quad (3.4)$$

which can be rearranged without altering the requirement of dimensional homogeneity into a friction factor type of term;

$$\pi_1 = \frac{\Delta P}{\left(\frac{L}{D}\right) \frac{\rho V^2}{2g_c}} = C_f \quad (3.5)$$

and $\pi_2 = d/D \quad (3.6)$

$$\pi_3 = \frac{\sigma}{\rho} \text{ or } \frac{\sigma - \rho}{\rho} \quad (3.7)$$

and $\pi_4 = \frac{\nu}{V_{AV} D} \text{ or } \pi_4 = \frac{V_{AV} D}{\nu} = R_e \quad (3.8)$

We can then write that;

$$f(C_f, d/D, \frac{\sigma - \rho}{\rho}, R_e) = 0 \quad (3.9)$$

Referring back to the derivation of the drag coefficient C_d^* the RHS of equation 3.2 is a form of the Froude number, that is, the ratio of the gravity forces to inertia forces. Two other quantities not considered in the dimensional analysis but which should be included are the number of spheres in the train, and their location in the pipe. Considering the geometry of the test section in cylindrical polar co-ordinates centered on the centerline of the pipe, and letting the eccentricity be represented by the radius vector stretching from the origin to the center of the sphere, it is apparent that for an oscillating sphere or sphere train the time average of the eccentricity will be some finite value.

The resulting effect is a buffeting of the spheres, which is caused by the turbulence inherent in the flow, and the shedding of vortices from the spheres. Above certain limiting diameter ratios, $d/D > 0.75$ the manner in which the wake vortices are produced is altered, causing the sphere to spin or roll rapidly about the inside of the test section. The combination of these effects then renders the concept of a stable symmetrically located sphere invalid. However, since the theory is not dependant upon the spheres being centered but is sufficiently general to encompass these effects the numerical values should be generally valid for all systems where spheres are hydrodynamically supported within a vertical pipe.

Returning to the system of figure 2, the pressure drop across the sphere or spheres will in general consist of four quantities.

- (1) The pressure drop ΔP_T associated with the support of the sphere or sphere train, and caused by a combination of form drag and skin friction acting on the spheres only.

- (2) The pressure drop ΔP_L caused by the friction between the pipe and fluid, flowing at the velocity required to suspend the spheres.
- (3) A pressure drop $\Delta P_L'$ due to the additional shear imposed on the flow by the presence of the sphere, over and above ΔP_L due to the friction between the walls and the fluid in the absence of the sphere.
- (4) Leading and trailing end effects of the sphere(s) ΔP_{E1} , and ΔP_{E2} ;
 $\Delta P_E = \Delta P_{E1} + \Delta P_{E2}$.

The pressure ΔP_m is measured at the positions along the tube where the end effects caused by the spheres are negligible, and consists of;

$$\Delta P_m = \Delta P_L + \Delta P_T + \Delta P_L' + \Delta P_E \quad (3.10)$$

The term ΔP_E in the above equation represents the end effect pressure drops of the leading and trailing ends of the sphere train. These quantities can only be obtained empirically because of the complex nature of the flow. The flow being turbulent results in a continual buffeting of the spheres, furthermore, vortices are being shed from the trailing end of the sphere train.

An expression ΔP_S can be defined if the constant pressure gradient terms of the total gradient along the section $(n - 1)d$ of the sphere train (see figure 2), are considered. The total pressure gradient is not constant along this entire section, however the deviation from constancy at the beginning and end of the sphere train is included in the end effects. ΔP_S then is,

$$\Delta P_S = \left[\left(\frac{dP}{dZ} \right)_T + \left(\frac{dP}{dZ} \right)_L + \left(\frac{dP}{dZ} \right)_L' \right] (n - 1)d \quad (3.11)$$

$(n - 1)d$ is used rather than nd for the train length because this provides a more realistic approach to the problem of allowing for end effects.

The measured pressure can then be written as;

$$\Delta P_m = \Delta P_S + (\Delta P_{E1} + \Delta P_{E2}) + \left(\frac{dP}{dZ}\right)_L (\ell_1 + \ell_2) \quad (3.12)$$

where

$$L = (n - 1)d + \ell_1 + \ell_2$$

Substituting for ΔP_S ;

$$\begin{aligned} \Delta P_m = & \left[\left(\frac{dP}{dZ}\right)_T + \left(\frac{dP}{dZ}\right)_L + \left(\frac{dP}{dZ}\right)_L' \right] (n - 1)d + (\Delta P_{E1} + \Delta P_{E2}) \\ & + \left(\frac{dP}{dZ}\right)_L (\ell_1 + \ell_2) \end{aligned}$$

and grouping the terms we have;

$$\begin{aligned} \Delta P_m = & \left[\left(\frac{dP}{dZ}\right)_T (n - 1)d + \left(\frac{dP}{dZ}\right)_L' (n - 1)d \right] \\ & + \left(\frac{dP}{dZ}\right)_L [(n - 1)d + \ell_1 + \ell_2] + \Delta P_{E1} + \Delta P_{E2} \end{aligned} \quad (3.13)$$

The quantity $(dP/dZ)_L'$ cannot be measured independantly of the term $(dP/dZ)_T$, therefore they have been combined into the single term $(\Delta P_S/L)$. Therefore,

$$\Delta P_m = \left(\frac{\Delta P_S}{L}\right) (n - 1)d + \left(\frac{\Delta P_L}{L}\right) (L) + \Delta P_E \quad (3.14)$$

and transposing we have;

$$\Delta P_m - \Delta P_L = \left(\frac{\Delta P_S}{L}\right) (n - 1)d + \Delta P_E \quad (3.15)$$

Once a section of developed flow has been achieved along the sphere train, it shall be assumed that regardless of the length of the train, the end effects remain constant. It is then a simple matter to determine $(\Delta P_S/L)$ from a graph of $\Delta P_m - \Delta P_L$ against n , and from these to determine ΔP_E .

Tawo⁽²⁸⁾ in his thesis on fluid flow in pipes containing sphere trains, has developed a pressure ratio PR1, which compared the pressure gradient in a tube containing a sphere train to that of a free tube. Such a ratio could be used to predict the pressure gradient in a pipe containing a sphere train if the pressure gradient of the free tube is known. The pressure ratio PR1, is defined as;

$$PR1 = (P_{1n} - P_{2n})/L \bigg/ (dP/dZ)_L$$

where $(P_{1n} - P_{2n})/L$ is the pressure gradient along the train, excluding end effects.

For the purpose of comparison, an expression similar to PR1 will be developed in the present work. From equation (3.12);

$$\Delta P_S = \Delta P_m - \Delta P_E - \left(\frac{dP}{dZ}\right)_L [L - (n - 1)d] \quad (3.16)$$

the gradient then is;

$$\frac{\Delta P_S}{(n - 1)d} = \frac{\Delta P_m}{(n - 1)d} - \frac{\Delta P_E}{(n - 1)d} - \left(\frac{dP}{dZ}\right)_L \left[\frac{L - (n - 1)d}{(n - 1)d}\right] \quad (3.17)$$

defining;

$$PR1 = \left[\frac{\Delta P_S}{(n-1)d} \right] / \left(\frac{dP}{dZ} \right)_L \quad (3.18)$$

and substituting, we have;

$$PR1 = \frac{\Delta P_m}{(n-1)d} - \frac{\Delta P_E}{(n-1)d} - \left(\frac{\Delta P_L}{L} \right) \left[\frac{L - (n-1)d}{(n-1)d} \right]$$

On collecting the terms together we have;

$$PR1 = 1 + \frac{L}{(n-1)d} \left[\frac{\Delta P_m}{\Delta P_L} - \frac{\Delta P_E}{\Delta P_L} - 1 \right] \quad (3.19)$$

Once a graph of $\Delta P_m - \Delta P_L$ has been plotted and ΔP_E is known, equation (3.19) can be used to calculate PR1, however, should ΔP_E not be known, a close approximation to PR1 can be made if ΔP_E is included in ΔP_m , this would then make,

$$PR1 = 1 + \frac{L}{nd} \left[\frac{\Delta P_m}{\Delta P_L} - 1 \right] \quad (3.20)$$

where $(n-1)d$ has been changed to nd to facilitate calculation.

A major portion of the experiments presented in this work deal with the effects of polymer on single spheres dynamically suspended in a vertical pipe. For these situations a developed $(dP/dZ)_T$ cannot exist, since a single sphere does not provide sufficient length in the direction of flow. Furthermore, the pressure drop across the single sphere is not equivalent to the end effects observed for the sphere trains, since these effects may extend for several diameters along the sphere train.

When dealing with polymer it is assumed that low solution concentrations (< 100 Wppm) produce solutions that are equivalent to Newtonian fluids, except that they produce less drag.

For unbounded external flows, such as flows around a sphere White⁽¹⁵⁾, (24) and Chenard⁽¹⁶⁾ have observed that the addition of polymer causes the drag coefficient in the laminar region to decrease, and in the turbulent region to increase; however for confined flows, that is where a sphere is suspended within a tube, the effect on the drag coefficient cannot be predicted. For these reasons the results of the polymer experiments were not compared with theory, but rather simply with the results of the water experiments.

IV EXPERIMENTAL APPARATUS

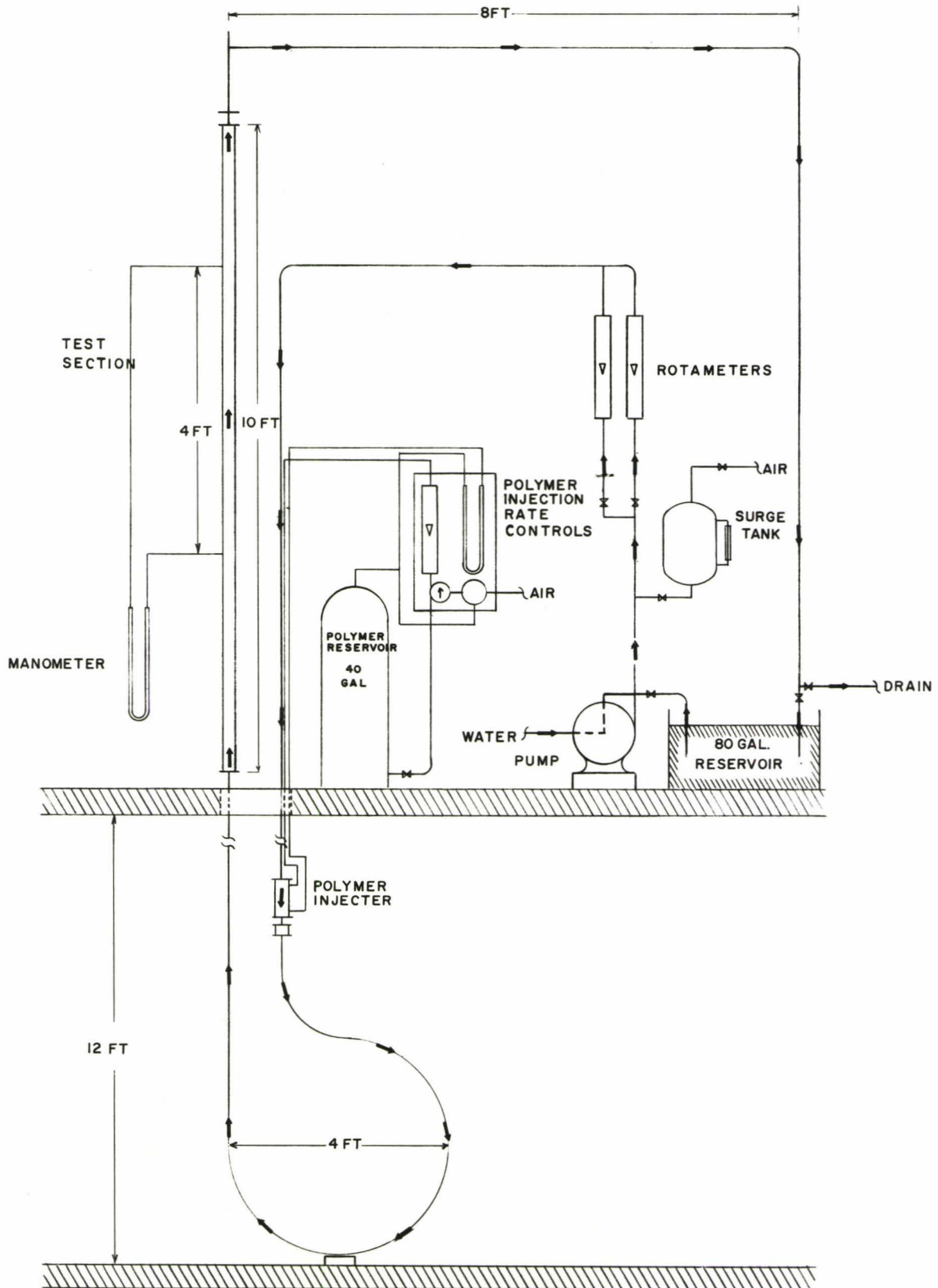
IV-1 The Flow System

The experimental apparatus consists of a vertical loop of 2" ID pipe approximately eighty feet in length, assembled as shown in figure 3. The fluid is circulated using a Worthington model 2CN-32 single stage centrifugal pump powered by a General Electric three horsepower 3600 RPM induction motor.

(Since the system can be, but is generally not intended to be used as a recirculating system, two sources of water have been used; the city mains for open circuit flow, and an eighty gallon reservoir for recirculating flow.)

Upon being discharged from the pump the water travels past a 904 cubic inch variable volume surge chamber, which dampens pressure fluctuations. Immediately after the surge tank are located two "Brooks" rotameter type flowmeters. The rotameters are installed in such a manner that the flow can be directed through either one, independent of the other. During the course of the experiments it was found that the original two rotameters did not adequately cover the entire flow range, and for this reason one of the existing rotameters was replaced by a third low flow rate rotameter.

After leaving the rotameters the flow passed along the pipework down to the level of the first floor, then back through a vertical section twenty feet long, to the second floor. The last ten feet of this vertical section is a glass tube which was used as a test section. A fine honeycomb filter is located at the entrance to the test section to homogenize and reduce the turbulence. Two ports for inserting the spheres were located



Apparatus Schematic

immediately above the test section.

A number of pressure taps are located along the entire length of the metal pipe below the test section, while the initial test section had pressure taps located twelve inches apart along its entire length. Two later versions of the test section, on which the majority of the tests were performed had pressure taps on the midsection, located four feet (five feet for the second one) apart.

Because the glass test section was extremely fragile, and subject to considerable mechanical and thermally induced stresses it was necessary to brace it at 2.5 foot intervals using rubber lined clamps. It was also necessary to isolate the tube at the bottom flange by a thick rubber gasket and at the top by a flexible tygon bellows piece to prevent the tube from breaking.

After leaving the test section the water passed along pipework into either the reservoir or the drains, depending upon the requirement. In order to recover the single spheres a gate valve was located in the vertical section above the reservoir, which when opened allowed the water and the sphere to be pumped into the reservoir. The trains of spheres were retrieved by hooking a metal eye located at the end of the train.

IV-2 The Polymer System

The circulation system used throughout these experiments was an open circuit system. This was done because in a recirculating system polymer rapidly becomes mechanically degraded.

The polymer injection apparatus consisted of a 40 gallon reservoir which held the concentrated aqueous polymer solution (2000 Wppm). The polymer from this reservoir was injected into the main stream using compressed air, controlled by a precision air line regulator, while the

injection rate was monitored using a "Brooks" flowmeter.

The polymer was injected into the flow of the main stream through a chamber located approximately thirty feet upstream of the test section. Immediately following this injection chamber was a turbulence promoter in the form of a centrally located sphere, occupying approximately 50% of the area of the pipe. It was expected that this sphere combined with the existing turbulence in the interval between the turbulence promoter and the test section would provide sufficient agitation to uniformly distribute the polymer throughout the flow. Visual inspection of poorly mixed polymer batches passing through the test section confirmed this.

During the course of the experiments it was found to be difficult to maintain a steady flow of polymer because of fluctuating main line pressures. Consequently, the system was modified to incorporate a differential manometer which measured the pressure difference between the air space above the polymer in the reservoir and the pressure in the injection chamber. This permitted continuous monitoring of the "driving" pressure and thus better control over the injection rate.

Preparation of the stock solution of polymer took place in plastic lined bins, using a "Hercules Standard Eductor" (manufactured by Hercules Inc.). The solution was later transferred to the reservoir using a hand operated positive displacement pump, which reduced polymer degradation in transfer, and permitted inspection of the batches to check for evidence of poor mixing.

IV-3 The Pressure Measuring System

Two manometer arrangements were used to measure the pressures during these experiments. The first method used a bank of inclined manometers to check the pressure gradient along the glass section of the pipe and

enabled the selection of the actual test section. The second arrangement used a single inclined manometer which was used to measure the pressure drops across the test section with and without the spheres.

Because of the short test section (four to five feet) and the relatively low velocities encountered in the experiments a very accurate device was required to measure the pressure. The manometer eventually used was a water jacketed carbon tetrachloride-in-glass inclined U tube manometer. (see figure 26 and plate 4). The manometer could be inclined from 6° to 30° from the horizontal, and was provided with a level to measure the angle of inclination. It was found that because of the temperature difference between the test section and the manometer that an apparent manometer reading was created when there was no flow through the test section. To minimize this reading the entire thirty inches of each manometer leg, as well as the connecting tubes were enclosed in a water jacket.

IV-4 The Spheres

The steel and plastic spheres used in this study had specific gravities of approximately 8.1, and 1.1 respectively.*

During the tests they were hydrodynamically suspended in four configurations eg.

- (i) single spheres,
- (ii) unattached sphere trains,
- (iii) flexibly attached sphere trains, and
- (iv) rigidly attached sphere trains.

For cases (iii) and (iv), the spheres were drilled and connecting hooks fitted into the cavities. The change in specific gravity caused by the installation of these devices was negligible.

* For exact value see Appendix VII - Data Tables.

V EXPERIMENTAL PROCEDURE

V-1 Tests Using Water Only

Experiments using water as the working fluid were carried out using all the sphere configurations, eg. single spheres, non attached sphere trains, flexibly attached trains, and rigidly attached trains. The resulting data had two fold value in that it provided data that could be compared to that of other experimenters as well as providing original data, as in the case of the sphere trains.

The procedure for single spheres and trains of spheres was similar. The flow of water would be started at least several hours prior to the actual testing to allow the temperature of the water and that of the apparatus in general to stabilize. When the apparatus was at thermal equilibrium the flow was stopped and the manometer no flow reading, as well as the water and room temperature recorded. The flow was then restarted and adjusted to stabilize the spheres in the center of the test section. When it was evident that the spheres were stable the flowrate and pressure drop, in addition to the mode of oscillation of the spheres, was recorded and the flow shut off and again the no flow manometer reading noted. This procedure was repeated for all the different diameters of steel and plastic spheres available. The diameter and weight of the spheres was also measured and recorded.

For the case of the steel sphere trains only one diameter ratio was comprehensively investigated because of the violent motion of the steel spheres. The rotating steel spheres had sufficient momentum to cause the test section to vibrate very violently which sometimes resulted in the spheres striking the inside entrance to a pressure tap. On one occasion the steel spheres actually broke

the test section, and after this the testing of steel sphere trains was discontinued.

V-2 Polymer Tests

The polymer experiments were carried out in much the same manner as those involving water, however, they were performed on single steel spheres only. Again the water flow was started and the water and apparatus allowed to come to thermal equilibrium. The flow of water was then stopped and the manometer zero reading as well as the water and room temperature recorded, and a sphere then inserted into the tube. The water flow was then restarted to raise the sphere to the center of the test section. When the system had stabilized the polymer injection was commenced and the appropriate concentration established in the test section. During the experiments requiring polymer additions it was required that the flowrates be carefully manipulated to maintain both the sphere in the center of the test section, and the required polymer concentration. When it was apparent that the sphere was stationary in the direction of the flow, the flowrates and pressure drops were noted. The foregoing procedure was repeated for concentrations of 25 Wppm and 50 Wppm. After the 50 Wppm tests the spheres were removed, and the system flushed for several minutes.

As a check, all the readings were repeated at least twice.



Plate #1 Overall view of apparatus, second floor

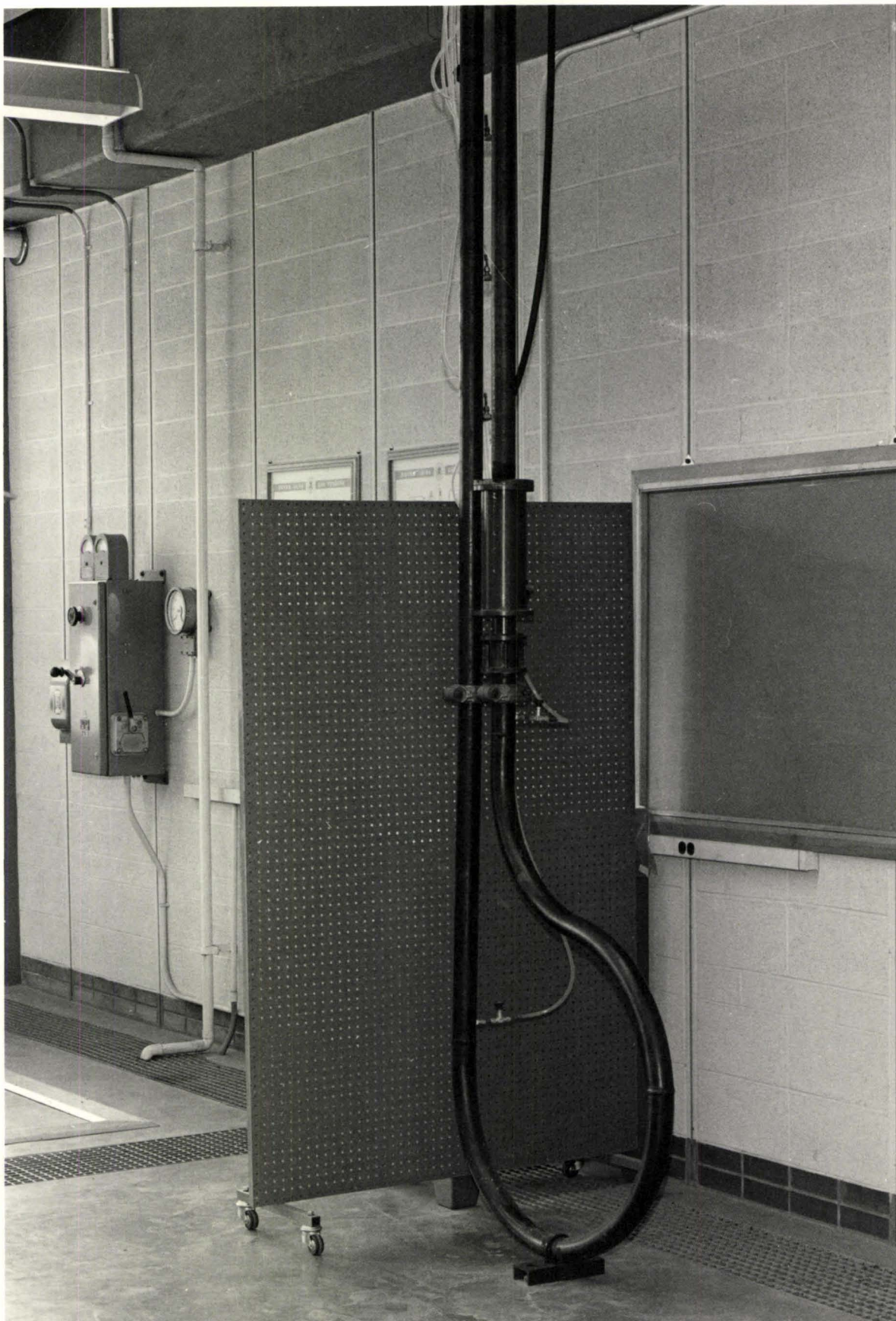


Plate #2 Apparatus on first floor, showing injection chamber and turbulence promoter



Plate #3 Polymer injector controls and flowmeter

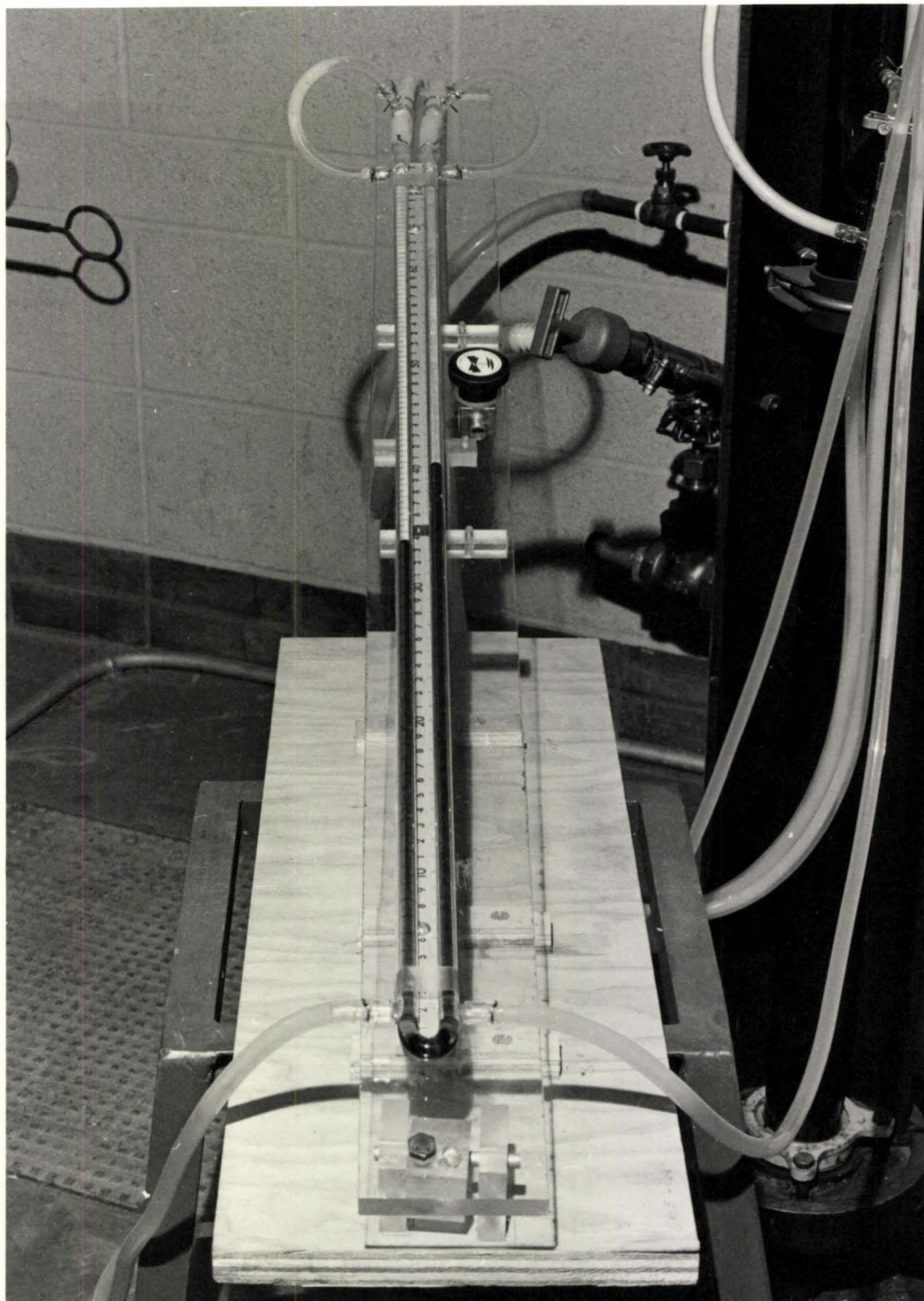


Plate #4 Water jacketed carbon tetrachloride in glass manometer, used for most measurements

SECTION VI
RESULTS

The graphs displayed in this section are based upon the measured data presented in tabular form in Appendix VII.

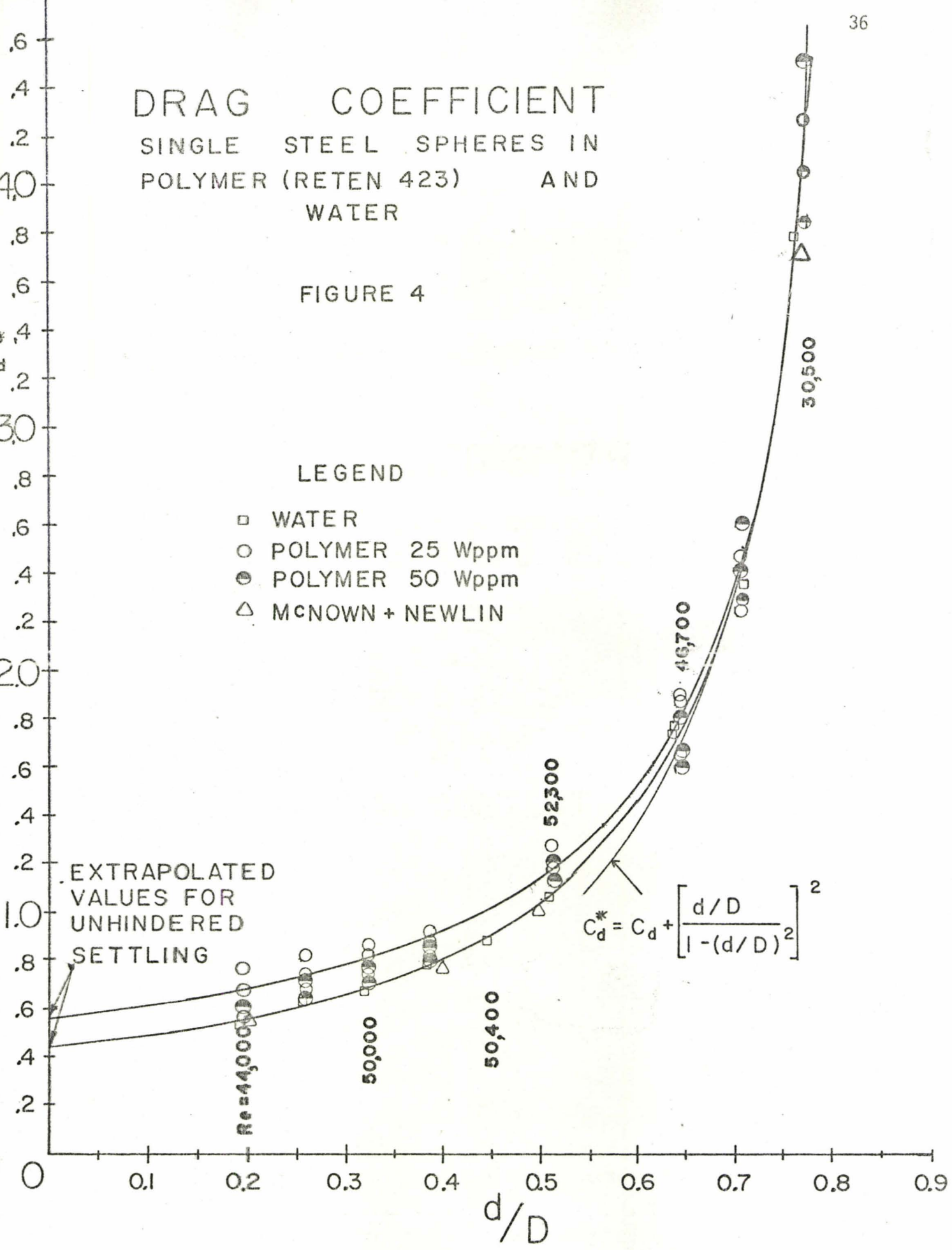
DRAG COEFFICIENT

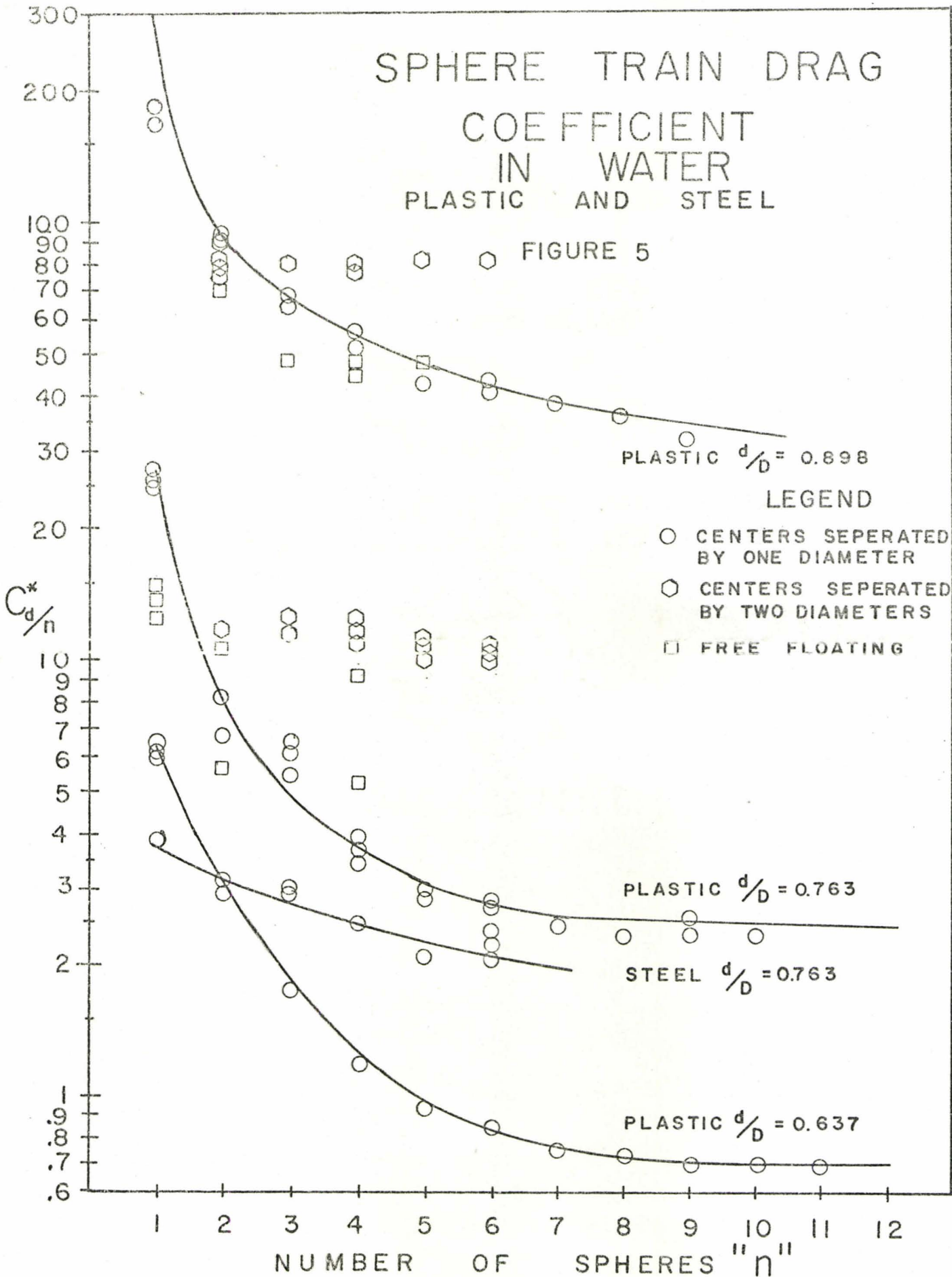
SINGLE STEEL SPHERES IN
POLYMER (RETEN 423) AND
WATER

FIGURE 4

LEGEND

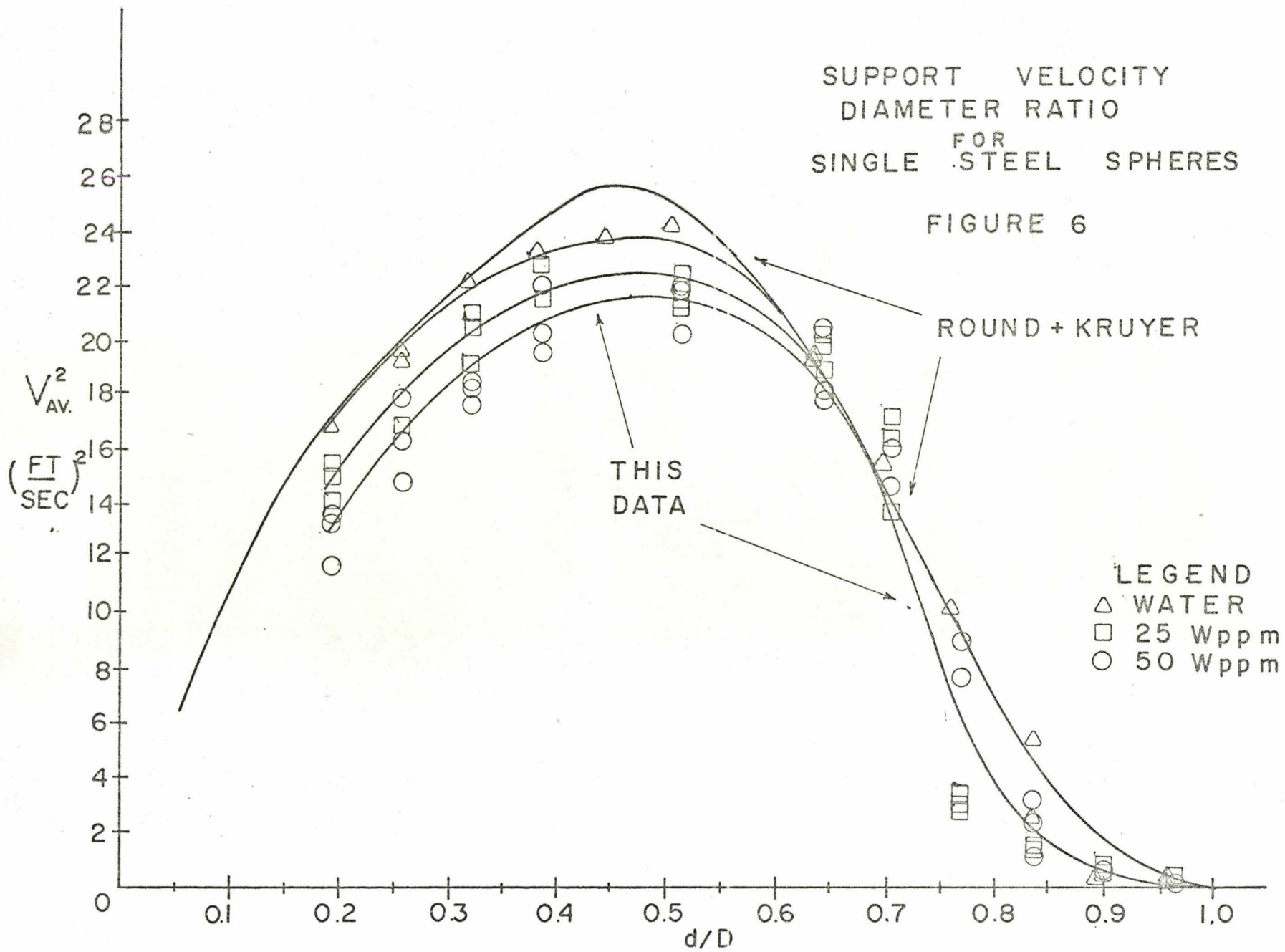
- WATER
- POLYMER 25 Wppm
- POLYMER 50 Wppm
- △ MCNOWN + NEWLIN





SUPPORT VELOCITY
DIAMETER RATIO
FOR
SINGLE STEEL SPHERES

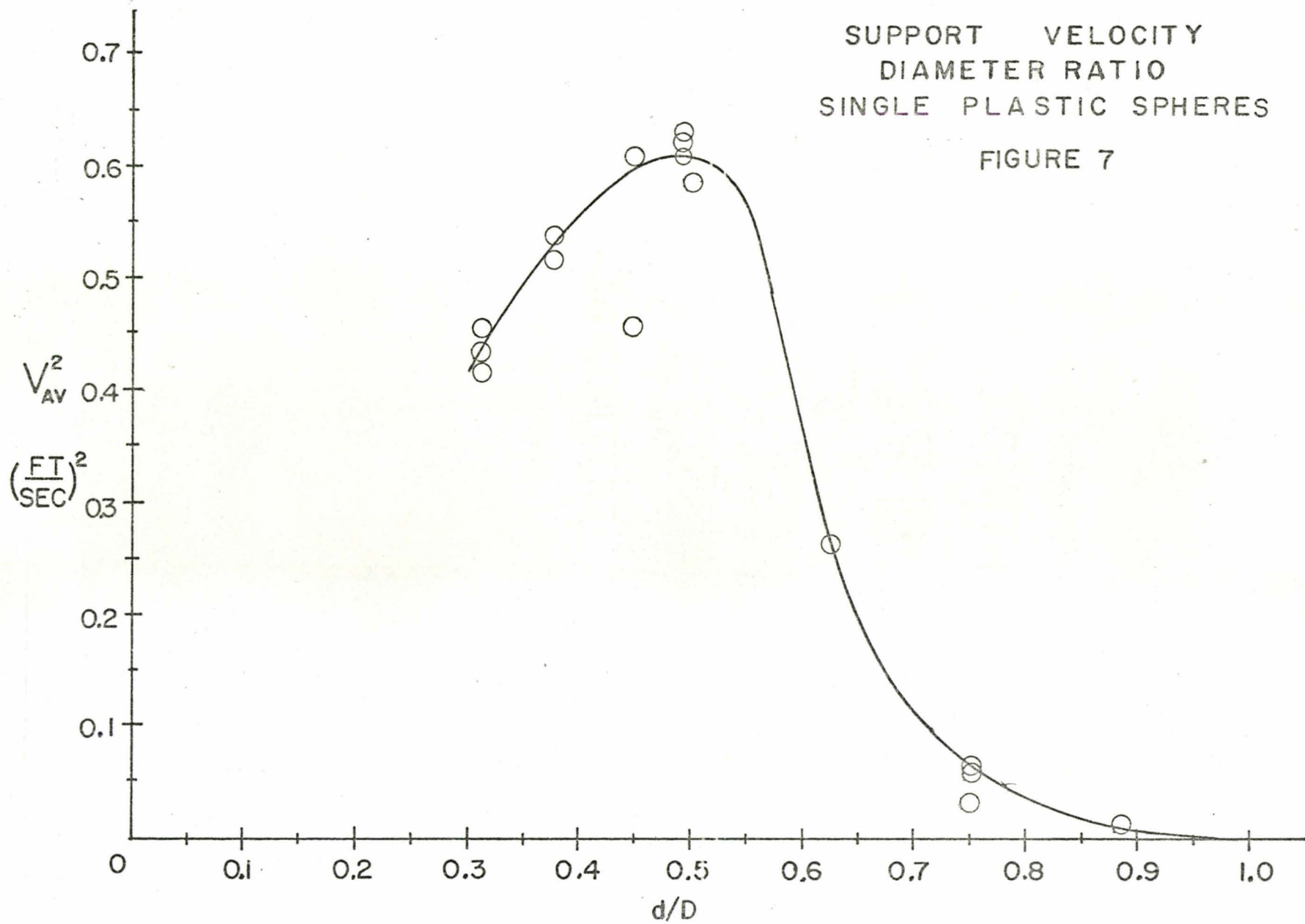
FIGURE 6



LEGEND
 Δ WATER
 \square 25 Wppm
 \circ 50 Wppm

SUPPORT VELOCITY
DIAMETER RATIO
SINGLE PLASTIC SPHERES

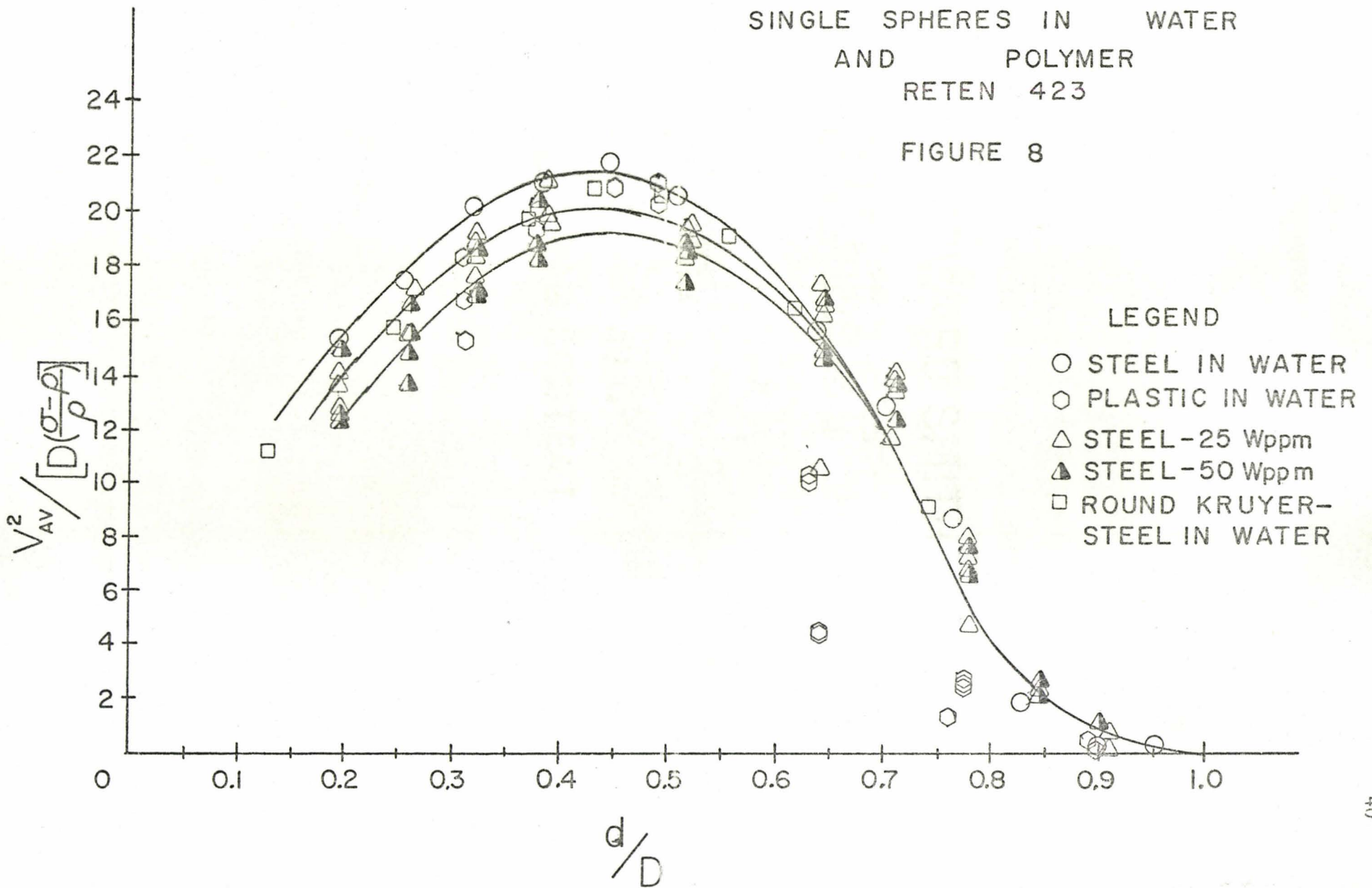
FIGURE 7



SUPPORT VELOCITY

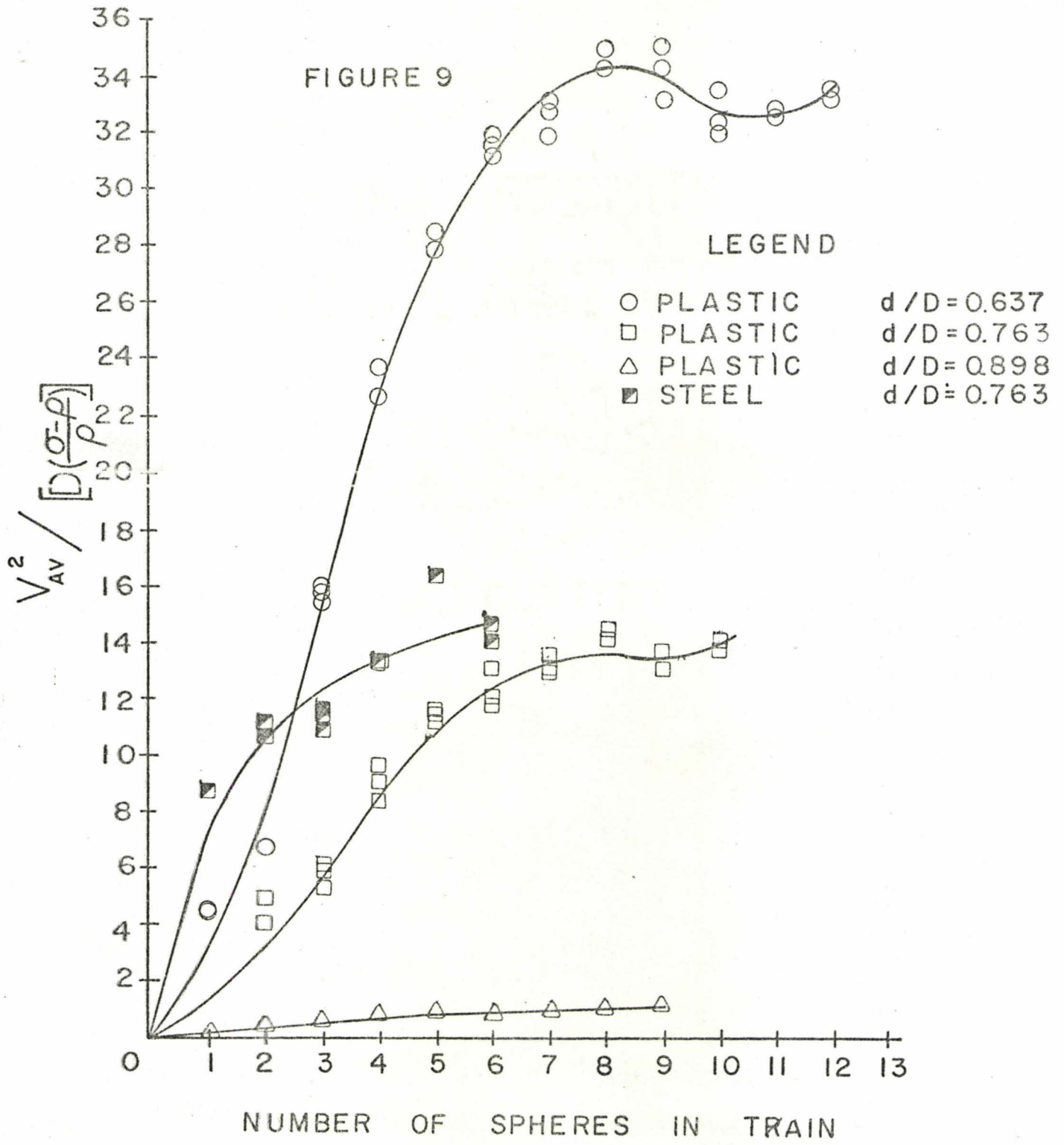
SINGLE SPHERES IN WATER
AND POLYMER
RETEN 423

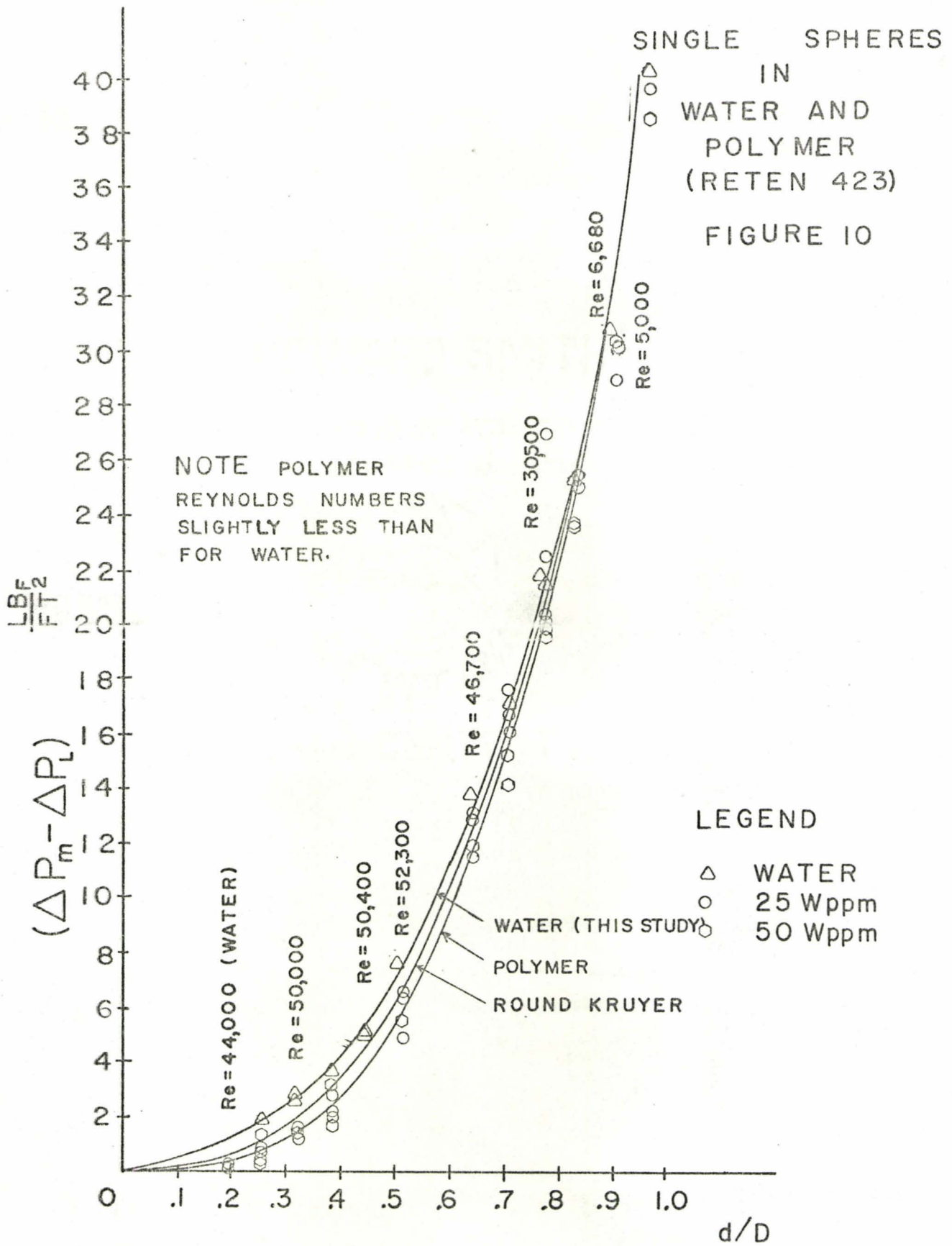
FIGURE 8

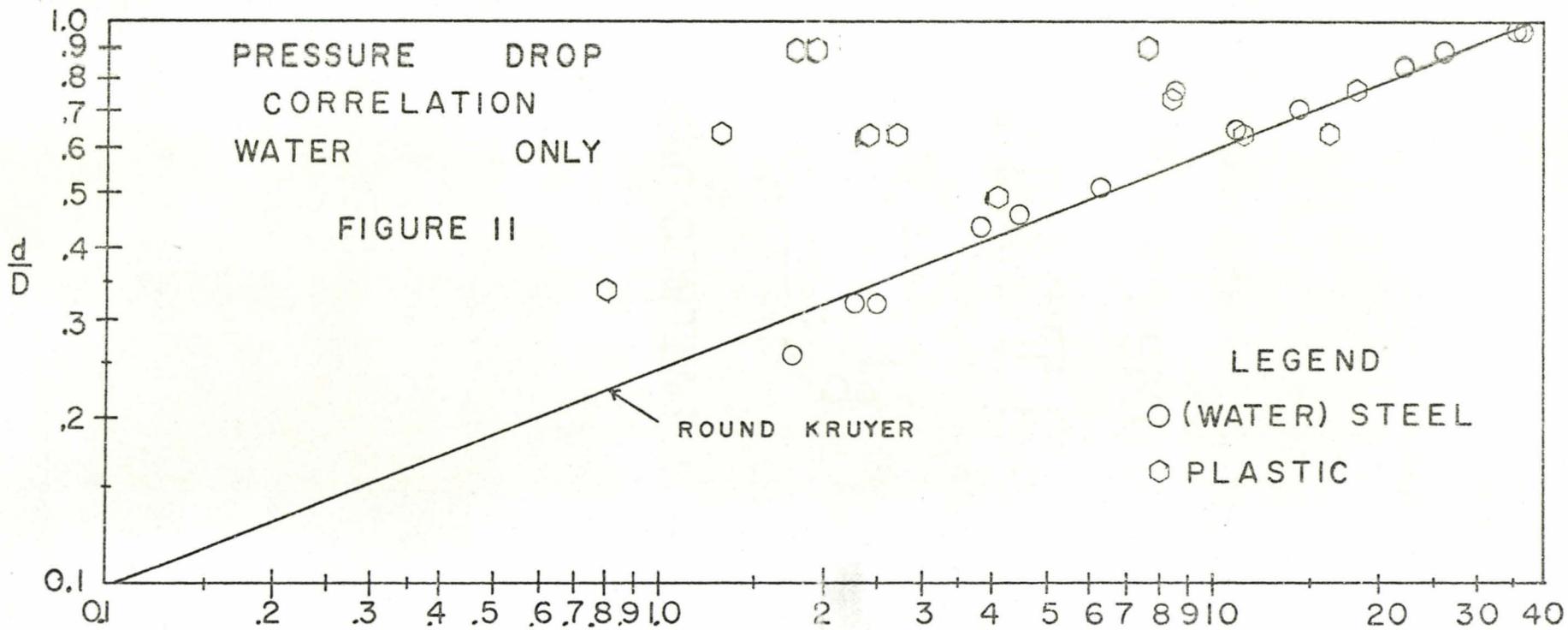


SPHERE TRAIN SUPPORT VELOCITIES

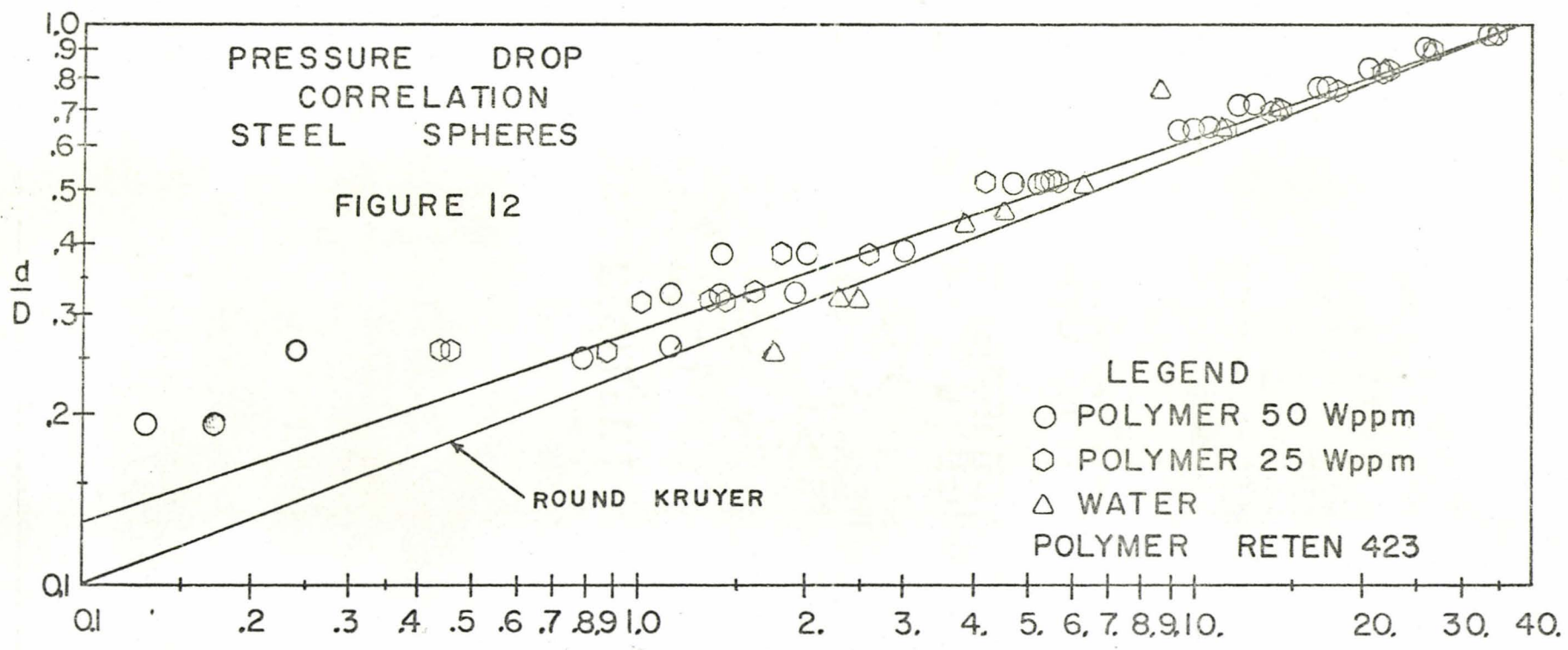
SEPERATION - d WATER ONLY







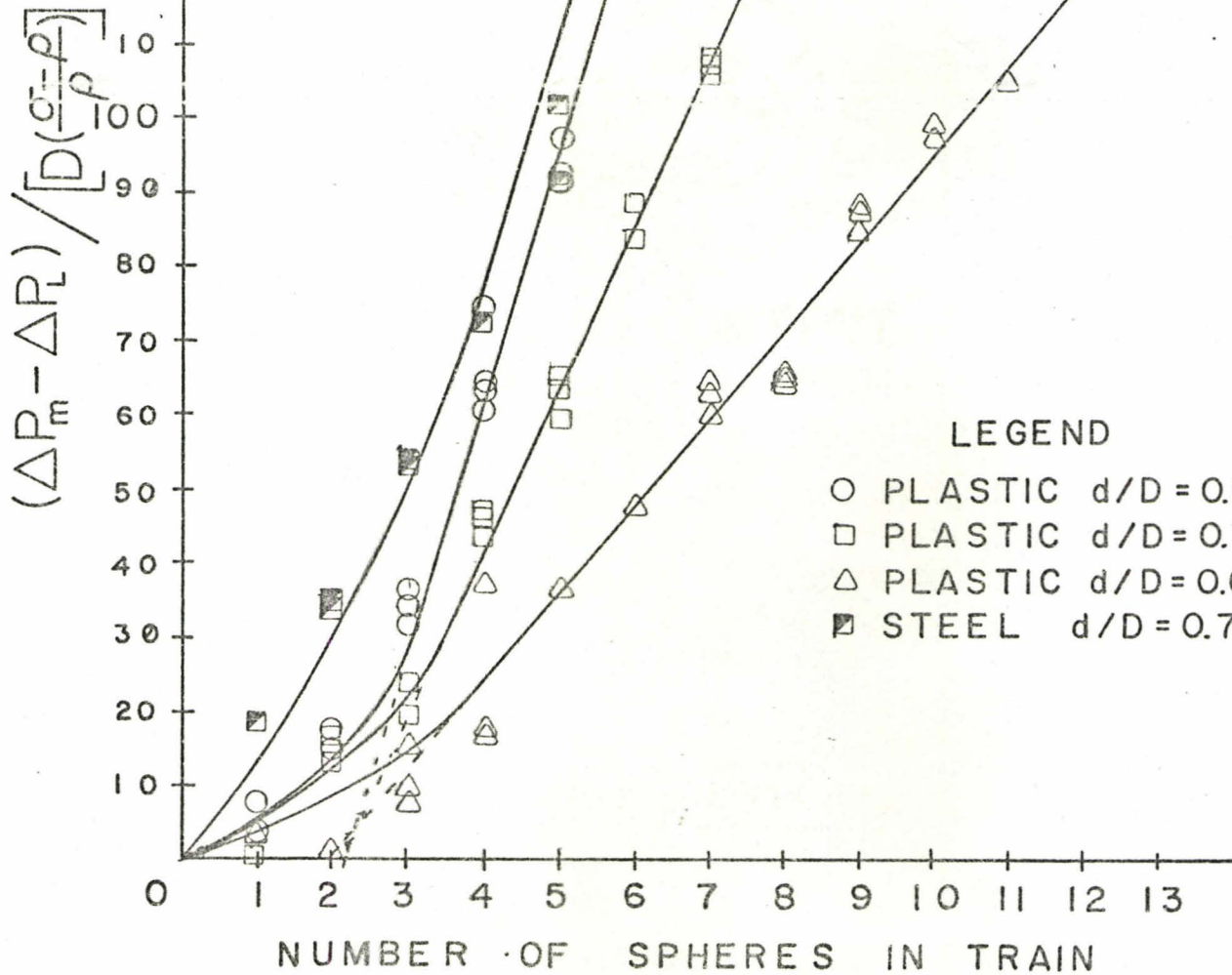
$$\frac{(\Delta P_m - \Delta P_L)}{[D(\frac{\sigma}{\rho})]}$$

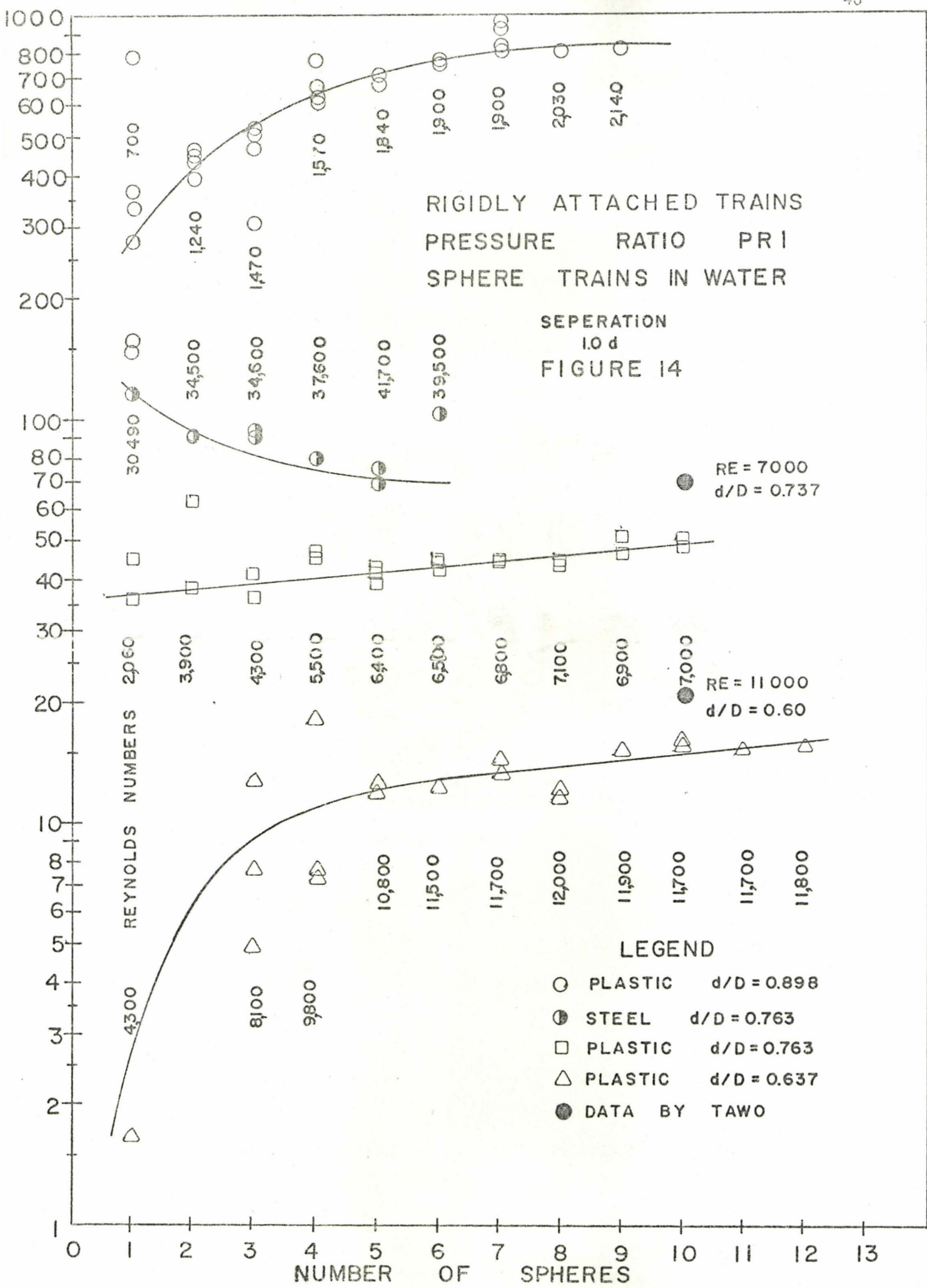


$$\frac{(\Delta P_m - \Delta P_L)}{[D(\frac{\sigma - \rho}{\rho})]}$$

SPHERE TRAIN PRESSURE
DROP CORRELATION
WATER ONLY SEPERATION - d

FIGURE 13





VII DISCUSSION

One important portion of these experiments dealt with the study of the hydrodynamic suspension of single spheres in water and polymer solution. Referring to figure 4, a graph of the drag coefficient as a function of the diameter ratio for single steel spheres in water and polymer, it can be seen that the anticipated trend is followed. That is, at $d/D = 0$ for both water and polymer the curve extrapolates to an unbounded settling value of $C_{d\text{WATER}} = 0.44$ or $C_{d\text{POLY}} = 0.56$ while asymptotically approaching $C_d^* = \infty$ as d/D approaches unity. The region between these limits is described by equation (3.1), chapter III where

$$C_d^* = \frac{4}{3} \left(\frac{\sigma - \rho}{\rho} \right) \frac{dg}{V_{AV}^2} \quad (7.1)$$

This equation emphasises the dependence of the drag coefficient on the Froude number.

For water the data presented in figure 4 compares favourably to that of McNown and Newlin⁽²⁾ and Round and Kruyer⁽²¹⁾ although the tests by McNown and Newlin were performed at a constant Reynolds number with the sphere rigidly fixed in the center of the pipe, whereas the results of Round and Kruyer were determined using a freely suspended sphere in an inclined tube. When tests are performed using freely suspended spheres, which can absorb energy by movement in addition to the usual manner through skin friction and pressure change, an increase in the drag coefficient can be expected, as shown by the results of Round and Kruyer when compared to those of McNown and Newlin. The results of this study generally follow the same trend as those

of Round and Kruyer, but have more scatter because of the less accurate support velocity measurements.

There is, of course, a great discrepancy between the equation;

$$C_d^* = \left[\frac{d/D}{1 - (d/D)^2} \right]^2 \quad (7.2)$$

and experimental results below $d/D = 0.82$; since this equation does not consider the effects of viscosity which are apparently predominant at the lower diameter ratios. At the higher diameter ratios the results of this study and those of references (2) and (21) agree. Figure 4 does not show results beyond a diameter ratio of 0.775 although tests were performed for diameter ratios up to 0.956. This is because the results in that range are adequately represented by equation (7.2).

When spheres are suspended in a dilute aqueous polymer solution the drag coefficients are similar to those obtained in water, as figure 4 shows, however, below a d/D ratio of 0.72 they are slightly greater than those for water. Equation (7.1) indicates that for C_d^* to increase in value, the supporting velocity V_{AV} must decrease, since for a given diameter ratio, all other factors remain constant.

It has been generally observed by other authors that the addition of polymer to turbulent pipe and flat plate flow decreases the skin friction. It is reasonable then to assume that along with the usual decrease in pressure drop accompanying a decrease in velocity, the polymer would further decrease the pressure drop due to skin friction along the wall of the pipe, as well as along the surface of the sphere. However, the weight of the sphere remains unchanged, therefore, the sum of the skin friction, and form drag components as well as buoyancy must still equal the weight of the sphere. This means that the form drag component must increase if the sphere skin friction decreases.

From figure 13, which shows the measured pressure drop across the sphere less the tube skin friction pressure drop, it can be seen that the pressure drop for polymer is less than that for water. Since it appears that the form pressure drop component is increased by the presence of polymer, then the pipe skin friction loss caused by the disturbance of flow around the sphere, and the skin friction component along the sphere, must have been greatly decreased to account for the net decrease.

For the case of a sphere settling in a unbounded polymer solution, White⁽¹⁵⁾ explained the increased drag, when the boundary layer was turbulent, as being due to an increased wake diameter. For this case, of confined flow past a sphere, it would appear that the same situation exists, provided the diameter ratio is less than 0.72.

It is interesting to note that polymer effects become noticeable as viscous effects become predominant in the system; since it is apparently because of viscous effects that equation (7.2) becomes invalid at approximately the same diameter ratio as polymer effects become apparent.

A question that has been raised is, what effects can the addition of drag reducing polymer have on the dynamics of the transport of capsules through pipelines? Since the precise physical characteristics, such as the ratio of the capsule specific gravity to fluid specific gravity, and the capsule shape and dimensions, play a very important part (references (3) to (10) and (20)) in determining the flow characteristics of a sphere through a pipeline, a rigorous answer cannot be made on the basis of this study. However, it can be postulated from the data presented in figure 4 and figure 12 that at high diameter ratios (where most capsule pipelines operate) the addition of polymer would reduce the drag of the transporting fluid passing through the pipework, thereby speeding the transfer of capsules in addition to lowering the energy

requirements. Furthermore, if the pipelines were to be operated at lower diameter ratios, where the addition of polymer has increased the drag coefficient, it might be expected that a further increase in the speed of capsule transfer would occur.

Since the drag coefficient is calculated from the support velocity it is to be expected that graphs of V_{AV} show the same trend as those of C_d^* . This is evident in figures 6 and 8, where the use of polymer produces a reduced supporting velocity; the velocity decreasing with increasing polymer concentration up to 50 Wppm at which point the maximum effect is observed.

In figures 6 and 8 the data of this study is also compared to that obtained by Round and Kruyer under similar circumstances. It can be seen that the support velocities obtained by Round and Kruyer⁽²¹⁾ are above those of this study. The reason for this is that spheres freely suspended in an inclined tube do not have the same degree of freedom that spheres suspended in a vertical tube have. In an inclined tube the spheres would rest on the wall, partly restricting their motion and ability to absorb energy through modes other than skin friction and pressure change. This would result in a decreased drag coefficient and increased support velocity, compared to that observed for a sphere suspended in a vertical tube. This type of effect was observed earlier, when the results of Round and Kruyer were compared to those of McNown and Newlin. The latter's results were for a sphere rigidly fixed in a tube, and showed a drag coefficient that was slightly less than that observed by Round and Kruyer for their freely suspended spheres.

In figure 8 an attempt has been made to correlate all available data to a single set of curves by taking into account the specific gravity ratio and the diameter of the test section. The resulting grouping of variables then is $V_{AV}^2/[D(\sigma - \rho)/\rho]$. The justification for this particular

grouping is that the drag coefficient analysis (see chapter III) indicated that the drag coefficient was a function of the Froude Number, and the above group is a form of the Froude Number. The diameter of the pipe has been used, rather than that of the sphere to allow data from different diameter test sections to be compared.

A similar type of correlation has been attempted with the pressure drops, as was done with the support velocities. The term $(\Delta P_m - \Delta P_L)$ was divided by $[D(\sigma - \rho/\rho)]$ and plotted against d/D , logarithmically. By doing this it appears that the data can be correlated using straight lines, as shown in figures 11 and 12. The resulting equations are, for water;

$$\ln(d/D) = 0.395 \ln \left\{ (\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})] \right\} - 1.408 \quad (7.3)$$

and for polymer:

$$\ln(d/D) = 0.331 \ln \left\{ (\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})] \right\} - 1.271 \quad (7.4)$$

The values for steel spheres in water agree very well with equation (7.3), and the results of Round and Kruyer⁽²¹⁾. The polymer results display a greater scatter than do those for water, but this can be expected because of the difficulties encountered in maintaining sphere stability while at the same time maintaining the appropriate polymer concentration. It is possible that this scatter conceals two separate lines, one for 25 and one for 50 Wppm polymer as was the case for the support velocity (V_{AV}^2 vs d/D). However, the graph of $(\Delta P_m - \Delta P_L)$ as a function of d/D for single spheres supported in a polymer solution, also had only a single line for both polymer concentrations. It is therefore possible that the effects on the pressure drop

of increasing the polymer concentration beyond 25 Wppm are so slight as to be negligible.

The results for plastic spheres in water however show considerable scatter. From the Error Analysis, Appendix I, the estimated error in this range of measurement was about $\pm 200\%$. The reason for this is that the manometer no flow reading is considerably larger than the actual pressure drop reading.

From a consideration of single spheres we now turn to the consideration of trains of spheres. Figure 5 shows the variation of "drag coefficient per sphere", as a function of the number of spheres in the train, for both rigidly and flexibly attached trains of plastic and steel spheres. It can be seen that C_d^*/n becomes virtually independent of the number of spheres in the train, once the length is beyond approximately eight or nine spheres. This trend is also evident in figure 13, a graph of sphere train pressure drop $(\Delta P_m - \Delta P_L) / D \left[\frac{\sigma - \rho}{\rho} \right]$ as a function of n , the number of spheres in the train.

From figure 5 it can be seen that the drag coefficients for unattached and flexibly attached sphere trains are greater than those for rigidly attached trains. The reason for this is that being less restricted the flexible sphere trains were able to absorb energy by movement, in addition to the usual manner, through skin friction and pressure change.

The single spheres had extremely complex modes of oscillation, which were partly carried over to the sphere trains. The very small single spheres alternated between clinging to the wall of the test section and bouncing back and forth on the wall. As the diameter ratio increased the excursion distance from the wall increased, until at a diameter ratio of approximately 0.5 the spheres were centralized in the flow, and rocked gently back and forth. As the diameter ratio approached 0.7 the rocking decreased,

and occasionally changed to violent spinning about the inside wall of the test section. This spinning action restricted the degrees of freedom of the spheres and consequently decreased the drag coefficient. The above described modes of oscillation of single spheres were also evident in the trains of both flexible and rigidly attached spheres. The motion of the unattached spheres was in every respect identical to that of the single spheres, while the motions of the flexibly attached trains were slightly restricted by the connections. The flexibly attached spheres tended to rotate in the free stream, or roll about the inside wall of the test section. For both these motions the centers of the individual spheres were approximately 120 to 180 degrees out of phase with those of the adjacent ones (i.e., a spiralling motion). The rigidly attached trains were centered in the free stream, and moved with a pitching or rocking motion, or rolled or transgressed about the inside wall of the pipe.

A graph of $V_{AV}^2 / [D(\frac{\sigma - \rho}{\rho})]$ similar to that for the single spheres, has been plotted for the trains of spheres and is shown in figure 9. As expected the same trend that was evident in figure 5 and 13 is evident in this graph; that is, the support velocity increases with increasing numbers of spheres until the train is seven or eight spheres long. At this point however the behaviour deviates from the expected. Rather than the support velocity becoming constant it decreases, then starts to increase again, when four or five more spheres have been added. Apparently this effect is related to the end effects, and the length of developed flow achieved along the spheres, although the precise mechanism cannot be postulated.

It was stated in the chapter on theory (chapter III) that the sphere train end effects could be determined from a graph of $\Delta P_m - \Delta P_L$ against n . Figure 13 is such a graph, showing $(\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})]$ as a function of n .

It was shown in chapter III, that the end effects, pressure drops, and the number of spheres could be related by the following equation;

$$(\Delta P_m - \Delta P_L) = \left(\frac{\Delta P_S}{L}\right) (n - 1)d + \Delta P_E \quad (3.15)$$

By obtaining the value of $\Delta P_m - \Delta P_L$ from figure 13 for two different values of n , it is possible using equation (3.15) to compute values for $\Delta P_S/L$ and ΔP_E . Substituting for the sphere train having $d/D = 0.898$, for $n = 4$, and $n = 5$, (plastic);

$$60 \times 0.043 = \left(\frac{\Delta P_S}{L}\right)(3)\left(\frac{1.74}{12}\right) + \Delta P_E$$

and

$$195 \times 0.043 = \left(\frac{\Delta P_S}{L}\right)(7)\left(\frac{1.74}{12}\right) + \Delta P_E$$

solving;

$$\frac{\Delta P_S}{L} = 10.05 \text{ lb}_F/\text{ft}^2/\text{ft}$$

$$\Delta P_E = -1.78 \text{ lb}_F/\text{ft}^2$$

The negative sign in ΔP_E indicating that it is a pressure decrease. For a sphere train having $d/D = 0.763$, for $n = 4$, and $n = 8$, (plastic);

$$41 \times 0.0394 = \left(\frac{\Delta P_S}{L}\right)(3)\left(\frac{1.478}{12}\right) + \Delta P_E$$

and

$$129 \times 0.0394 = \left(\frac{\Delta P_S}{L}\right)(7)\left(\frac{1.478}{12}\right) + \Delta P_E$$

therefore

$$\frac{\Delta P_S}{L} = 7.0 \text{ lb}_F/\text{ft}^2/\text{ft}$$

$$\Delta P_E = -0.96 \text{ lb}_F/\text{ft}^2$$

For a sphere train having $d/D = 0.763$, for $n = 4$, and $n = 6$, (steel);

$$79. \times 1.169 = \left(\frac{\Delta P_S}{L}\right)(3)\left(\frac{1.497}{12}\right) + \Delta P_E$$

$$144 \times 1.169 = \left(\frac{\Delta P_S}{L}\right)(7)\left(\frac{1.497}{12}\right) + \Delta P_E$$

therefore

$$\frac{\Delta P_S}{L} = 305 \text{ lb}_F/\text{ft}^2/\text{ft}$$

$$\Delta P_E = -21.7 \text{ lb}_F/\text{ft}^2$$

For a sphere train having $d/D = 0.637$, for $n = 4$, and $n = 8$, (plastic);

$$85.0 \times 0.0465 = \left(\frac{\Delta P_S}{L}\right)(3)\left(\frac{1.235}{12}\right) + \Delta P_E$$

$$70. \times 0.0465 = \left(\frac{\Delta P_S}{L}\right)(7)\left(\frac{1.235}{12}\right) + \Delta P_E$$

therefore

$$\left(\frac{\Delta P_S}{L}\right) = 5.1 \text{ lb}_F/\text{ft}^2/\text{ft}$$

$$\Delta P_E = -0.415 \text{ lb}_F/\text{ft}^2$$

It is evident that as the diameter ratio decreases the pressure gradient $\Delta P_S/L$ and the end effects also decrease.

The final quantity of interest is the pressure ratio PR1 which is shown in figure 14 plotted as a function of n , the number of spheres. The quantity PR1 is a ratio of the pressure gradient in the free tube, to that in the tube occupied by the sphere train and is a function of the diameter ratio and Reynolds number also. Knowing this ratio, and the pressure gradient in the free tube, would, if PR1 is sufficiently general, allow the pressure gradient in a tube containing a stationary sphere train to be predicted. To determine how general this ratio is, a comparison of PR1 obtained under two slightly different conditions has been made. The data obtained by Tawo⁽²⁸⁾ for a train rigidly fixed to the tube wall was compared to the data of this present study wherein the train was freely suspended in a vertical tube.

The data of this study, presented in figure 14 can be described by equation (3.20) (chapter III), however, to compare it to that obtained by Tawo requires that the end effects be eliminated as in equation (3.19) (chapter III).

$$\text{PR1} = 1 + \frac{L}{(n-1)d} \left[\frac{\Delta P_m}{\Delta P_L} - \frac{\Delta P_E}{\Delta P_L} - 1 \right] \quad (3.19)$$

Substituting into equation (3.19), for the plastic spheres having $d/D = 0.763$ at the point where $n = 10$, which is the point at which this data can best be compared to that of Tawo.

$$PR1 = 1 + \frac{5.0}{9 \times 1.978} \left[\frac{7.37}{.560} + \frac{.96}{.560} - 1 \right]$$

therefore

$$PR1 = 63.5$$

which compares favourably with the result $PR1 = 68$ achieved by Tawo.

VIII CONCLUSIONS

On the basis of analysis and experimental results presented earlier, the following conclusions can be made;

(1) For steel spheres dynamically suspended in a dilute aqueous polymer solution within a cylindrical boundary, the drag coefficient in the range $0 < d/D < 0.7$ is increased over that observed in water. Apparently this increase in drag coefficient is accompanied by a decrease in skin friction pressure drop along the pipe wall and along the sphere surface, and an increase in form pressure drop across the sphere.

(2) For single spheres hydrodynamically suspended in water the pressure drop can be expressed by the implicit equation;

$$\ln(d/D) = 0.395 \ln \left\{ (\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})] \right\} - 1.408$$

(3) For a single sphere suspended in dilute aqueous polymer solutions the pressure drop can be expressed by the implicit equation;

$$\ln(d/D) = 0.331 \ln \left\{ (\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})] \right\} - 1.271$$

(4) For sphere trains dynamically suspended in water, within a cylindrical boundary, the drag coefficient per sphere is a function of the diameter ratio, the specific gravity ratio, and the method of connecting the spheres. For rigidly connected spheres the drag

coefficient per sphere is less than for flexibly attached ones. The drag coefficient per sphere in the rigidly attached trains decreased to an approximately constant value as the number of spheres approached nine.

- (5) For trains of rigidly attached spheres dynamically suspended in water, the pressure drop $(\Delta P_m - \Delta P_L) / [D(\frac{\sigma}{\rho})]$ is a linear function of the number of spheres in the train, and a function of the diameter ratio and specific gravity ratio of the spheres, provided the number of spheres in the train is greater than five.
- (6) For trains of spheres the ratio of the pressure gradient along the sphere train to the pressure gradient in the free pipe, becomes a constant value once the number of spheres in the train is greater than nine. This final value of $PR1$ is a function of the diameter ratio and specific gravity ratio of the suspended spheres as well as the pipe Reynolds number. The values for $PR1$ obtained in this study are in agreement with those obtained by Tawo.

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APPENDIX I
ERROR ANALYSIS

It is difficult to exactly specify the error in any given measurement or calculation, usually however a range can be specified. It is customary when a large number of readings are taken to specify the measurement as being within a given number of standard deviations from the mean of the readings. Such a measure gives the degree of reproducibility, or precision of a measurement.

The accuracy of a measurement however is a measure of how close the value is to the "true" value; it is obvious that a measurement can have good precision but poor accuracy. In this chapter an attempt will be made to estimate the accuracy of the results.

In table 1 are listed estimates of the accuracy of the primary measurements made in this experiment. They are based on the type of instrument they were recorded with and the experience gained in using them.

I-1 Error in V_{AV} - Without Polymer

The accuracy of the measurement V_{AV} is based on the accuracy of the component measurements using the "most probable" method to estimate the errors. Now,

$$V_{AV} = \frac{GPM}{D^2} \times K$$

where

$$K = \frac{4}{\pi \times 6.229 \times 60}$$

then

TABLE I
ERROR ESTIMATES IN MEASURED QUANTITIES

Description	Symbol	Error
Tube diameter	D	$\pm 1.0\%$
Sphere diameter	d	$\pm 0.1\%$
Steel		
Plastic		$\pm 0.9\%$
Rotameter reading	GPM	#1 (15-40 GPM) $\pm 5 \rightarrow \pm 1\%$
		#2 (1-14 GPM) $\pm 7 \rightarrow \pm 1\%$
		#3 (0-5 GPM) $\pm 5 \rightarrow \pm 1\%$
Polymer flowmeter	\dot{m}_p	$\pm 10 \rightarrow \pm 4\%$
Distance between pressure taps	L	$\pm .1\%$
Error in manometer reading	h_m	$\pm 20 \rightarrow \pm 1\%$ (Both legs combined)
Error in manometer inclination ($\sin \theta$)		$\pm 0.05\%$
SG of manometer fluid	γ_m	$\pm .08\%$
Error in weighing spheres		$\pm .5\%$
Steel		
Plastic		$\pm 1.0\%$
Variation in weight of polymer powder	m_p	$\pm 2\%$
Error in water in polymer mix	m_w	$\pm 0.3\%$
Error in water temperature	T_w	$\pm 1^\circ\text{C}$

$$d(V_{AV}) = \sqrt{\sum \left(\frac{\delta V_{AV}}{\delta x} * dx \right)^2}$$

therefore

$$d(V_{AV}) = \left\{ \left[\frac{d(\text{GPM})}{D^2} \right]^2 + [2(\text{GPM})d(D)]^2 \right\}^{1/2}$$

Dividing by V_{AV} we have;

$$\frac{d(V_{AV})}{V_{AV}} = \left\{ \left[\frac{d(\text{GPM})}{\text{GPM}} \right]^2 + \left[\frac{2d(D)}{D} \right]^2 \right\}^{1/2}$$

I From table 1 using the estimated error in the rotameters at low flow rates;

Rotameter #1

$$\frac{d(V_{AV})}{V_{AV}} = \left\{ [5]^2 + [2(1)]^2 \right\}^{1/2} = \pm 5.4\%$$

Rotameter #2

$$\frac{d(V_{AV})}{V_{AV}} = \left\{ [7]^2 + [2(1)]^2 \right\}^{1/2} = \pm 7.3\%$$

Rotameter #3

$$\frac{d(V_{AV})}{V_{AV}} = \left\{ [5]^2 + [2(1)]^2 \right\}^{1/2} = \pm 5.9\%$$

II Similarly from table 1 at high flow rates we have;

$$\frac{d(V_{AV})}{V_{AV}} = \left\{ [1]^2 + [2(1)]^2 \right\}^{1/2} = \pm 2.2\%$$

I-2 Error in V_{AV} with Polymer

With polymer V_{AV} is;

$$V_{AV} = (GPM_{WATER} + GPM_{POLY.}) \frac{K}{D^2}$$

I At low flow rates; (using rotameter #2)

$$\Delta GPM_{WATER} = 0.07 \times 4.2 = 0.294$$

$$\Delta GPM_{POLY.} = 0.10 \times 0.13 = 0.013$$

therefore;

$$\Delta GPM = \frac{(0.294 + 0.013) \times 100}{4.2 + 0.13} = \pm 7.08\%$$

It is apparent that injecting polymer does not appreciably alter the accuracy with which V_{AV} is measured in spite of the relatively large fluctuations in the polymer flowrate.

I-3 Error in Pressure Drop Measurements

The pressure drop is calculated from the equation;

$$\Delta P_m = h_{ACT} (\gamma_m - 1) \sin \theta K \quad (1.1)$$

h_m is the manometer reading including density effects, while h_{ACT} is the true manometer reading, corrected for density effects;

$$h_{ACT} = h_m - h_0$$

hence the error in h_{ACT} is;

$$\Delta h_{ACT} = \frac{\Delta h_m + \Delta h_0}{h_m - h_0} \quad (1.2)$$

and at low flow rates as $(h_m - h_0) \rightarrow 0$, $\Delta h_{ACT} \rightarrow \infty$.

I At low flow rates; ($R_e \cong 2600$)

There is considerable scatter in the C_f vs R_e data obtained in this experiment but it seems to be consistently below the Blasius line, therefore using the experimental results at $R_e = 2600$;

$$V_{AV} = \frac{R_e v}{D} = 0.28 \text{ ft/sec}$$

and

$$\Delta P_m = C_f \left(\frac{L}{D}\right) \frac{\rho v^2}{2g_c}$$

therefore

$$\Delta P_m = 0.027 \times \left(\frac{5.0}{0.1615}\right) \times \frac{62.4 \times (.028)^2}{.1615} = 0.0565 \text{ lb}_F/\text{ft}^2$$

A typical value of h_0 at this flow rate is $h_0 = .75$ cm. using equation (1.1);

$$\Delta P_0 = 0.258 \text{ lb}_F/\text{ft}^2$$

Using equation (1.2) the error in the manometer reading is;

$$\Delta h_{\text{ACT}} = \frac{[0.2 \times (.258 + .565)] + [.2 \times .258] \times 100}{.056} \cong \pm 200\%$$

Combining this with the error in manometer fluid density, and angle of inclination measurements the error in the pressure measurement is;

$$\Delta P_m = \left\{ [200]^2 + [.08]^2 + [.05]^2 \right\}^{1/2} \cong \pm 200\%$$

The value at first seems very large, however it must be remembered that this is in a region where the pressure drops are very small, and the initial reading caused by the density differences is larger than the actual reading. It is to be expected that the results in this region would be poor. At low flow rates therefore the pressure drops were obtained from the theoretical correlation $C_f = \frac{64}{R_e}$. At higher flow rates, where the no flow manometer reading (which remains relatively constant) is a smaller percentage of the total reading, the error in the pressure measurement becomes less.

II For the high flow rates ($R_e \cong 50,000$)

As before,

$$V_{AV} = 5.38 \text{ ft/sec}$$

and

$$\Delta P = 15.2 \text{ lb}_F/\text{ft}^2$$

Again for

$$h_0 = .75 \text{ cm.}, \Delta P_0 = .258 \text{ lb}_F/\text{ft}^2$$

therefore

$$\Delta h_{\text{ACT}} = \frac{[0.01 \times (15.2 \times .258)] + [.2 \times .258] \times 100}{15.2} = \pm 1.36\%$$

and similarly

$$\Delta P_m = \left\{ (1.36)^2 + (.08)^2 + (.05)^2 \right\}^{1/2} \cong \pm 1.36\%$$

I-4 Error in the Friction Factor

The friction factor was calculated from the equation;

$$C_f = \frac{\Delta P_m}{\left(\frac{L}{D}\right) \frac{\rho V^2}{2g_c}} = \frac{\Delta P_m}{\left(\frac{L}{D}\right) \frac{(\text{GPM})^2}{D^4} \times K}$$

where the various conversion constants are fluid density (assumed completely accurate compared to the other measurements) have been lumped into K.

then;

$$\Delta C_f = \left\{ [\Delta (\Delta P_m)]^2 + [\Delta L]^2 + [2(\Delta \text{GPM})]^2 + [5(\Delta D)]^2 \right\}^{1/2}$$

The variation in the accuracy of ΔC_f with Reynolds number must be expected to be highly non linear because of the non-linearity of the component terms, and since the friction factor Reynolds number results are so important,

it was decided to calculate the accuracy of C_f for a complete range of Reynolds numbers. The listing of the computer program to do this is in table 2. Figure 15 shows the variation of the accuracy of the friction factor with the Reynolds number and figure 16 shows the percent deviation of the experimental results from the theoretically expected value of the friction factor.

I-5 Error in Polymer Concentration

The error in the concentration of polymer in the test section consists of two basic components, firstly the error in the concentration of the stock solution, and secondly the error caused by the mixing of the solution with the main flow of water to the test section.

I The Concentration Error in Mixing of the Stock Solution at 2000 Wppm:

$$\text{Concentration} = \frac{m_p}{m_w} = \frac{2 \times 10^3}{10^6}$$

$$\Delta(\text{CONC.}) = (\Delta \text{ POLY.} + \Delta \text{ WATER}) = (2.0 + 0.3) \cong 2\%$$

The polymer powder can be weighed to a much better accuracy than $\pm 2\%$, however in mixing some of it clings to the walls of the eductor.

II Error in the Concentration in the Test Section:

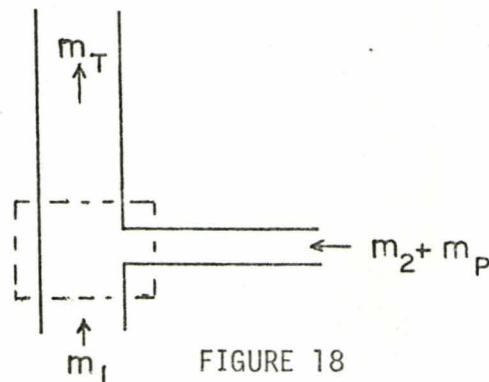


FIGURE 18

TABLE 2

```

PROGRAM IST (INPUT, OUTPUT, TAPE5=INPUT, TAPE6=OUTPUT)
REAL NU
DIMENSION ID(100), IX(100), IY(100), RRE(5, 100), DDPT(5, 100), V(30),
1 GPM(30), DGPM(30), XE(30), DPA(30), DEL(30), DDP(30), DCF(30), XRE(30)
2 , DP(30)
COMMON/111/RE(5, 100), DPT(5, 100), D, NU, RO, N
COMMON/222/ ISUB(5)
RO=62.4
D=0.1615
NU=1.744E-05
VF=5.0
VO=0.05
GPMF=1.0
GPMO=5.0
DPF=0.07
DPI=0.01
DDPO=0.258

C
C READ DIGITIZER DATA
K=1
NN=500
340 DO 300 I=1, NN
IF (NN.EQ.1) GO TO 310
READ (5, 305) ID(I), IX(I), IY(I)
305 FORMAT (3I10)
IF (IX(I).EQ.0) GO TO 320
RRE(K, I)=FLOAT(IX(I))/100.0
DDPT(K, I)=FLOAT(IY(I))/100.0
300 CONTINUE
320 K=K+1
ISUB(K-1)=I-1
IF (K.GE.5) GO TO 330
GO TO 340
330 NN=1
GO TO 340
310 READ (5, 42) XPL, YPL, XACT, YACT
42 FORMAT (4F20.2)

C
C CONVERT DIGITIZER DATA TO ACTUAL VALUES
SFX1=XPL/(ALOG(XACT)-ALOG(1000.0))
SFY1=YPL/(ALOG(YACT)-ALOG(0.001))
DO 43 I=1, 4
WRITE (6, 70)
70 FORMAT (60X, *PE*, 20X, *CF*//)
KK=ISUB(I)
DO 43 J=1, KK
RE(I, J)=EXP((PRE(I, J)/SFX1)+ALOG(1000.0))
DPT(I, J)=EXP((DDPT(I, J)/SFY1)+ALOG(0.001))
WRITE (6, 46) RE(I, J), DPT(I, J)
46 FORMAT (45X, 2E20.5)
43 CCNTINUE

C
DO 700 I=1, 21
V(I)=(FLOAT(I-1)*(VF-VO)/20.0)+VO
GPM(I)=V(I)*D*D*3.14159*6.229*60.0/4.0

```



```
000210 DGPM(I)=(FLOAT (I-1)*(GPMF-GPMO)/20.0)+GPMO
000216 XE(I)=V(I)*D/NU
000221 L=1
000222 CALL INTERP(V(I),L,DP(I),XRE(I))
000225 DPA(J)=((FLOAT(I-1)*(DPF-DPI)/20.0)+DPI)*DP(I)
000234 DEL(I)=DPA(I)+DDPO
000237 DDP(I)=(DEL(I)*100.0)/DP(I)
000242 DCF(I)=SQRT((DCP(I)**2)+1.0+((2.0*CGPM(I))**2)+16.0)
000253 700 CONTINUE
000255 WRITE(6,701)
000260 701 FORMAT(20X,*VEL*,11X,*RE*,13X,*GPM*,12X,*DGPM*,10X,*DP*,10X,
1 *DPA*,12X,*DEL*,12X,*DDP*//)
000260 DO 705 I=1,21
000262 WRITE(6,702) V(I),XE(I),GPM(I),DGPM(I),DP(I),DPA(I),DEL(I),DDP
000305 702 FORMAT(10X,8F15.3//)
000305 705 CONTINUE
000307 WRITE(6,746)
000313 746 FORMAT(H1,35X,*ESTIMATED ERROR IN FRICTION FACTOR*//)
000313 WRITE(6,748)
000317 748 FORMAT(46X,*RE*,14X,*CF*//)
000317 DO 747 I=1,21
000321 WRITE(6,703) XE(I),DCF(I)
000330 703 FORMAT(40X,2F15.3)
000330 747 CONTINUE
000332 STOP
000334 END
```

UNUSED COMPILER SPACE

006700

```

SUBROUTINE INTERP (V,L,DH,CLR)
C
000007 REAL NU
000007 COMMON/111/RE(5,100),DPT(5,100),D,NU,RO,N
000007 CCMCN/222/ ISUB(5)
C
000007 IF (L.GE.10) GO TO 200
000011 DL=5.0
000013 D=0.1615
000014 CLR=V*D/NU
50 IF (CLR.LE.2500.0) GO TO 130
000017 IF (CLR.LT.9400.0) K=1
000021 IF (CLR.LT.9400.0) GO TO 230
000024 C
000026 IF (L-5) 210,210,220
000030 210 K=3
000031 GO TO 230
000032 220 K=4
000033 230 J=ISUB(K)
000035 DO 100 I=1,J
000037 IF (CLR.LE.RE(K,I)) GO TO 110
000043 100 CONTINUE
C
000045 WRITE (6,120) L
000052 120 FORMAT (10X,*DATA NOT IN RANGE*,5X,*SET NUMBER*,5X,I2//)
000052 DH=0.00
000055 GO TO 500
C
000056 110 I=I-1
000060 CF=(DPT(K,I)-DPT(K,I+1))*((CLR-RE(K,I))/(RE(K,I+1)-RE(K,I)))+DPT
1,I+1)
000074 DH=(CF*DL*RO*V*V)/(D*2.0*32.17)
000102 GO TO 500
000103 130 DH=(32.0*DL*RO*V*V)/(32.17*D*CLR)
000112 GO TO 500
C
000112 200 WRITE (6,300)
000116 300 FORMAT (2X,*CF DATA EXCEEDED*//)
000116 500 RETURN
000117 END
UNUSED COMPILER SPACE
010100

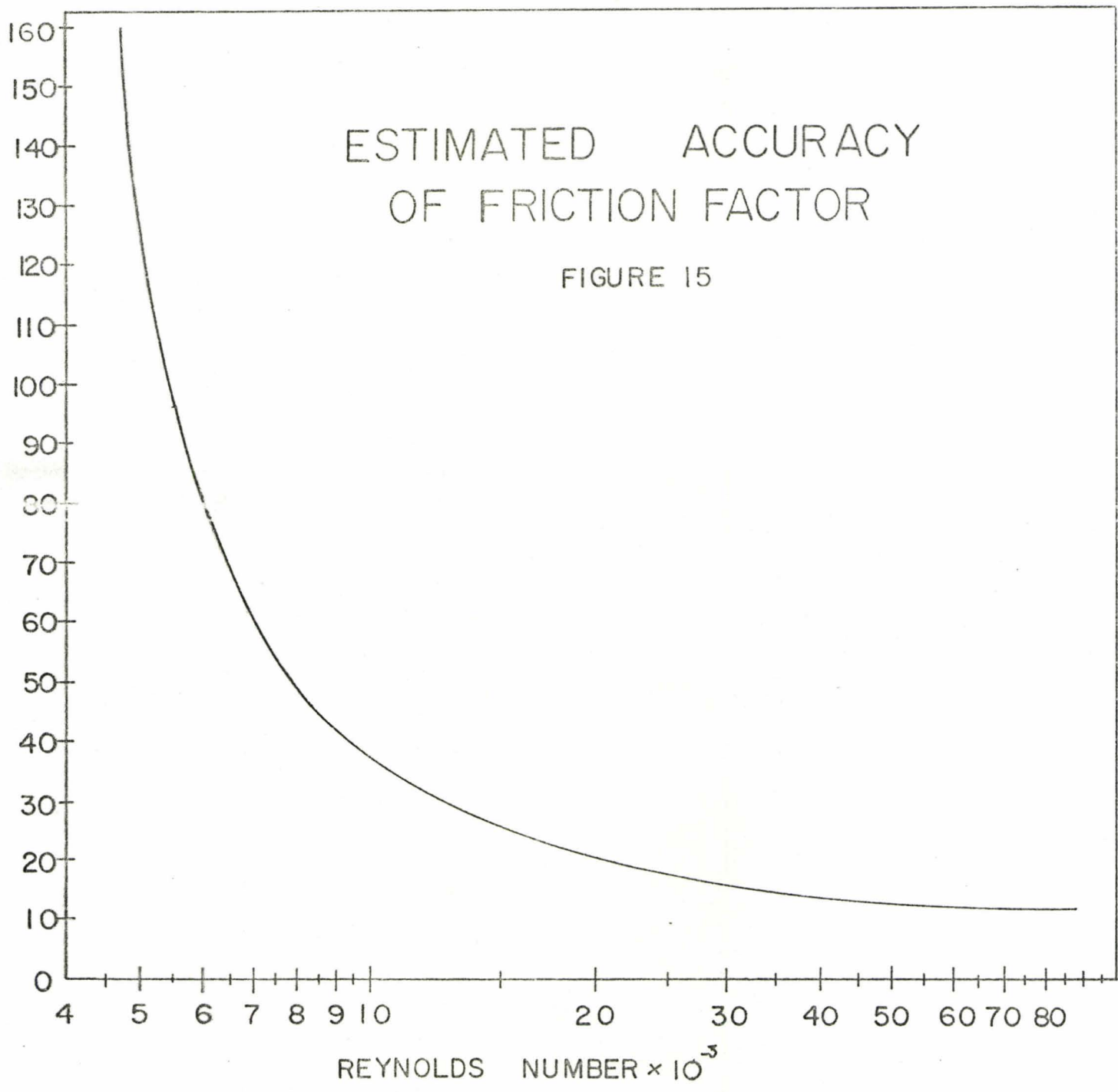
```

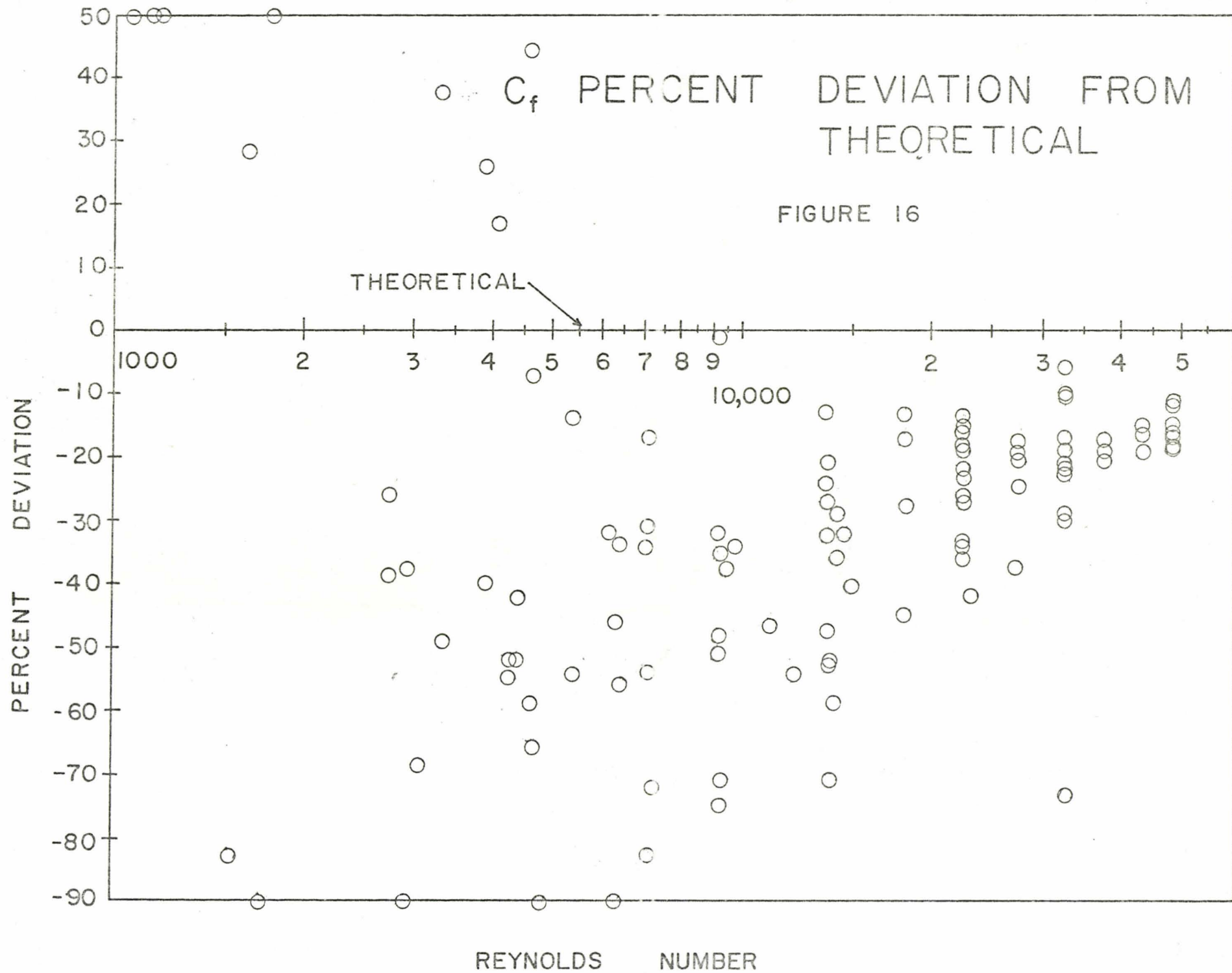
ESTIMATED ERROR IN FRICTION FACTOR

RE	CF
463.016	2487.560
2754.946	407.689
5046.875	124.708
7338.804	54.435
9630.734	36.813
11922.663	32.003
14214.593	27.872
16506.522	24.686
18798.452	22.453
21090.381	20.362
23382.311	19.028
25674.240	17.985
27966.170	17.035
30258.099	16.426
32550.029	15.499
34841.958	14.759
37133.888	14.234
39425.817	14.123
41717.747	13.697
44009.676	13.788
46301.606	13.271

ESTIMATED ACCURACY OF FRICTION FACTOR

FIGURE 15





$$m_2 = m_p + m_w$$

$$m_T = m_1 + m_2 = m_1 + m_p + m_w$$

But $m_p \ll m_w$

therefore

$$\text{CONC.} \cong \frac{m_p}{m_1 + m_w}$$

(i) at low flow rates;

$$\Delta m_1 = 0.04 \times 8.5 = 0.34$$

$$\Delta m_w = 0.2 \times 0.1 = 0.002$$

therefore

$$\Delta \text{CONC.} = \left\{ (20)^2 + \left[\frac{.34 + .002}{85 + .1} \times 100 \right]^2 \right\}^{1/2} = \pm 20.4\%$$

Most of this error is due to the error in measuring the polymer flow rate which was observed at times to fluctuate as much as $\pm 20\%$ at very low flow rates.

(ii) at high flow rates;

$$\Delta m_1 = 0.01 \times 38 = .38$$

$$\Delta m_w = 0.04 \times 0.5 = 0.02$$

$$\text{and } \text{CONC.} = \left\{ (4)^2 + \left[\frac{.38 + .02}{.38 + .5} \times 100 \right]^2 \right\}^{1/2} = \pm 4.1\%$$

I-6 Error in Reynolds Number

The Reynolds number is calculated using;

$$R_e = \frac{V_{AV} D}{\nu}$$

The value of the kinematic viscosity is a direct function of the temperature of the water, which could be measured to within 1°C. This would cause a variation in ν of;

$$3^\circ\text{C } \nu = 1.7435 \times 10^{-5} \text{ ft}^2/\text{sec}$$

$$4^\circ\text{C } \nu = 1.6885 \times 10^{-5} \text{ ft}^2/\text{sec}$$

$$5^\circ\text{C } \nu = 1.0364 \times 10^{-5} \text{ ft}^2/\text{sec}$$

$$\Delta \nu = \left[\frac{(1.7435 - 1.6364) \times 10^{-5}}{1.6885 \times 10^{-5}} \right] \times 100 = \pm 6.32\%$$

I At low flow rates;

$$\Delta R_e = \left\{ (5.4)^2 + (1)^2 + (6.32)^2 \right\}^{1/2} = \pm 8.4\%$$

II At high flow rates;

$$\Delta R_e = \left\{ (3)^2 + (1)^2 + (6.32)^2 \right\}^{1/2} = \pm 7.05\%$$

I-7 Error in Diameter Ratio

For steel spheres (from table 1);

$$\Delta (d/D) = \left\{ (1.0)^2 + (.1)^2 \right\}^{1/2} \cong \pm 1\%$$

For plastic spheres (from table 1);

$$\Delta (d/D) = \left\{ (1.0)^2 + (.5)^2 \right\}^{1/2} \cong \pm 1\%$$

I-8 Error in the Combined Pressure Drop Terms

I For low pressure drop values; for

$$(\Delta P_m - \Delta P_L) / [D(\frac{\sigma - \rho}{\rho})] = 5.0$$

and $d/D = 0.763$ (Plastic), from figure 6,

$$V_{AV}^2 = .075$$

therefore

$$R_e \cong 2500$$

Since this value is in the laminar region the error in

$$(\Delta P_m - \Delta P_L) / [D(\frac{\sigma}{\rho})]$$

is essentially that in ΔP_m which was earlier found to be about $\pm 200\%$.

II For the Region Where $\Delta P_m - \Delta P_L$ is larger; from figure 9 for $d/D = 0.563$, and $(\Delta P_m - \Delta P_L) = 10$, and from figure 6

$$V_{AV}^2 = 22.8$$

therefore

$$R_e \cong 44,000$$

From figure 27

$$C_f = 0.0175$$

therefore

$$\Delta P_L = 11.98 \text{ lb}_F/\text{ft}^2$$

therefore

$$\Delta P_m = 10.0 + 11.98 = 21.90 \text{ lb}_F/\text{ft}^2$$

It was calculated in section I-3 that at high flow rates the error in the pressure drop measurement was about $\pm 1.5\%$. Therefore

$$\Delta (\Delta P_m - \Delta P_L) = \frac{(0.015 \times 21.98) + (0.015 \times 11.98) \times 100}{10.0} = \pm 5.1\%$$

1-9 Error in the Specific Gravity of the Spheres

$$SG = \frac{m}{\frac{\pi d^3}{6}}$$

where m is in gm and d is in cm.

For steel (from table 1);

$$\Delta SG = \left\{ (.5)^2 + [3(1)]^2 \right\}^{1/2} \cong \pm .6\%$$

For plastic (from table 1);

$$\Delta SG = \left\{ (1.0)^2 + [3(1)]^2 \right\}^{1/2} \cong \pm 2\%$$

I-10 Error in the Drag Coefficient

In chapter III (Theory), it was shown that,

$$C_d^* = \frac{4}{3} \left(\frac{\sigma - \rho}{\rho} \right) \frac{dg}{V_{AV}^2}$$

It will be assumed that ρ and g are exact compared to the other variables; therefore

$$C_d^* = \left\{ [d(d)]^2 + [2(d V_{AV}^2)]^2 + [d(G)]^2 \right\}^{1/2}$$

For steel a typical accuracy is;

$$\Delta C_d^* = \left\{ (.1)^2 + [2(3.0)]^2 + [.6]^2 \right\}^{1/2} \cong 6\%$$

For plastic a typical accuracy is;

$$\Delta C_d^* = \left\{ (.5)^2 + [2(4.0)]^2 + (2)^2 \right\}^{1/2} \cong \pm 8.75\%$$

APPENDIX II
MIXING THE POLYMER

The polymer used throughout this experiment was Reten 423, a polyacrylamide drag reducing polymer manufactured and supplied by Hercules Inc., and having an approximate molecular weight of 10^{10} . All the polymer used in these experiments came from one batch to minimize variation in polymer properties.

Before mixing, it was necessary to determine the moisture content of the polymer powder. This was done by taking three samples of approximately six grams each and heating them in an oven at 140°C for several hours. The results are shown in table 3.

Sample	Initial Wt.	Final Wt.	% moisture
1	7.276 gm	7.0135 gm	3.21%
2	3.035 gm	3.8479 gm	2.74%
3	5.500 gm	5.264 gm	4.29%

TABLE 3

An average moisture content being about 3.75%, or say 4% for convenience.

The polymer used in the experiments was mixed in bins lined with disposable plastic liners. Bins #4, #5, and #6 contained 149.6 lbm, and bin #3 contained 136.4 lbm of water when filled to a predetermined mark.

A stock solution having a concentration of 2000 Wppm of polymer was required; the appropriate water polymer amounts are; (say for bin #4)

$$\frac{m_p}{m_w} = \frac{2 \times 10^3}{10^6}$$

therefore

$$\begin{aligned} m_p &= m_w \times 2 \times 10^{-3} \\ &= 149.6 \times 2 \times 10^{-3} \\ &= 0.299 \text{ lbm} \end{aligned}$$

allowing for 4% moisture;

$$m_p = 1.04 \times 0.299 = 0.311 \text{ lbm}$$

The polymer was mixed with the water using a Hercules Standard Eductor, and allowed to stand undisturbed for several hours before being gently and very briefly stirred, and again several hours before use. All the polymer batches were allowed to stand at least eighteen hours before use.

When the polymer was required it was transferred from the bins to the reservoir by a hand operated positive displacement pump.

APPENDIX III
CALIBRATION CURVES

The average velocity of the water flowing through the test section was measured using rotameters. Only one of the four incorporated in the apparatus had a calibration curve available that could be used. Two of the remaining three did not have reliable curves and the third one was used to monitor the polymer injection rate, and so required special recalibration.

The calibration of the water rotameters was carried out by measuring the change in the volume of water in a tank of known dimensions while recording the elapsed time. The tank used, was the reservoir of the main flow system.

The dimensions of the tank are;

$$L = 47.75 \pm 0.125 \text{ inches}$$

$$W = 24.0 \pm 0.0625 \text{ inches}$$

$$h = h_1 - h_2 \pm 0.1 \text{ cm.}$$

The height (or depth of water) is measured in centimeters for convenience. Therefore

$$U = 1.628 h \text{ imperial gallons.}$$

The maximum possible error in reading the stop watch was ± 0.1 sec. Some typical results for the large rotameter (#1) are shown in Table 4.

#	$h_1 - h_2$ (cm)	Time (sec)	GPM	Flowmeter
1	20	58.4	33.4	130
2	22	72.0	29.8	120
3	20	77.8	25.1	109
4	20	91.4	21.4	99
5	20	109.4	17.8	90
6	20	139.8	14.0	80
7	20	189.4	10.3	69
8	7	100.0	6.8	59
9	5	131.9	3.7	50
10	1.5	166.5	.88	41

TABLE 4

The error in the flow rate is;

$$\Delta \text{GPM} = \left\{ (\Delta L)^2 + (\Delta W)^2 + (\Delta T)^2 \right\}^{1/2}$$

For reading #1;

$$\Delta \text{GPM} = \left\{ \left(\frac{.125}{47.75} \right)^2 + \left(\frac{.0625}{24.00} \right)^2 + \left(\frac{.1}{20} \right)^2 + \left(\frac{.1}{58.4} \right)^2 \right\}^{1/2} = \pm .64\%$$

For reading #9;

$$\Delta \text{GPM} = \left\{ \left(\frac{.125}{47.75} \right)^2 + \left(\frac{.0025}{24.00} \right)^2 + \left(\frac{.1}{5} \right)^2 + \left(\frac{.1}{131.9} \right)^2 \right\}^{1/2} = \pm 2.0\%$$

The smallest rotameter was also calibrated using this tank and typical results are summarized in table 5. Since the same tank was used to calibrate both flowmeters the errors can be expected to be similar. For reading #1, in table 5;

$$\Delta \text{GPM} = \left\{ \left(\frac{.125}{47.75} \right)^2 + \left(\frac{.0025}{24.00} \right)^2 + \left(\frac{.0625}{2.875} \right)^2 + \left(\frac{.1}{350} \right)^2 \right\}^{1/2} = \pm 2.21\%$$

For reading #10;

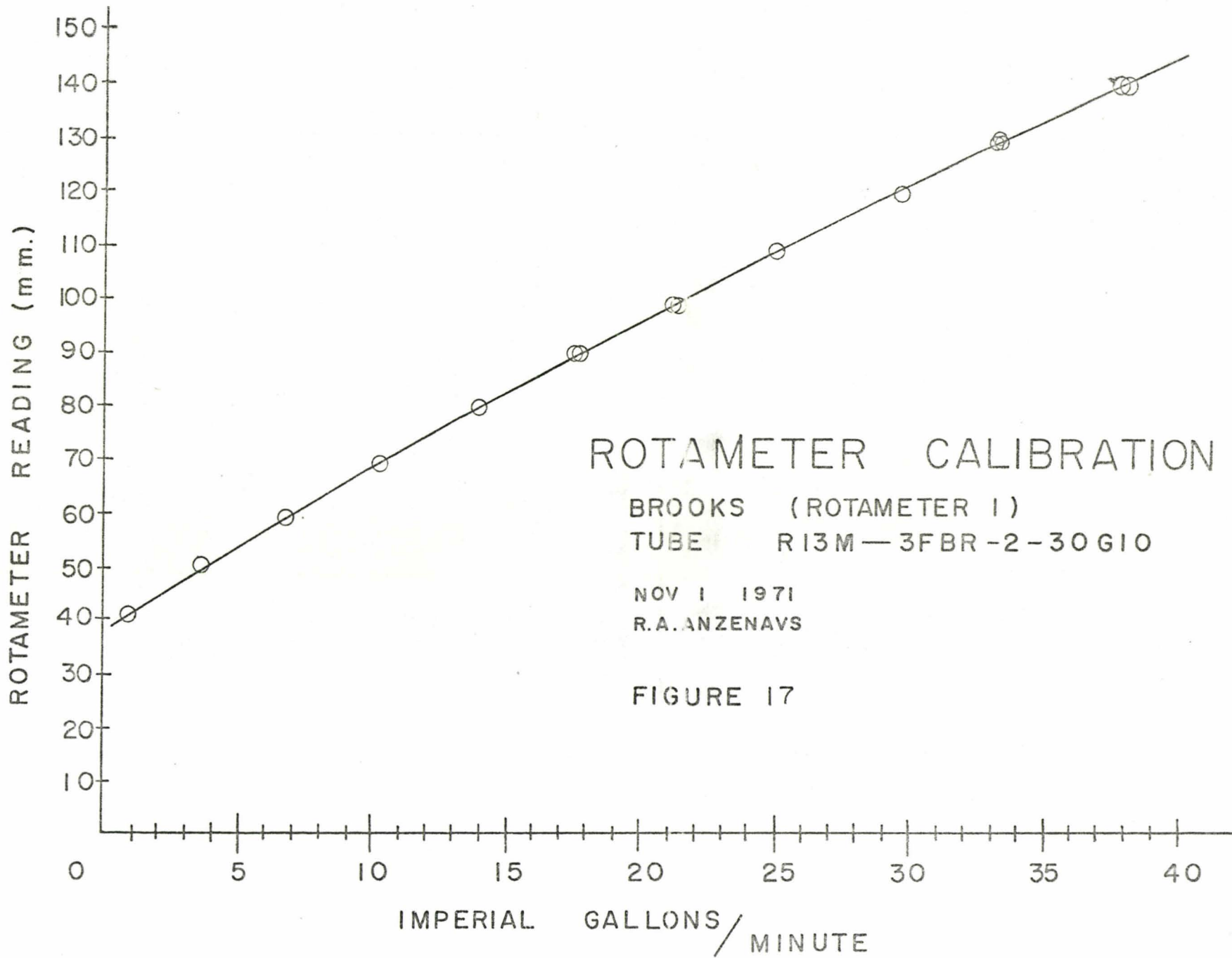
$$\Delta \text{GPM} = \left\{ \left(\frac{.125}{47.75} \right)^2 + \left(\frac{.0625}{24.00} \right)^2 + \left(\frac{.0625}{0.500} \right)^2 + \left(\frac{.1}{180} \right)^2 \right\}^{1/2} = \pm 12.5\%$$

#	Gallons	Time (Minutes)	GPM	Flowmeter
1	2.065	5.83	.35	1.1
2	4.131	5.82	.71	3.1
3	4.647	4.32	1.07	4.95
4	7.229	4.86	1.48	7.03
5	6.713	3.59	1.87	9.05
6	10.844	4.79	2.26	11.1
7	8.262	3.08	2.68	13.15
8	10.327	3.33	3.10	15.0
9	6.713	2.90	2.31	16.95
10	11.877	2.93	4.05	19.45
11	11.877	2.57	4.62	22.20
12	11.360	2.15	5.27	24.50

TABLE 5

The third rotameter came with a calibration curve supplied by the manufacturer. The calibration curves for all the rotameters are shown in figures 17, 18 and 19.

It was necessary to recalibrate a flowmeter for use with the polymer solution. This was done by preparing a stock solution of 2000 Wppm of the polymer that would be used in experiments under exactly the same conditions as would be found in the experiments. The apparatus was assembled exactly as it would be when the experiments would be performed except that



ROTAMETER CALIBRATION

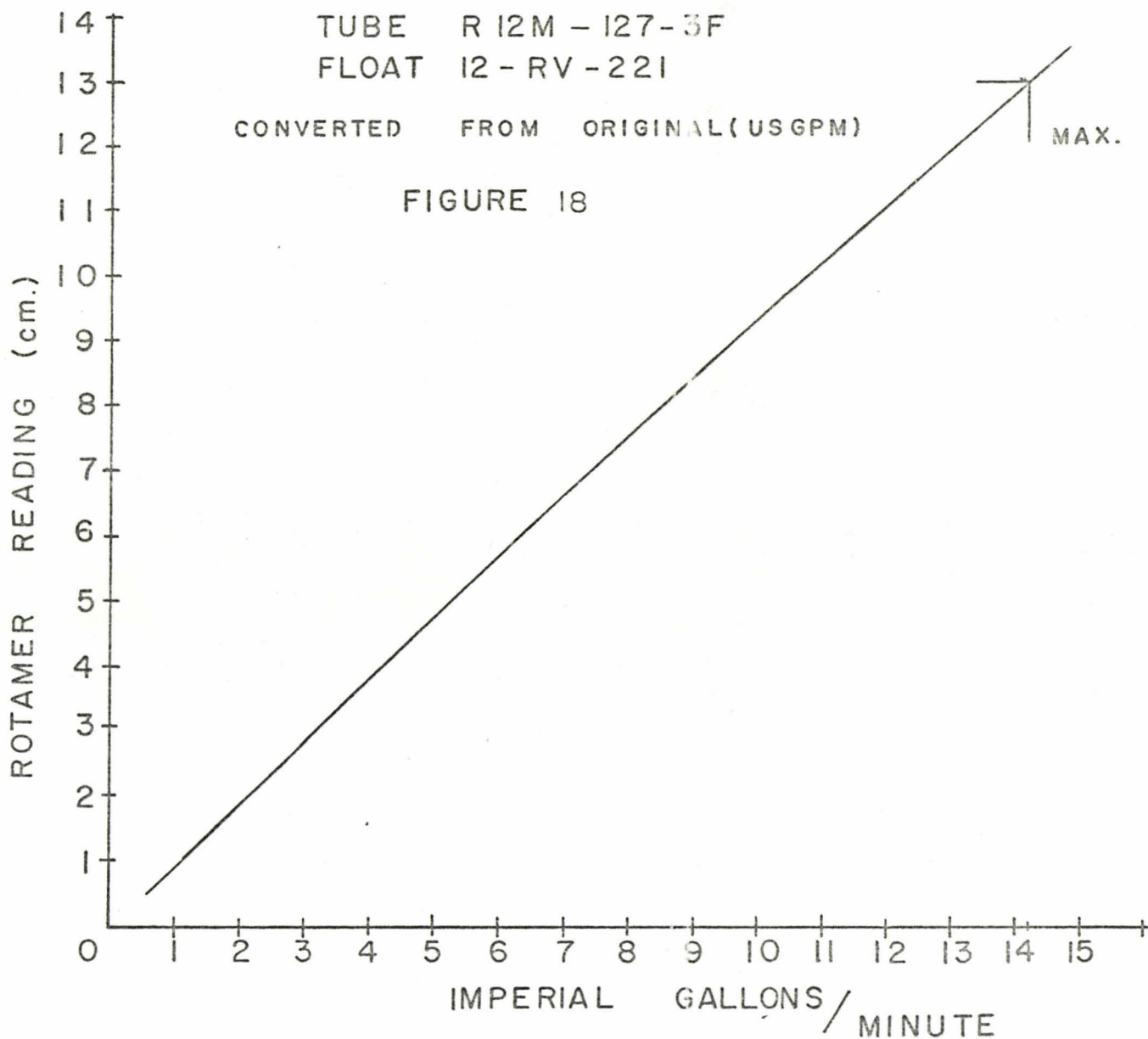
BROOKS (ROTAMETER 2)

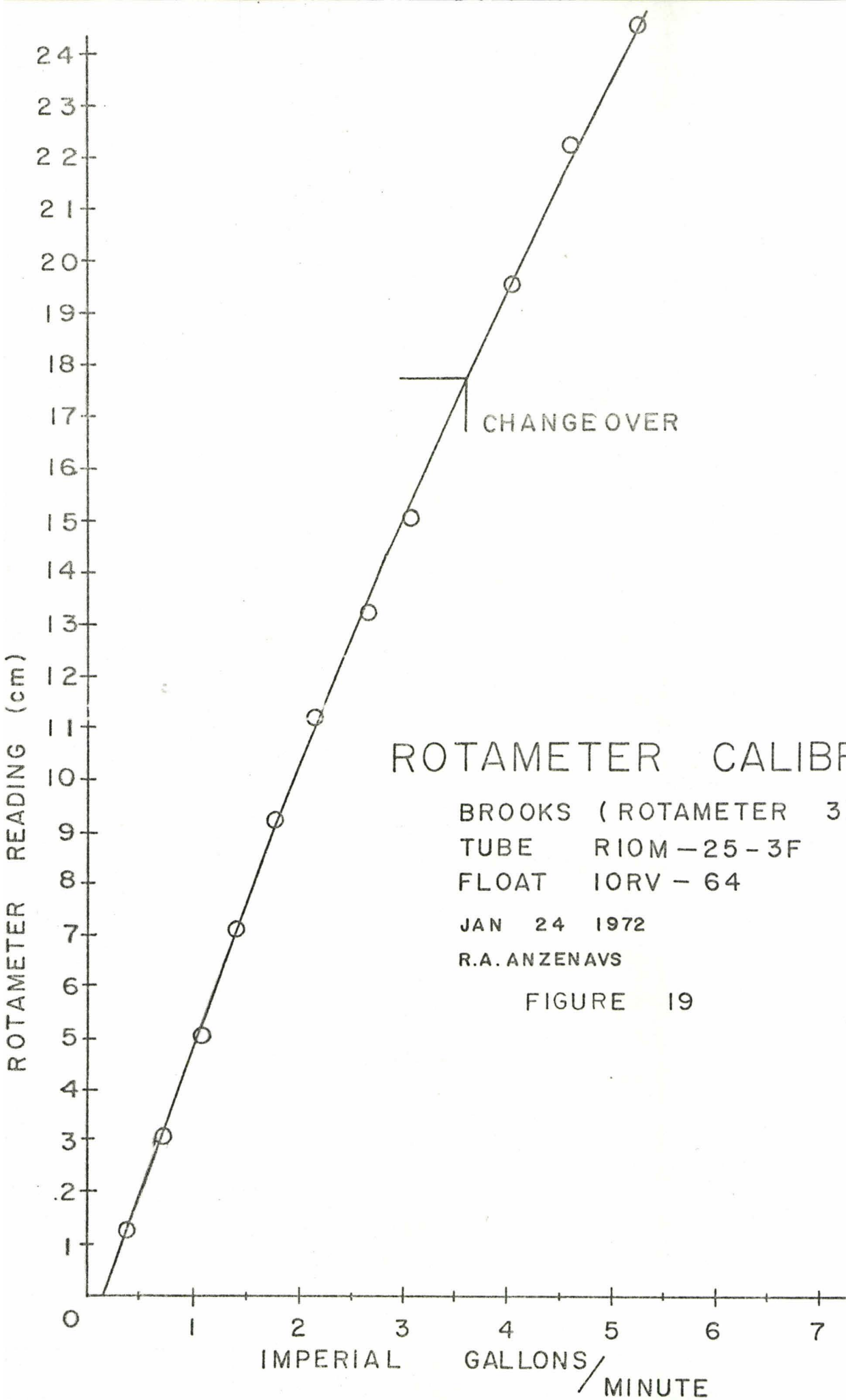
TUBE R 12M - 127-3F

FLOAT 12 - RV - 221

CONVERTED FROM ORIGINAL (USGPM)

FIGURE 18





ROTAMETER CALIBRATION

BROOKS (ROTAMETER 3)

TUBE RIOM-25-3F

FLOAT IORV-64

JAN 24 1972

R.A. ANZENAUS

FIGURE 19

POLYMER ROTAMETER CALIBRATION

RETEN 423 CONCENTRATION

2000 Wppm

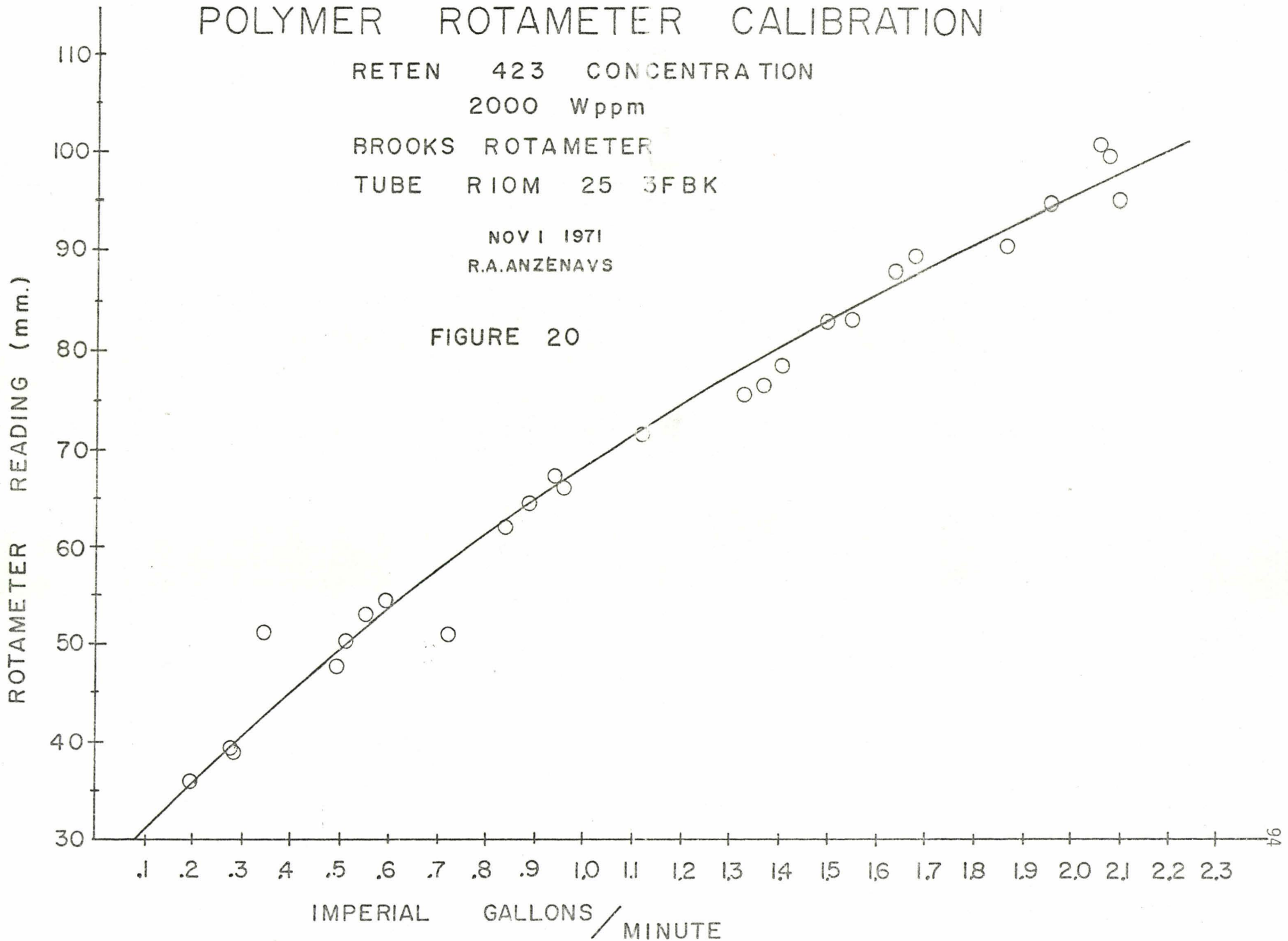
BROOKS ROTAMETER

TUBE RIOM 25 3FBK

NOV 1 1971

R.A.ANZENAVS

FIGURE 20



the discharge from the rotameters was hooked into a tank calibrated in imperial gallons. A series of measurements of volume discharged against time were taken as with the other rotameters and the results are shown in figure 20.

During the course of the calibration it was found that both aging and mixing of the polymers had a profound effect on the accuracy of the results, and therefore great care was taken during the calibration procedure to ensure that the results were truly representative of 2000 Wppm polymer used.

An estimate of the error in the calibration of the flowmeter is not presented because the errors caused by reading the stop watch and the tank volume are far less than the error caused by variation in the polymer properties. Hence the error in the rotameter is taken as being represented by the scatter in the points.

Once all the rotameters were calibrated it was necessary to make a cross reference chart that showed the appropriate flow meter settings for a given concentration.

Referring to figure 21; for 10 Wppm in the test section.

$$\frac{m_p}{m_2} = 2 \times 10^{-3} \quad \text{- stock solution}$$

$$\frac{m_p}{m_1 + m_2} = 10^{-5} \quad \text{- desired concentration}$$

therefore

$$\frac{m_1 + m_2}{m_2} = \frac{2 \times 10^{-3}}{10^{-5}} = 200$$

therefore

$$m_2 = \frac{m_1}{200} + \frac{m_2}{200}$$

and
$$m_2 = m_1 \left[\frac{1}{200 - 1} \right]$$

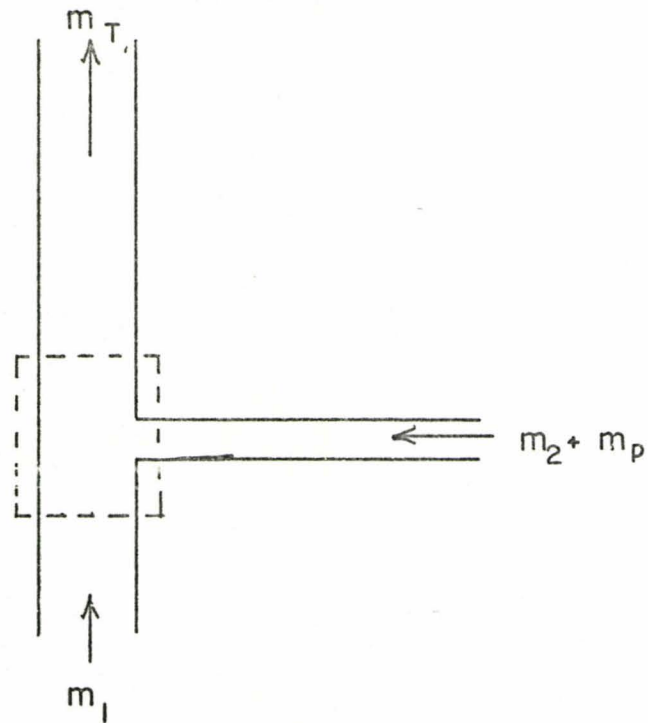


FIGURE 21

For 25 Wppm;

$$\frac{m_1 + m_2}{m_2} = \frac{2 \times 10^{-3}}{2.5 \times 10^{-5}} = 80$$

For the pertinent concentrations;

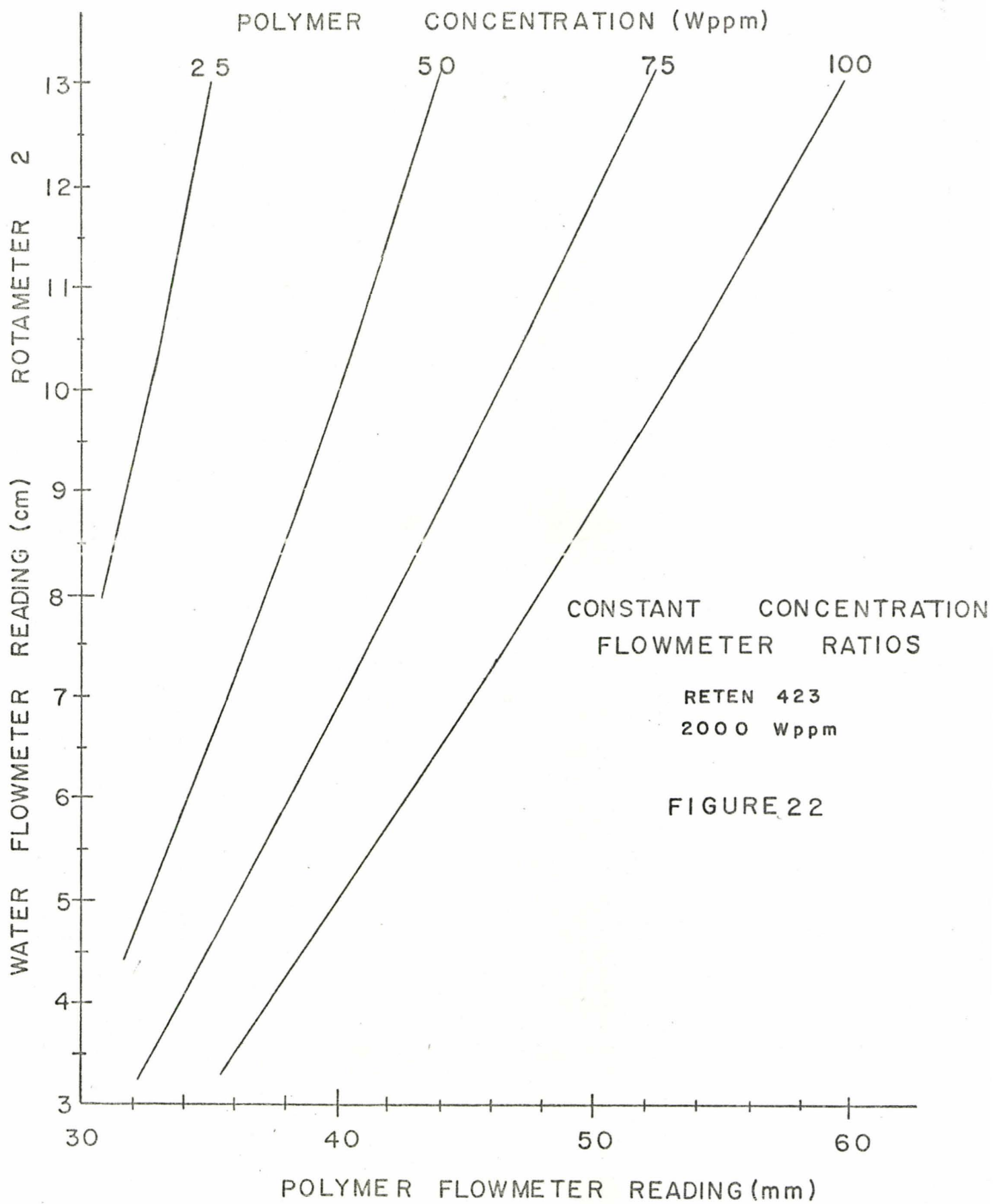
Conc. (Wppm)	10	25	50	75	100
$m_1 + m_2/m_2$	200	80	40	26.75	20
m_2 in terms of m_1	$\frac{1}{200 - 1}$	$\frac{1}{80 - 1}$	$\frac{1}{40 - 1}$	$\frac{1}{26.75 - 1}$	$\frac{1}{20 - 1}$

TABLE 6

Table 7 summarizes the necessary calculations to obtain a cross reference chart. Figures 22 and 23 show the flow meter setting for the required concentrations as calculated in Table 7.

Main Flowmeter m_1		10 Wppm		25 Wppm		50 Wppm		75 Wppm		100 Wppm	
Rot.	GPM(m_1)	GPM(m_2)	Rot.	GPM(m_2)	Rot.	GPM(m_2)	Rot.	GPM(m_2)	Rot.	GPM(m_2)	Rot.
140	38.2	.192	33.5	.484	49.2	.98	67.8	1.48	82.4	2.01	95.7
130	33.9	.170	34.5	.429	76.9	.869	64.0	1.315	78.0	1.782	90
120	29.69	.149	33.5	.376	44.8	.760	60.0	1.151	73.0	1.562	84.5
110	25.50	.128	32.5	.323	42.1	.654	56.0	.99	68.0	1.341	78.6
100	21.55			.272	39.5	.551	52.0	.835	63.0	1.131	72.4
90	17.80			.225	37.5	.456	48.1	.69	57.3	.936	66.0
80	14.25			.181	35.0	.365	44.3	.554	52.0	.75	59.6
70	10.75			.136	33.0	.276	39.3	.417	76.2	.569	52.8
60	7.25					.186	35.5	.282	40.0	.382	44.8
50	3.65							.142	33.0	.192	35.6

TABLE 7



POLYMER CONCENTRATION (Wppm)

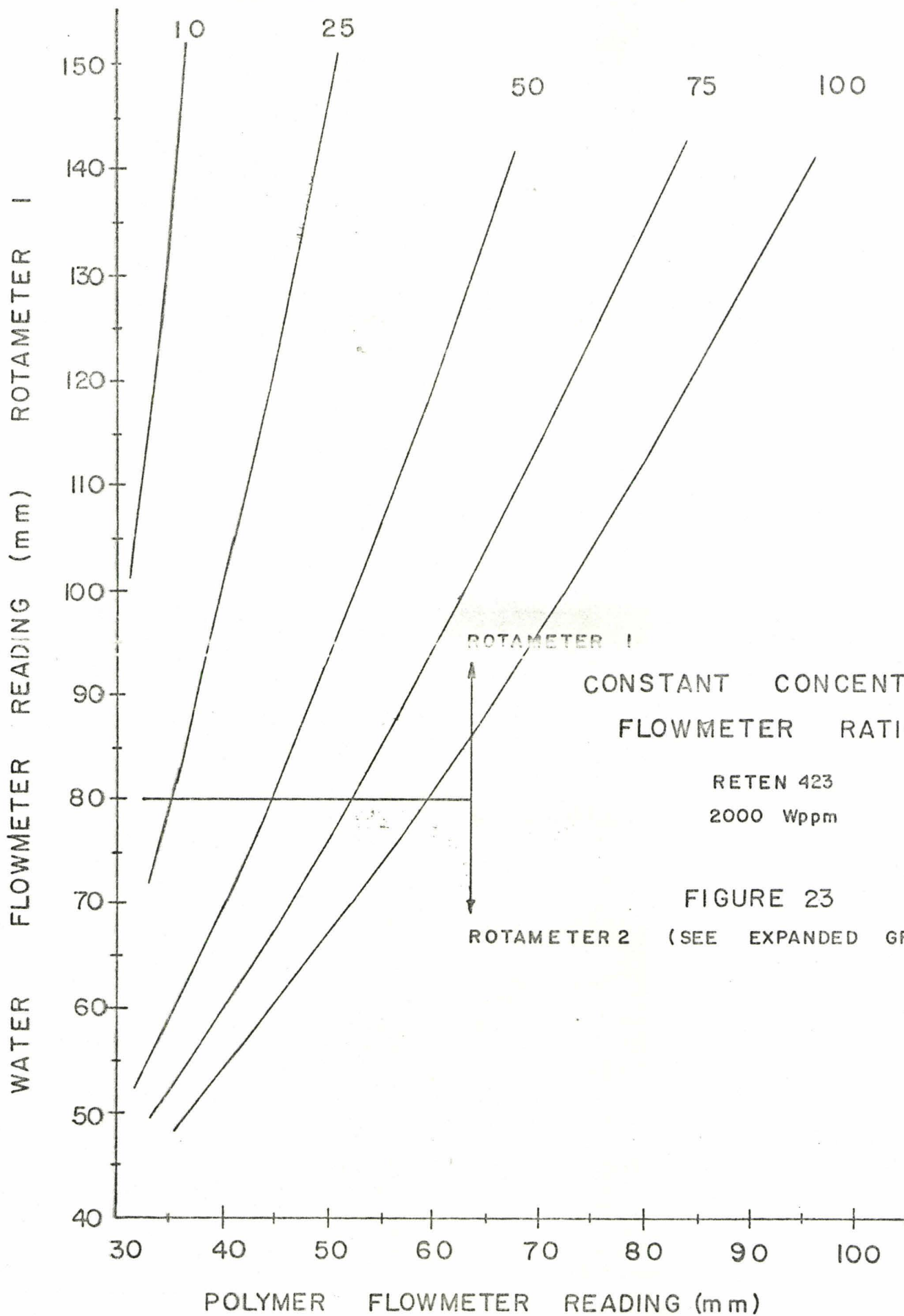


FIGURE 23
ROTAMETER 2 (SEE EXPANDED GRAPH)

APPENDIX IV

DETERMINATION OF THE INSIDE DIAMETER OF THE TEST SECTION

From the error analysis performed in Appendix I it can be seen that the diameter of the test section enters into the friction factor calculations to the fifth power. It is therefore important that an accurate value for the diameter be known. To determine this, the test section was filled with water to approximately 80% of its length, the length noted, and the volume of water discharged measured using a graduated cylinder. This procedure was repeated twice.

Because of their relatively small size it was obvious that the bell shaped entrances to the pressures taps had negligible effect on the measurements, hence they were neglected. Table 8 summarizes the results.

TABLE 8

U_1 (litres)	U_2 (litres)	\bar{U} (litres)	L (inches)	D (ft)	
4.452	4.453	4.453	80.94	0.1634	TUBE 1
4.063	4.061	4.062	84.00	0.1615	TUBE 2

APPENDIX V

PRESSURE GRADIENT WITHIN THE TEST SECTION

It was demonstrated in the chapter on theory (chapter III) that the pressure gradient due to the liquid alone is an important part of the calculation of pressure drop across the spheres or sphere trains. Furthermore the measurement itself provides an indication of the kind of accuracy that can be expected from the equipment.

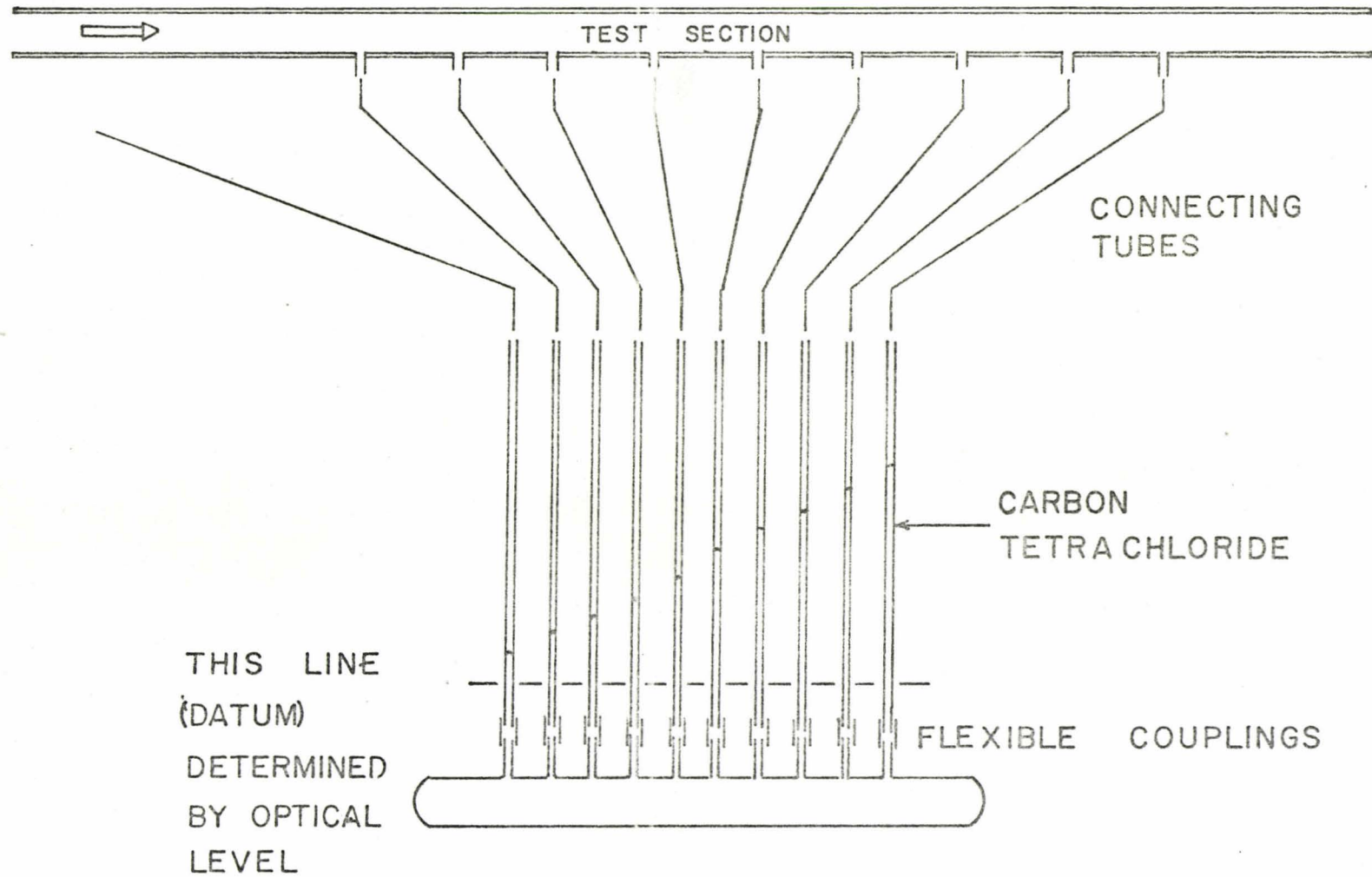
When the polymer is injected it would also be expected that the pressure gradient would change, since the polymer is a friction reducing agent. The amount of change being an indication of the polymer's effectiveness.

The first phase of this study was to determine if the flow in the test section was developed. This was done by measuring the pressure gradient along the length of pipe. Where the flow is developed that pressure gradient becomes constant. To determine this, the vertical section of the apparatus had pressure taps fitted at frequent intervals, and a bank of inclined manometers were used to measure a continuous pressure gradient between the taps.

Figure 24 shows the manometer used, and figure 25 shows the pressure at each station. From these figures it can be seen that flow in the test section is fully developed, but that the flange and the change in diameter at the entrance to the test section causes a slight disturbance. For subsequent tests the bank of manometers and the series of readings were discarded and only two pressure taps, located four and five feet apart depending on the tube, were used to make the measurements.

MANOMETER SCHEMATIC

FIGURE 24

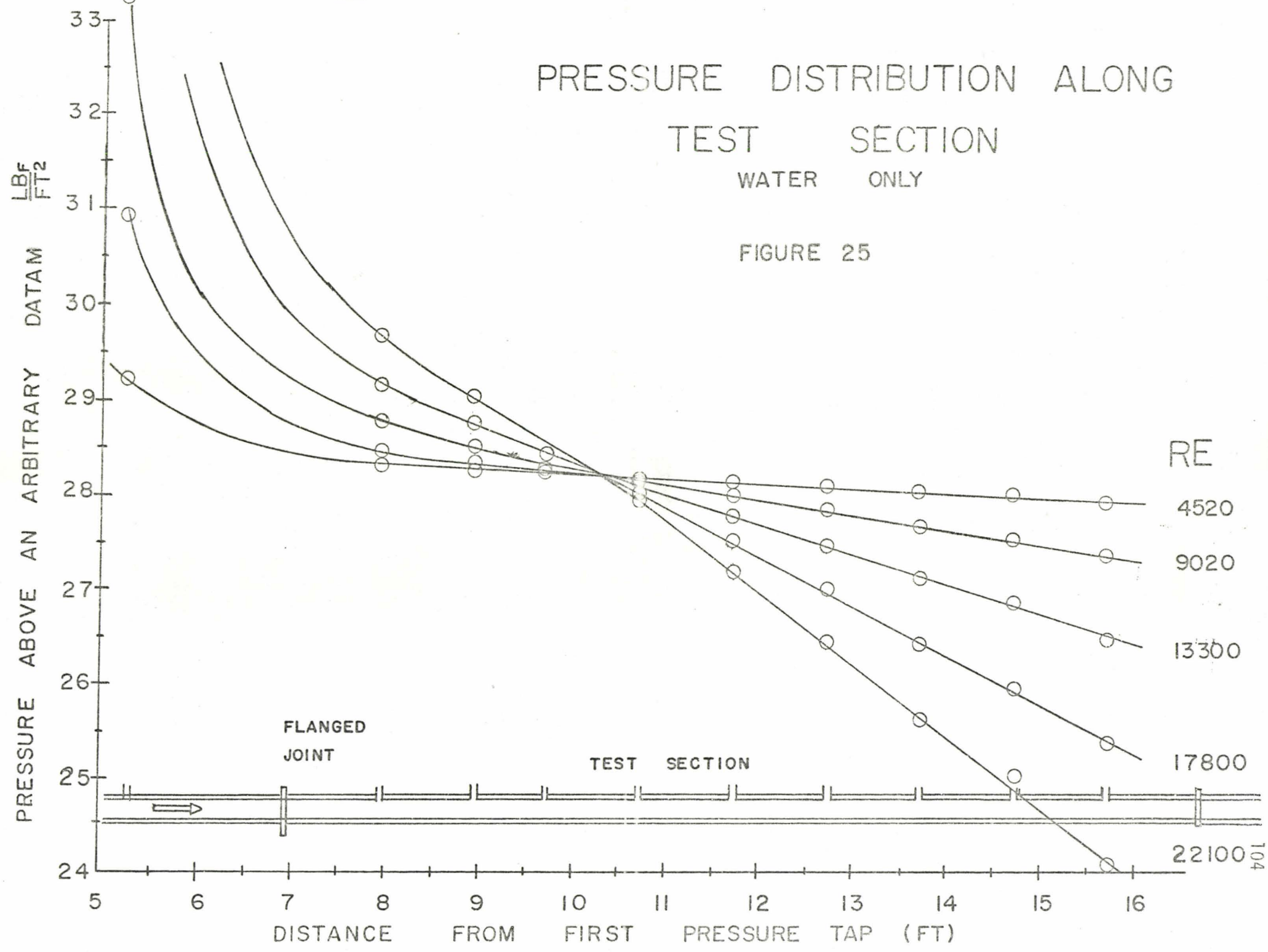


PRESSURE DISTRIBUTION ALONG

TEST SECTION

WATER ONLY

FIGURE 25



RE

4520

9020

13300

17800

22100

FLANGED
JOINT

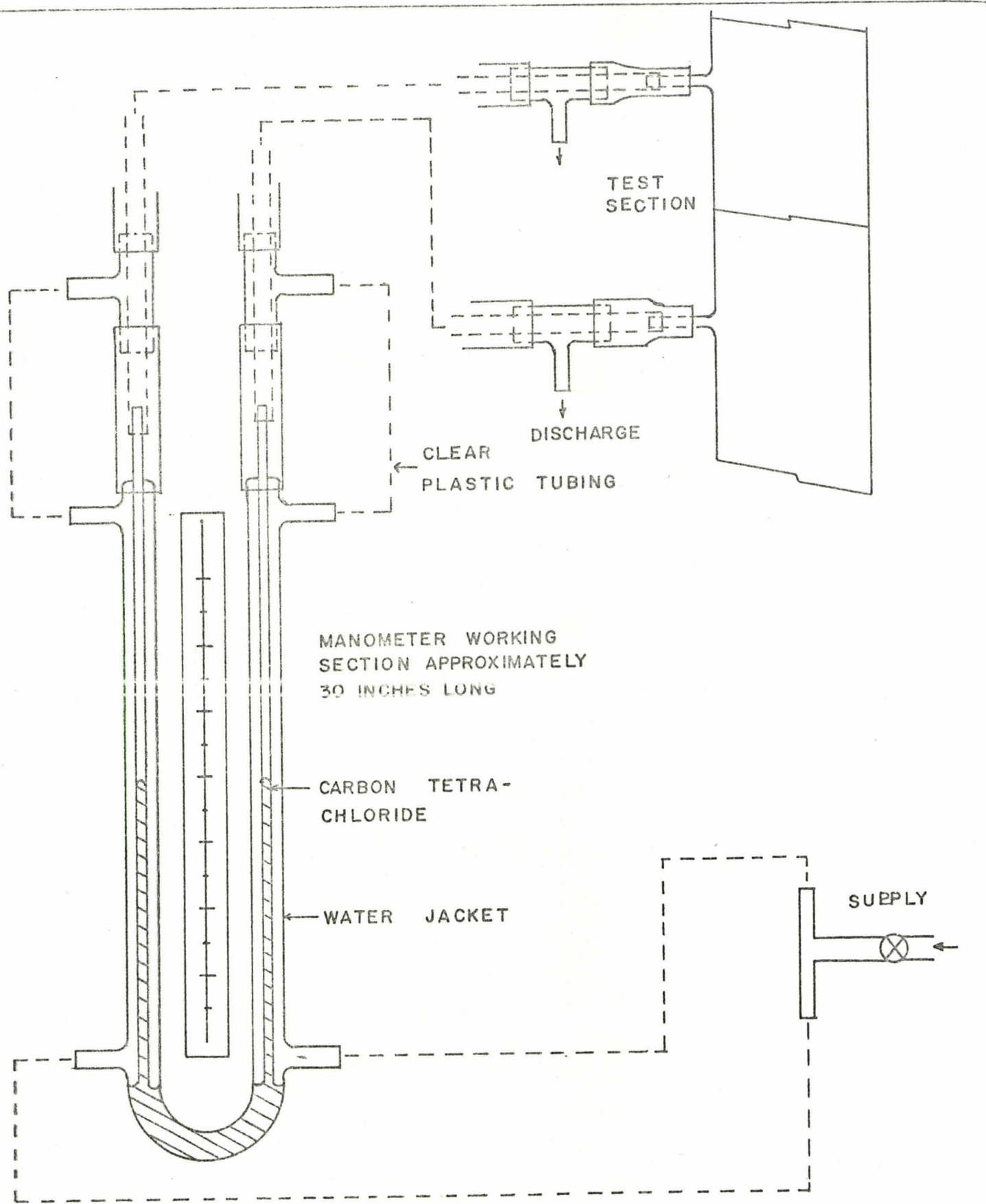
TEST SECTION

PRESSURE ABOVE AN ARBITRARY DATUM
LBF/FT²

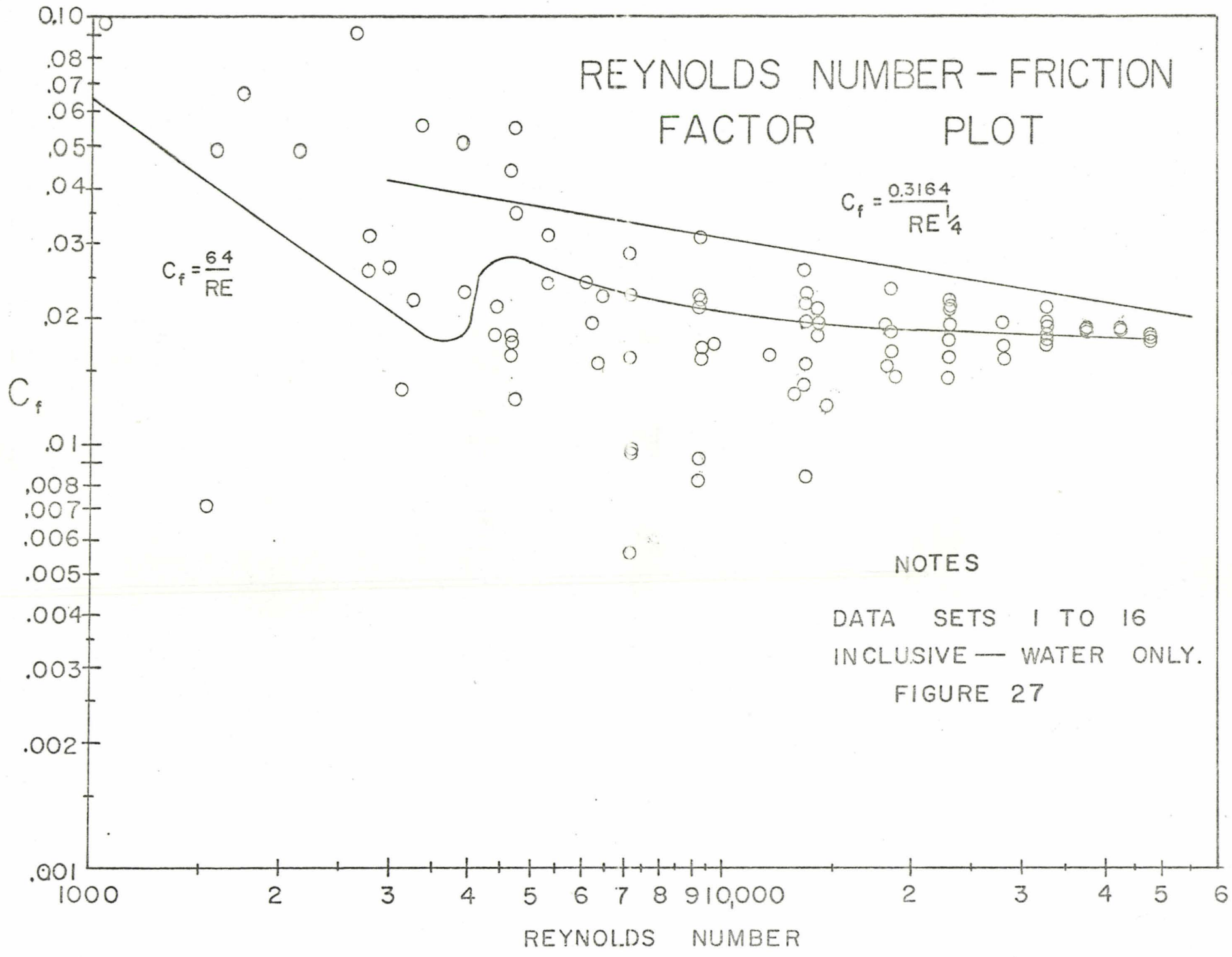
33
32
31
30
29
28
27
26
25
24

5 6 7 8 9 10 11 12 13 14 15 16

DISTANCE FROM FIRST PRESSURE TAP (FT)



MANOMETER SCHEMATIC
FIGURE 26



NOTES

DATA SETS 1 TO 16
INCLUSIVE — WATER ONLY.
FIGURE 27

From the chapter on errors, Appendix I, it can be seen that very large errors are to be expected at low Reynolds numbers, decreasing exponentially as the Reynolds number increases. The three main sources of this error are the error in the average velocity, the error in the diameter of the pipe, and the error in the pressure drop.

The first error, by careful calibration was reduced to a minimum, and the error in the pipe diameter was similarly reduced to virtually a negligible amount. However, the error in the pressure drop was difficult to reduce. A special manometer was developed, and is shown in figure 26. The inside diameter of this manometer was three millimeters to ensure that at low angles of inclination the meniscus would not deform, and would maintain the same shape as it had at higher angles. It was found that the temperature difference between the test section and manometer could cause a reading on the manometer when there was no flow. To overcome this the entire manometer assembly, that is manometer plus connecting tubes were enclosed in a water jacket that maintained the temperature close to that found in the test section. However even with these precautions the initial reading could not be eliminated entirely.

To estimate the magnitude of the temperature effects, consider the situation shown in figure 28.

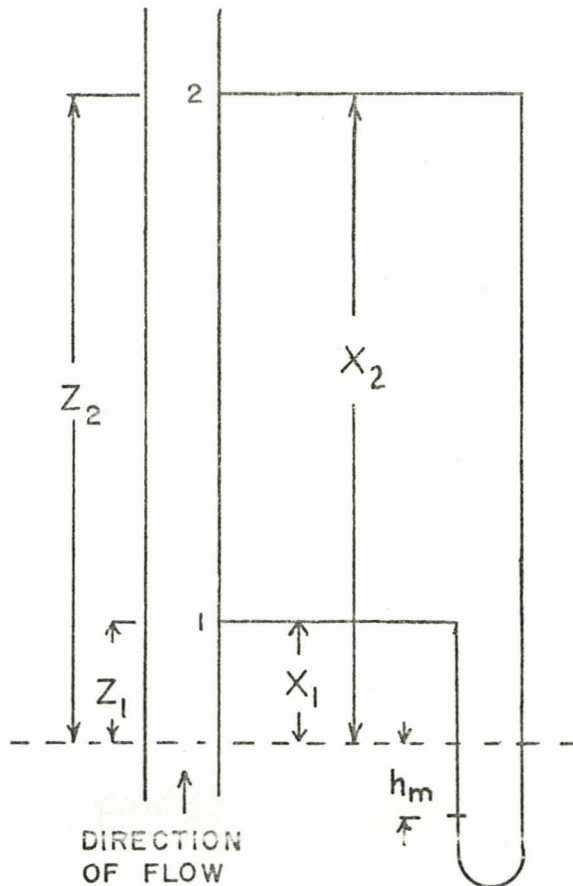


FIGURE 28

Applying the Bernoulli's equation between points 1 and 2,

$$\frac{V_1^2}{2g} + \frac{P_1}{\gamma_T} + Z_1 = \frac{V_2^2}{2g} + \frac{P_2}{\gamma_T} + Z_2 + h_f$$

and assuming that $V_1 = V_2$, then;

$$h_f = \frac{P_1 - P_2}{\gamma_T} + (Z_1 - Z_2) \quad (5.1)$$

Consider now the closed loop, starting from point 1 and going around the manometer to point 2.

$$P_1 + x_1 \gamma_c + h_m \gamma_c - h_m \gamma_m - x_2 \gamma_c = P_2$$

Therefore

$$P_1 - P_2 = \gamma_c (x_2 - x_1) + h_m (\gamma_m - \gamma_c) \quad (5.2)$$

Substituting these results into equation (5.1);

$$h_f = \gamma_c \frac{(x_2 - x_1)}{\gamma_T} + h_m \frac{(\gamma_m - \gamma_c)}{\gamma_T} + (Z_1 - Z_2) \quad (5.3)$$

and letting $Z_1 - Z_2 = \Delta Z$, then;

$$h_f = \Delta Z \left(\frac{\gamma_c}{\gamma_T} - 1 \right) + h_m \left(\frac{\gamma_m - \gamma_c}{\gamma_T} \right) \quad (5.4)$$

In order to determine what the no flow manometer reading is, put $h_f = 0$;

and let the reading be represented by $(h_m)_0$;

$$(h_m)_0 = \Delta Z \left(\frac{\gamma_T - \gamma_c}{\gamma_m - \gamma_c} \right) \quad (5.5)$$

For a test section length of five feet, and assuming that the manometer and connecting tubes are at room temperature while the test section is at 5°C, then;

$$\gamma_c = 0.99707$$

$$\gamma_T = .99999$$

$$\gamma_m = 1.5934$$

therefore

$$\begin{aligned} (h_m)_0 &= 5.0 \left(\frac{.99999 - .99707}{1.5934 - .99707} \right) \\ &= 0.0268 \text{ ft of water} \end{aligned}$$

Converting this to a manometer reading;

$$h_m = \frac{30.48 \Delta P}{(62.4)(\gamma_m - \gamma_c) \sin \theta} \text{ cm. of fluid.}$$

For the zero reading calculated above

$$\Delta P = 0.0268 \times 62.4 = 1.673 \text{ lb}_F/\text{ft}^2$$

therefore

$$(h_m)_0 = \frac{30.48 \times 1.673}{(62.4)(1.5934 - .99707)(.275)} = 4.98 \text{ cm.}$$

Thus at a manometer inclination of 16° (the usual value throughout the test) and for carbon tetrachloride under water, a zero reading as large as 5 cm. could be expected.

By adding the water jacket the temperature of the connecting tubes and manometer could be maintained close to that of the test section, and the zero reading could be reduced to approximately 1 to 2 cm., but could not be eliminated entirely because of the heat loss from the water jacket.

To obtain the form of the equation to calculate the pressure drop which incorporates this zero reading, consider the following equation;

$$(h_m)_0 = \Delta Z \left[\frac{\gamma_T - \gamma_c}{\gamma_m - \gamma_c} \right] \quad (5.6)$$

or
$$\Delta Z \left(\frac{\gamma_c - \gamma_T}{\gamma_T} \right) = \left(\frac{\gamma_c - \gamma_m}{\gamma_T} \right) (h_m)_0 \quad (5.7)$$

Substituting equation (5.7) into equation (5.4);

$$h_f = \left(\frac{\gamma_c - \gamma_m}{\gamma_T} \right) h_{m0} + h_m \left(\frac{\gamma_m - \gamma_c}{\gamma_T} \right)$$

or

$$h_f = \left(\frac{\gamma_m - \gamma_c}{\gamma_T} \right) (h_m - h_{m0})$$

To calculate the friction factor, the head loss from points 1 to 2 is required; then

$$C_f = \frac{hf}{\left(\frac{L}{D} \right) \frac{\rho V^2}{2g_c}}$$

and substituting;

$$C_f = \frac{62.4 \left(\frac{\gamma_m - \gamma_c}{\gamma_T} \right) \frac{(h_m - h_{m0}) \sin \theta}{30.48}}{\left(\frac{L}{D} \right) \frac{\rho V^2}{2g_c}}$$

where h_m and h_{m0} are in centimeters. This equation has been used to calculate the friction factor as a function of the Reynolds number. Figure 27 shows the results obtained for this apparatus.

Using the relationships

$$C_f = \frac{64}{R_e}$$

and

$$C_f = \frac{0.3164}{R_e^{1/4}}$$

a deviation plot has been obtained and is compared with the predicted error of Appendix I, (see figure 16).

It can be seen that for laminar flow the results are very poor. However in this region

$$C_f = \frac{64}{R_e}$$

is known to hold rigorously and thus for the purpose of further calculations the pressure drop can be obtained exactly.

At a Reynolds number of 44,000 where because of the large values to be measured the accuracy would be expected to be better than for the low Reynolds number range, the friction factor is still below the expected value. In fact it appears to be about 10% consistently low with a scatter commensurate with the error analysis. This possibly indicates that the flow is somehow altered resulting in a decreased friction factor. In fact the measurements of the diameter of the test section indicate that the test section is barrel-shaped to a slight degree; it is possible that this slight divergence of flow as it enters the test section is responsible for the decreased friction

factor. Because the results appear consistently low it was decided to use the experimental results rather than the Blasius correlation.

Since part of the tests were to be carried out using polymer rather than pure water, and since polymer alters the pressure gradient it was important that a good friction factor, Reynolds number curve for polymer be obtained.

The tests for polymer were carried out in the same manner as those for water, and the friction factor was calculated using the same computer program. The tests were performed for polymer concentrations of 10, 25, 50, 75, and 100 Wppm. The results are shown in figure 29.

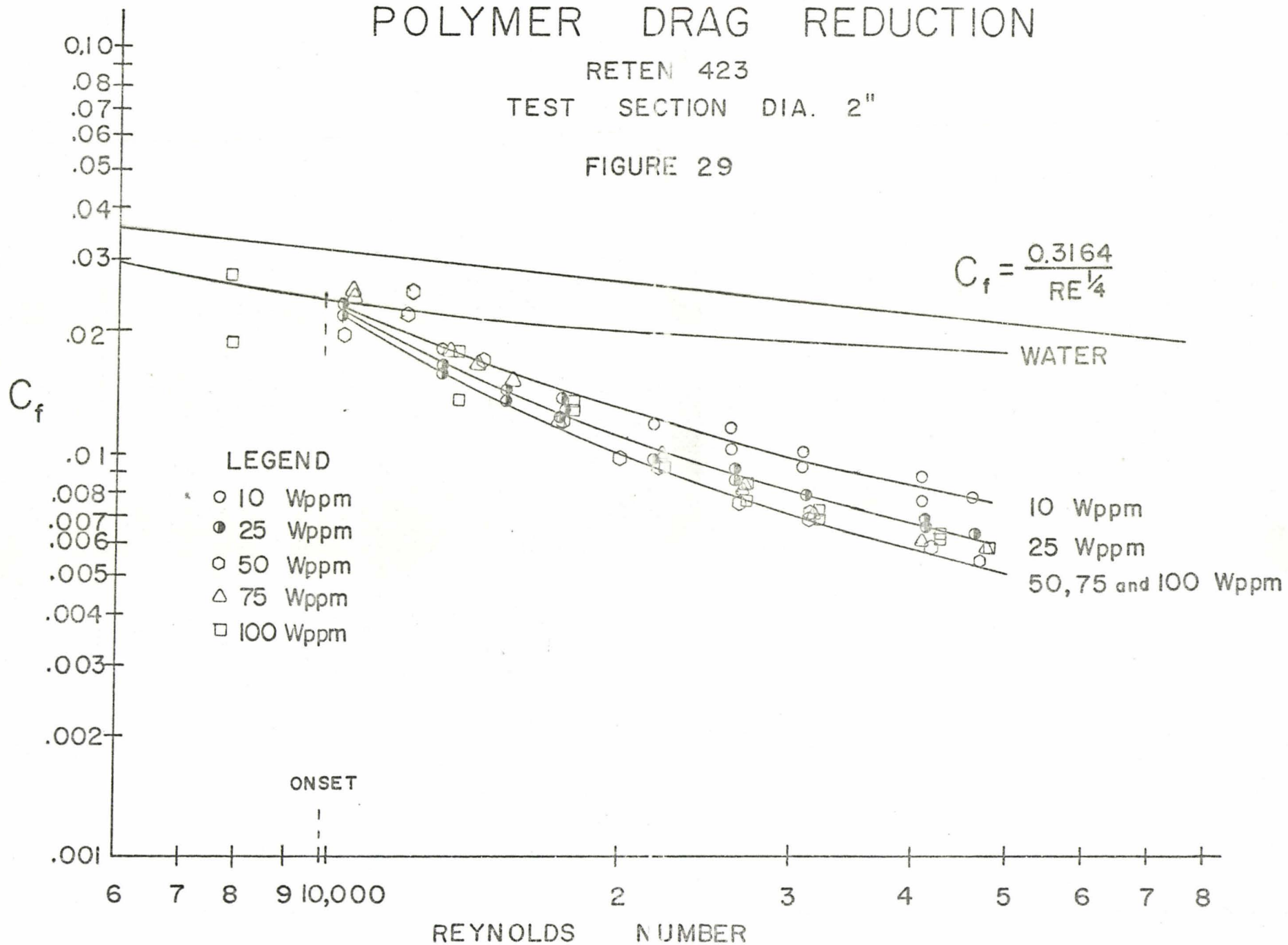
Perhaps because the polymer tests were performed at higher Reynolds numbers the error was less, but the scatter in the polymer data appears less than that for water. It is also evident that maximum drag reduction occurs at a concentration of about 50 Wppm.

POLYMER DRAG REDUCTION

RETEN 423

TEST SECTION DIA. 2"

FIGURE 29



APPENDIX VI
PROPERTIES OF THE POLYMER

Part of this experimental study was devoted to the examination of the effects a drag reducing solution has on a sphere hydrodynamically supported within a pipe. The substance used to achieve drag reduction was a polyacrylamide having a trade name Reten 423, and produced by Hercules Inc. This polymer has only recently been developed and therefore some effort was devoted to a study of its properties.

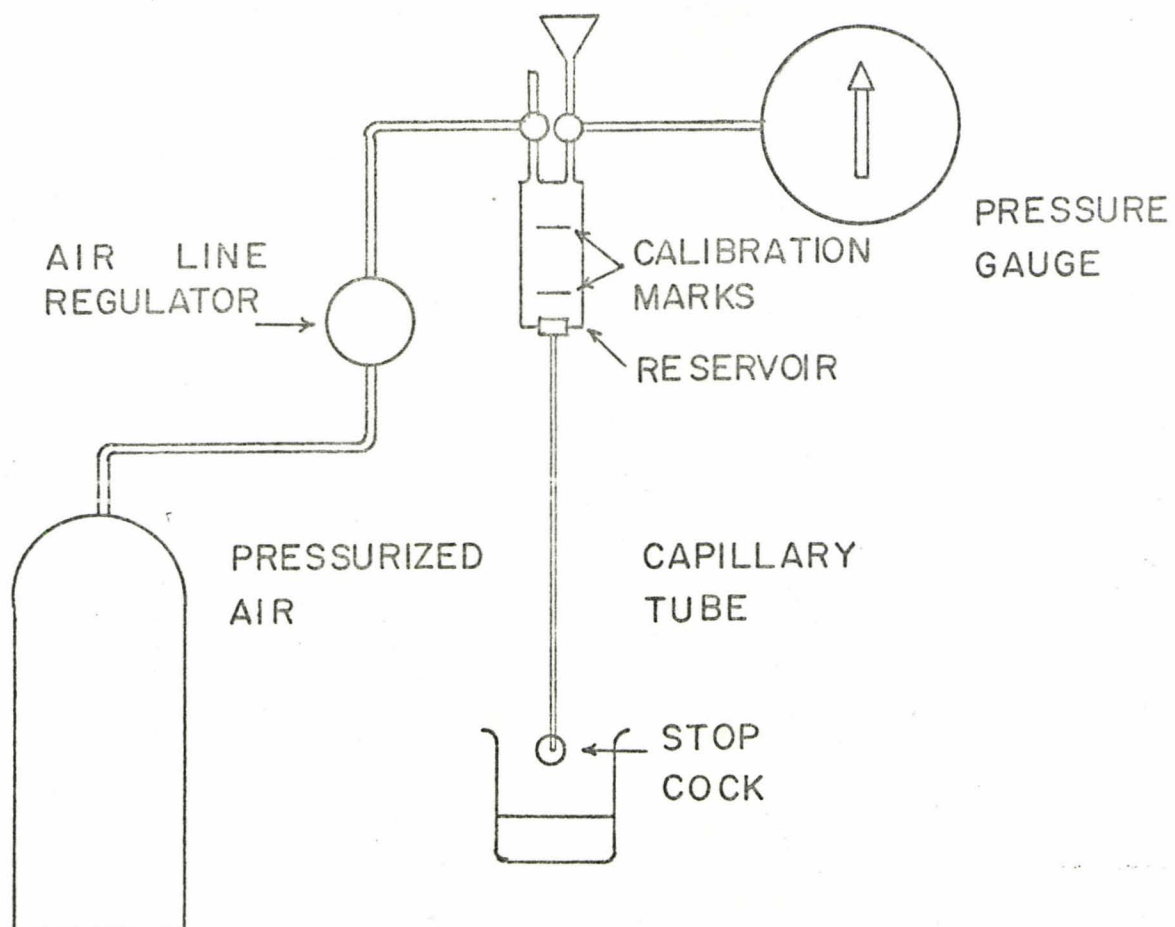
There are many tests that can be performed on the polymer, however those of a chemical nature are exceedingly difficult and tiresome to perform. For the purposes of this study only simple tests that reveal the physical properties of the polymer will be performed. These include firstly determining the change of physical properties of the polymer with time and secondly its rheological categorization, and finally its drag reducing properties in tubes of different sizes.

The instruments used to perform the tests are: a Brookfield cone and plate viscometer model LVT-CP, a capillary tube viscometer (sometimes referred to as a Hoyt Rheometer), and the two inch diameter main test section.

The first property studied was that of variation of drag reducing properties with time. According to that manufacturer several hours should be allowed to elapse between the time the polymer is mixed and used, to allow the polymer molecules to "relax". If the polymer is used immediately after it is mixed it has been observed that its drag reducing properties are not nearly as great as when it has been allowed to stand for several hours.

CAPILLARY TUBE VISCOMETER

FIGURE 30



In order to know how long the polymer must be allowed to "relax" a batch was mixed under the usual conditions and samples taken at regular time intervals and the apparent viscosity of each sample measured using the cone and plate viscometer.

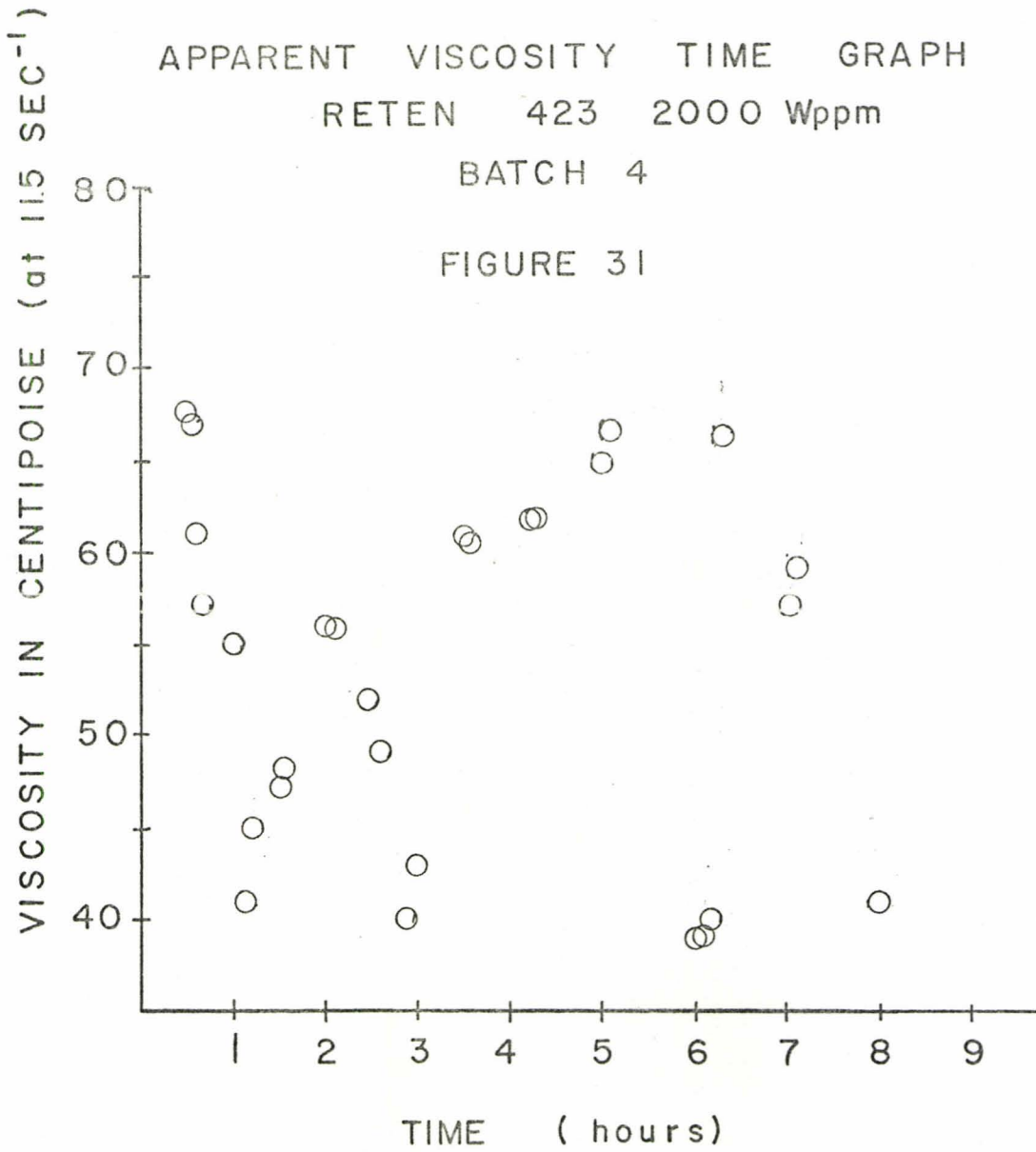
This instrument measures the proportionality constant in the equation

$$\tau = \mu \frac{du}{dy} \quad (6.1)$$

which makes the results of the polymer tests somewhat qualitative, in that the above equation is applicable only to laminar flow in Newtonian fluids. However, concentrated polymer solutions are non-Newtonian, that is μ is not a constant. Nevertheless it was felt that if μ were measured at a given shear rate ($\frac{du}{dy} = 11.5 \text{ sec}^{-1}$) its values would be an indication of the state of relaxation of the polymer.

Many such tests were performed, and a typical result is shown plotted in figure 31. Different batches varied widely, although the trend indicated in figure 31 was evident in most. In all cases the apparent viscosity dropped sharply in the first hour, climbed again briefly, then dropped and resumed its climb. The peak was generally reached after about six hours after the time of mixing, and maintained. Occasionally the apparent viscosity dropped some time after reaching the peak, although this was not a phenomenon that was always observed. Consequently no batch was used before being aged at least eighteen hours.

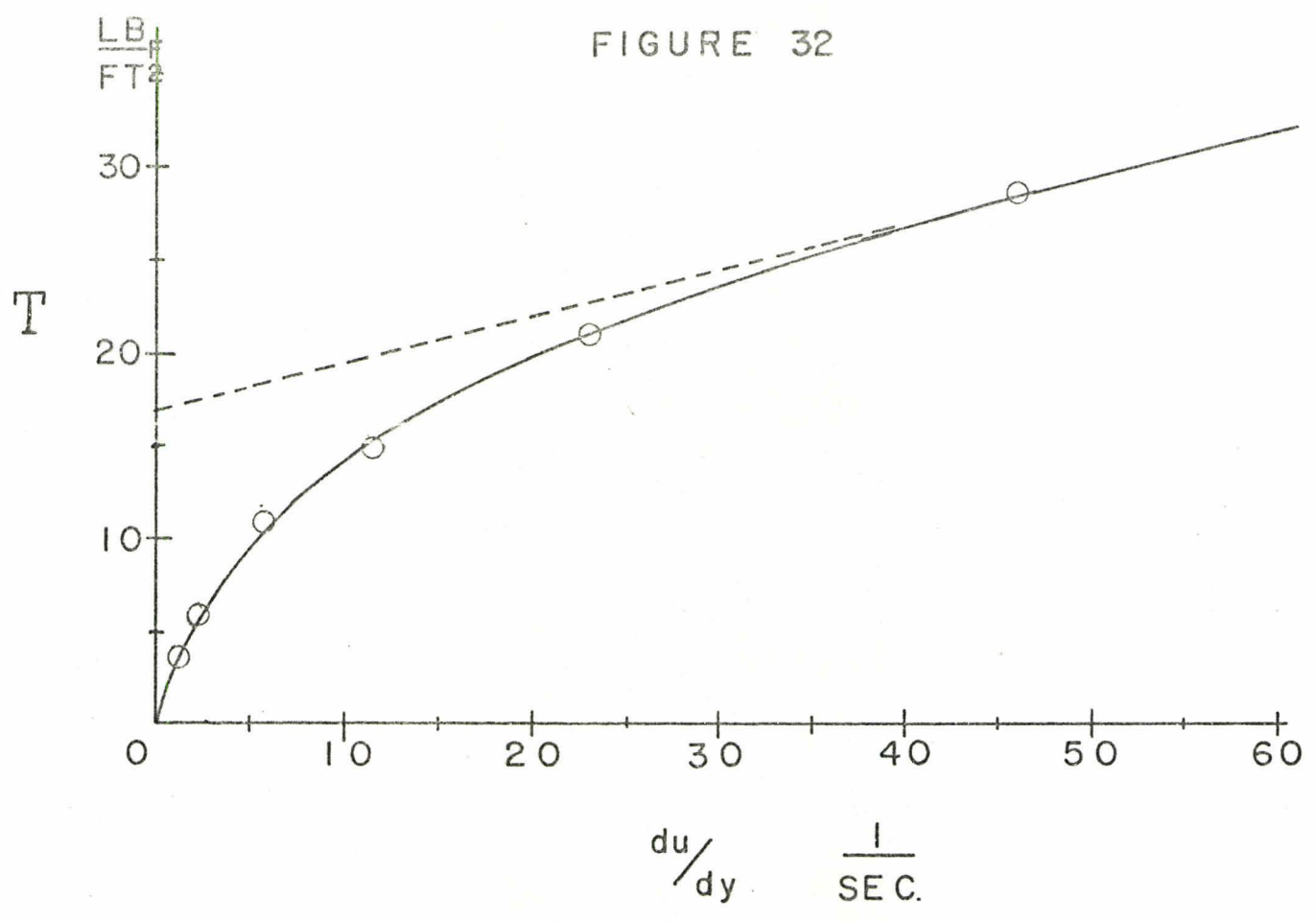
The next step was to categorize the rheological character of the concentrated 2000 Wppm polymer solution. To do this the Brookfield cone and plate viscometer was used. A single sample of the solution was taken and its viscosity measured at different shear rates.



SHEAR STRESS SHEAR RATE
GRAPH

RETEN 423
2000 Wppm

FIGURE 32



The results are shown in figure 32. It is apparent that concentrated Reten 423 is a pseudo-plastic fluid. At a shear rate of between 35 and 45 sec^{-1} , its shear stress becomes proportional to its shearing rate, but below this value it decreases with increasing shear rate. The viscosity beyond this value becomes $\mu = 0.25 \text{ lb}_F \text{ sec/ft}^2$ compared to a water value of $\mu = 2 \times 10^{-5} \text{ lb}_F \text{ sec/ft}^2$.

It has been observed by other authors that polymer solutions exhibit a "diameter-effect" in their drag reducing properties. To determine if this effect occurs with Reten 423 a series of tests were performed using a Hoyt Rheometer similar to the one described in references (33) and (39) and shown in figure 30. The data measured using this instrument is presented in tabular form in tables 9, 10 and 11, and in graphical form in figure 33.

It has been postulated that this diameter effect occurs because of the thinness of the shear layer in capillary tubes, and is therefore completely independent of polymer properties. The results shown in figure 33 seem to bear this out. In figure 33 a comparison between data obtained in a 0.08 inch tube and a 2.0 inch tube show that in the smaller tube, drag reduction commences at lower concentrations and with greater effectiveness and at lower Reynolds numbers than for the much larger tubes. However beyond certain Reynolds numbers the drag reduction in the capillary tube becomes less than that in the test section. This occurrence is consistent with an explanation of a thin shear layer that allows the polymer to alter the velocity profile to a greater extent than would occur with a large shear layer.

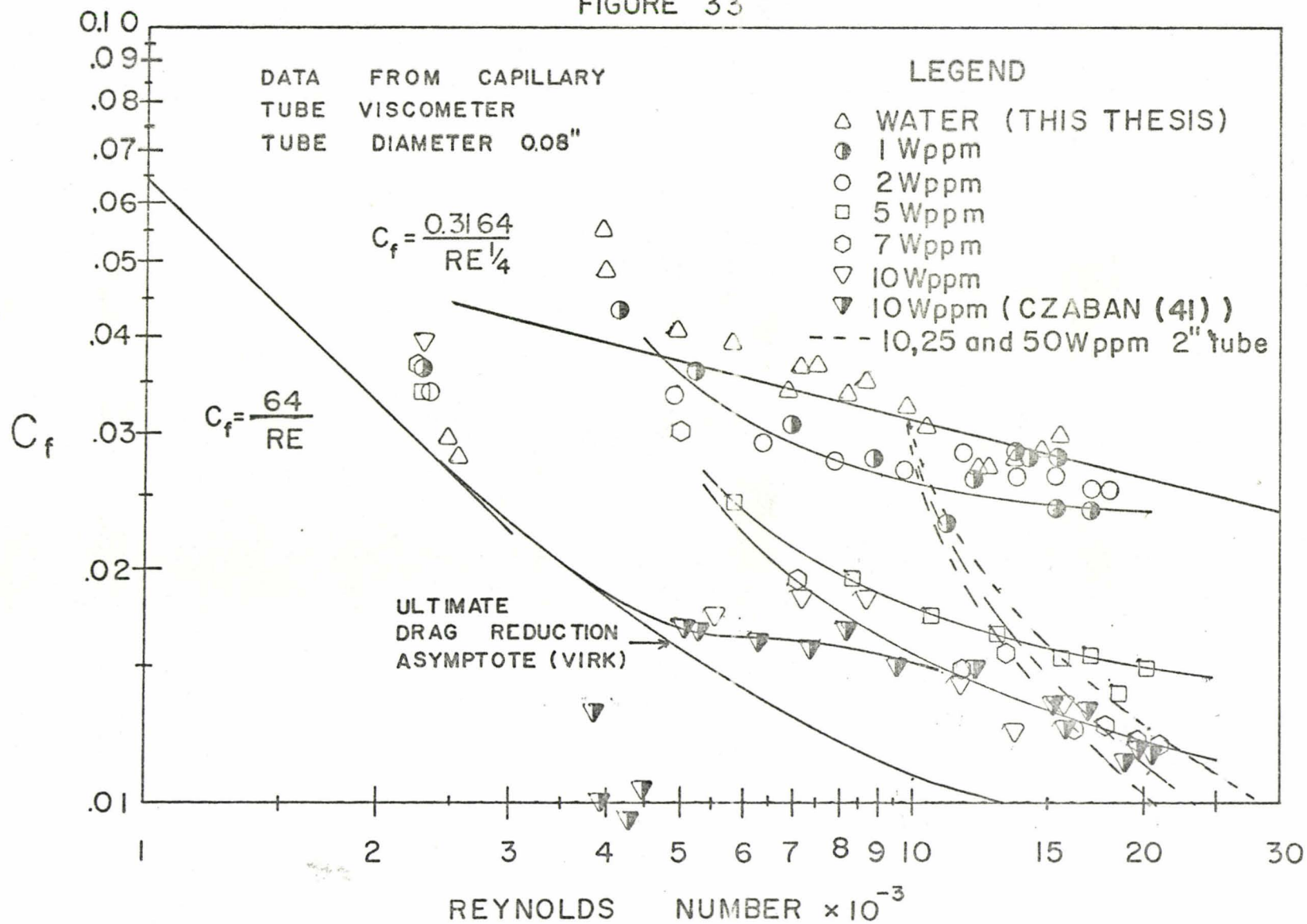
The final property of interest is one to be derived from the drag reduction data obtained in the two inch diameter test section. Meyer has

FRICTION FACTOR

REYNOLDS NUMBER

RETEN 423 POLYMER

FIGURE 33




```

PROGRAM TST (INPUT, OUTPUT, TAPE5=INPUT, TAPE6=OUTPUT)
DIMENSION PG(45,10), T(45,10), V(10), VSQ(10), RE(10), DP(10), K1(10)
1 K2(10), CF(10)
000003 REAL K, K1, K2, NU, L
000003 INTEGER SETS

C
000003 K=0.5
000005 D=0.08/12.0
000006 L=1.25
000010 NU=1.06E-5
000011 CONST=(0.0035316*4.0)/(3.14159*D*D)

C
000014 READ (5,10) SETS
000022 10 FORMAT (I2)
000022 DO 1 I=1, SETS
000024 1 READ (5,2) (PG(I,J), J=1,10)
000042 DO 3 I=1, SETS
000043 3 READ (5,2) (T(I,J), J=1,10)
000061 2 FORMAT (10F6.2)

C
000061 WRITE (6,9)
000064 9 FORMAT (H1,40X, *FRICTION FACTOR-REYNOLDS NUMBER DATA*//)
000064 DO 4 I=1, SETS
000066 DO 5 J=1, 10
000067 IF (T(I,J).EQ.0.0) GO TO 11
000073 V(J)=CONST/T(I,J)
000077 VSQ(J)=V(J)*V(J)
000101 RE(J)=V(J)*D/NU
000104 DP(J)=144.0*PG(I,J)+101.4
000111 K1(J)=(DP(J)*4.0*D*32.17)/(2.0*62.4*L*VSQ(J))
000120 K2(J)=((1.0+K)*D)/(L)
000124 CF(J)=K1(J)-K2(J)
000127 GO TO 5
000127 11 CF(J)=0.0
000131 RE(J)=0.0
000132 5 CONTINUE

C
000134 WRITE (6,6) I
000142 6 FORMAT (1H0,30X, *DATA SET NUMBER*,4X,I2)
000142 WRITE (6,7) (RE(J), J=1,10)
000154 7 FORMAT (1H0,10X, *RE*,4X,10E9.2)
000154 WRITE (6,8) (CF(J), J=1,10)
000166 8 FORMAT (11X, *CF*,4X,10E9.2)

C
000156 4 CONTINUE

C
000171 STOP
000173 END

UNUSE D COMPILER SPACE
007600

```

TABLE 10
MEASURED DATA

#1		#2		#3		#4		#5		#6		#7		#8	
P	T	P	T	P	T	P	T	P	T	P	T	P	T	P	T
PSIG	SEC	PSIG	SEC	PSIG	SEC	PSIG	SEC	PSIG	SEC	PSIG	SEC	PSIG	SEC	PSIG	SEC
0.0	27.0	0.0	27.3	0.0	27.8	0.0	28.0	0.0	26.3	0.0	28.5	0.0	25.9	0.0	29.5
2.4	16.2	2.1	15.6	2.5	13.0	2.3	11.8	2.1	16.1	2.4	12.7	2.6	14.0	2.7	11.6
4.2	11.2	3.2	12.0	3.5	10.0	5.1	7.8	3.2	12.8	3.5	9.1	3.6	11.8	3.8	8.7
7.0	8.7	5.2	9.2	5.5	8.2	8.4	6.0	5.5	9.4	5.8	7.2	6.0	9.5	5.5	7.4
6.5	9.0	8.0	7.2	8.3	6.6	12.0	5.0	8.5	7.7	8.8	5.6	10.5	6.7	8.5	5.6
9.6	7.9	11.6	5.7	12.3	5.6	11.2	4.2	11.4	6.6	12.1	4.9	15.7	5.6	11.6	4.6
13.6	5.8	15.6	5.2	16.6	4.7	20.6	3.8	16.4	5.2	15.9	4.0	20.2	4.8	16.6	4.0
17.0	5.1	19.6	4.8	20.8	4.2	24.3	3.9	19.5	4.9	19.8	3.6	24.5	4.4		
23.0	4.3	22.8	4.2	24.8	3.8	28.3	3.2	24.0	4.4	23.0	3.3	28.0	4.0		
		25.2	4.0	27.5	3.6			27.7	4.2	27.4	3.1				

The equation for use with the capillary tube viscometer is;

$$\frac{P_1}{\gamma} \frac{V_1^2}{2g} + \Delta Z = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + \frac{K V_2^2}{2g} + \frac{2 f V_2^2 L}{Dg}$$

where $K = 0.5$

Tube diameter

$D = 0.080$ inches

Length

$L = 1.25$ ft.

Temperature

$T = 21^\circ\text{C}$

Viscosity of water at 21°C $\nu = 1.06 \times 10^{-5}$ ft²/sec

TABLE 11

FRICTION FACTOR-REYNOLDS NUMBER DATA

	DATA SET NUMBER 1										Water
RE	2.36E+03	3.93E+03	5.68E+03	7.31E+03	7.07E+03	8.60E+03	1.10E+04	1.25E+04	1.48E+04	0.	
CF	3.17E-02	5.50E-02	3.96E-02	3.71E-02	3.71E-02	3.57E-02	2.92E-02	2.76E-02	2.59E-02	0.	
	DATA SET NUMBER 2										1 Wppm
RE	2.33E+03	4.08E+03	5.30E+03	6.92E+03	8.34E+03	1.12E+04	1.22E+04	1.33E+04	1.52E+04	1.59E+04	
CF	3.26E-02	4.48E-02	3.55E-02	3.07E-02	2.69E-02	2.29E-02	2.61E-02	2.82E-02	2.41E-02	2.41E-02	
	DATA SET NUMBER 3										2 Wppm
RE	2.29E+03	4.89E+03	6.36E+03	7.76E+03	9.54E+03	1.14E+04	1.35E+04	1.52E+04	1.67E+04	1.77E+04	
CF	3.41E-02	3.39E-02	2.45E-02	2.43E-02	2.23E-02	2.35E-02	2.16E-02	2.13E-02	2.05E-02	2.03E-02	
	DATA SET NUMBER 4										5 Wppm
RE	2.27E+03	5.39E+03	8.16E+03	1.06E+04	1.27E+04	1.52E+04	1.67E+04	1.87E+04	1.99E+04	0.	
CF	3.47E-02	2.44E-02	1.93E-02	1.74E-02	1.65E-02	1.51E-02	1.58E-02	1.44E-02	1.50E-02	0.	
	DATA SET NUMBER 5										Water
RE	2.42E+03	3.95E+03	4.97E+03	6.77E+03	8.26E+03	9.64E+03	1.22E+04	1.33E+04	1.45E+04	1.52E+04	
CF	2.97E-02	4.82E-02	4.15E-02	3.44E-02	3.42E-02	3.28E-02	2.78E-02	2.80E-02	2.90E-02	3.08E-02	
	DATA SET NUMBER 6										7 Wppm
RE	2.23E+03	5.01E+03	6.99E+03	8.84E+03	1.14E+04	1.30E+04	1.59E+04	1.77E+04	1.93E+04	2.05E+04	
CF	3.62E-02	3.07E-02	1.89E-02	1.81E-02	1.51E-02	1.58E-02	1.26E-02	1.26E-02	1.20E-02	1.29E-02	
	DATA SET NUMBER 7										Water
RE	2.46E+03	4.55E+03	5.39E+03	6.70E+03	9.50E+03	1.14E+04	1.33E+04	1.45E+04	1.59E+04	0.	
CF	2.85E-02	4.21E-02	3.84E-02	3.88E-02	3.09E-02	3.18E-02	2.93E-02	2.97E-02	2.75E-02	0.	
	DATA SET NUMBER 8										10 Wppm
RE	2.16E+03	5.49E+03	7.31E+03	8.60E+03	1.14E+04	1.38E+04	1.59E+04	0.	0.	0.	
CF	3.94E-02	2.74E-02	1.84E-02	1.83E-02	1.43E-02	1.21E-02	1.34E-02	0.	0.	0.	

proposed a law of the wall applicable to polymer such that;

$$u^+ = \frac{1}{k} \ln y^+ + 5.5 + \alpha \ln \left(\frac{u_*'}{u_*} \right) \quad (6.2)$$

where α is a property of the polymer dependant upon concentration and species.

Meyer has derived the following modified friction factor relation for

Reynolds number large enough that the wall friction exceeds u_*' ;

$$\frac{1}{\sqrt{f}} = \left(4 + \frac{\alpha}{2}\right) \log (Re \sqrt{f}) - 0.394 - \frac{\alpha}{2} \log \left(\frac{2 u_*' D}{u} \right) \quad (6.3)$$

F. M. White⁽²⁵⁾ has collected data for Guar Gum and Polyox WSR 301 showing the variation of α with concentration.

To calculate α it is first necessary to determine u_*' the threshold friction velocity. From figure 29 the threshold value occurs at;

$$Re = 9750$$

$$C_f = 0.023$$

or $f = 0.00515$

Now $u_*' = \sqrt{\frac{\tau_0}{\rho}}$ at onset;

or $u_*' = \sqrt{\frac{\Delta P R g_c}{2 L \rho}}$ (6.4)

By definition

$$C_f = \frac{\Delta P}{\left(\frac{L}{D}\right) \frac{\rho V^2}{2g_c}} \quad (6.5)$$

At onset;

$$R_e = \frac{VD}{\nu} = 9750$$

therefore

$$u = \frac{9750 \times 1.6885 \times 10^{-5}}{6.1615}$$

$$= 1.019 \text{ ft./sec.}$$

and substituting into (6.5) we have;

$$\Delta P = 0.023 \times \left(\frac{5.0}{.1615} \right) \frac{62.4 \times (1.019)^2}{2 \times 32.2}$$

$$= 0.717 \text{ lb}_F/\text{ft}$$

Thus on substituting into equation (6.4) we can write;

$$u_{*0}' = \left\{ \frac{0.717 \left(\frac{.1615}{2} \right) (32.2)}{2 \times 5.0 \times 62.4} \right\}^{1/2}$$

$$= 0.05466 \text{ ft/sec}$$

The value of α can be determined from equation (6.4) by substituting at any value of Reynolds number greater than the threshold value. Letting

$$R_e = 20,500$$

$$C_f = 0.010$$

or $f = 0.0025$

and substituting into equation (6.3) we have;

$$\frac{1}{\sqrt{.0025}} = \left(4 + \frac{\alpha}{2}\right) \log [(20,500) \sqrt{.0025}] - .394$$

$$- \frac{\alpha}{2} \log \left[\frac{2(.0546) (.1615)}{1.6845 \times 10^{-5}} \right]$$

Collecting terms and dividing we finally have;

$$\alpha = 83.24$$

This value seems extremely high when compared to the data of White⁽²⁵⁾ who calculated a maximum value of $\alpha = 11$ for both polyox and Guar Gum. It must be noted however that the threshold value of friction velocity for Reten 423 is extremely low, 0.055 ft/sec compared to 0.23 ft/sec for Guar Gum and 0.08 ft/sec for Polyox WSR 301.

APPENDIX VII

DATA TABLES

000211
000214
000222
000222
000224
000236
000251
000251

200 LJCT(I)=I
 READ (5,72) NPPTS
72 FORMAT (I2)
 DO 41 I=1,NPPTS
41 READ (5,40) RRE(I),DDPT(I)
 READ (5,42) XPL,YPL,XACT,YACT
40 FORMAT (2F6.2)
42 FORMAT (4F20.2)

C
C
C

 CONVERT DIGITIZER DATA TO ACTUAL VALUES

000251
000260
000266
000271
000271
000273
000273
000314
000324
000324

 SFX1=XPL/(ALOG(XACT)-ALOG(1000.0))
 SFY1=YPL/(ALOG(YACT)-ALOG(0.001))
 WRITE (6,70)
70 FORMAT (23X,*REYNOLDS NUMBER*,5X,*FRICTION FACTOR*//)
 DO 43 I=1,NPPTS
 RE(I)=EXP((RRE(I)/SFX1)+ALOG(1000.0))
 DPT(I)=EXP((DDPT(I)/SFY1)+ALOG(0.001))
 WRITE (6,44) RE(I),DPT(I)
44 FORMAT (20X,2E15.5)
43 CONTINUE

C
C
C
C
C
C
C

 INITIALIZE PROGRAM PRELIMINARY CALCULATIONS

000327
000330
000332
000336
000340
000343
000346
000351
000353
000356
000350
000353
000355
000370
000372
000375
000377

 DO 20 L=1,SETS
 DS(L)=DS(L)/12.0
 IF (L.GT.26) D=0.1615
 DO 20 I=1,N
 FCT(L,I)=0.0
 CRX(L,I)=0.0
 CD(L,I)=0.0
 DPDIF(L,I)=0.0
 DPC(L,I)=0.0
 VSQAV(L,I)=0.0
 DPL(L,I)=0.0
 DPM(L,I)=0.0
 VPR(L,I)=0.0
 XLG(L,I)=0.0
 XRE(L,I)=0.0
 DPZ(L,I)=0.0
 BLDL(L,I)=0.0

C

000402
000404
000415

 IF (V(L,I).EQ.0.0) GO TO 20
 FCT(L,I)=((GM(L,I)-GC)/GT)*THT(L,I)/30.48
 V(L,I)=V(L,I)*(0.1605*4.0)/(3.14159*D*D*60.0)

C

000425
000432

20 CONTINUE
 D=0.16343

C
C
C

 CORRECT FOR THERMAL NON ZERO

000434
000435
000436
000441
000450

 DO 21 L=1,SETS
 DO 21 I=1,N
 IF (V(L,I).EQ.0.0) GO TO 21
 CRX(L,I)=(ZRO1(L,I)+ZRO2(L,I))/2.0
21 CONTINUE

```

C
C      CALCULATE PRESSURE DROP ACROSS CAPSULE ETC
C
000455 DO 30 L=1,SETS
000457 IF (L.LE.26) GO TO 310
000461 D=0.1615
000463 DL=5.0
C
000464 310 DOVD(L)=DS(L)/D
000467 BUO(L)=(SIG(L)-RO)/RO
000471 BUO1(L)=(SIG(L)-RO)/SIG(L)
000474 DO 31 I=1,N
C
000475 IF (V(L,I).EQ.0.0) GO TO 31
000500 DPC(L,I)=((A(L,I,2)-A(L,I,1))-CRX(L,I))*RO*FCT(L,I)
000512 VSQAV(L,I)=V(L,I)*V(L,I)
000514 CALL INTERP (V(L,I),L,DPM(L,I),BLDL(L,I),XRE(L,I))
000521 DPDF(L,I)=DPC(L,I)-DPM(L,I)
000530 CD(L,I)=(4.0/3.0)*(DS(L)*32.17/VSQAV(L,I))*((SIG(L)-RO)/RO)
000543 VPR(L,I)=VSQAV(L,I)/(BUO(L)*D)
000550 XLG(L,I)=DPDF(L,I)/(BUO(L)*D)
000554 DPZ(L,I)=1.0+(DL/(SPN(L,I)*DS(L)))*((DPC(L,I)/BLDL(L,I))-1.0)
000567 31 CONTINUE
000572 30 CONTINUE
C
C
C      OUTPUT PORTION OF PROGRAM
C
000574 DO 50 L=1,SETS
000576 DS(L)=DS(L)*12.0
000600 WRITE (6,51) (LINE(L,J),J=1,7)
000614 51 FORMAT (H1,20X,7A10)
C
000614 WRITE (6,52) DS(L),SIG(L)
000624 52 FORMAT (H0,10X,*SPHERE DIAMETER*,F10.5,25X,*SPHERE DENSITY LB PER
1 FT.,3*,F10.5//)
000624 WRITE (6,62) DOVD(L)
000632 62 FORMAT (10X,*D OVER D RATIO*,5X,F10.5)
000632 WRITE (6,65) NU(L)
000640 65 FORMAT (10X,*VISCOSITY*,10X,E10.3)
000640 WRITE (6,63) BUO(L)
000646 63 FORMAT (10X,*((SIGMA-RO)/RO)*,6X,F10.5)
000646 WRITE (6,80) BUO1(L)
000654 80 FORMAT (10X,*SIGMA-RO/SIGMA*,5X,F10.5//)
000654 WRITE (6,400)
000650 400 FORMAT (H0,20X,*MANOMETER READING (CM)*,10X,*ZERO 1*,10X,*ZERO 2*)
000650 DO 401 J=1,N
000652 WRITE (6,402) (A(L,I,J),J=1,2),ZRC1(L,I),ZRC2(L,I)
000705 402 FORMAT (25X,F5.2,5X,F5.2,13X,F5.2,11X,F5.2)
000705 401 CONTINUE
000710 WRITE (6,311) (LJCT(I),I=1,N)
000722 311 FORMAT (H0,17X,10I9)
000722 WRITE (6,53) (GM(L,I),I=1,N)
000737 53 FORMAT (10X,*MAN. GM*,5X,10E9.2)
000737 WRITE (6,55) (SPN(L,I),I=1,N)
000754 55 FORMAT (10X,*SPHERE NO*,3X,10E9.2)
000754 WRITE (6,54) (V(L,I),I=1,N)

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000771 54 FORMAT (10X,*(V-AV)*6X,10E9.2)
000771 WRITE (6,59) (VSOAV(L,I),I=1,N)
001006 59 FORMAT (10X,*(V-AV)-SQ*,3X,10E9.2)
001006 WRITE (6,61) (CD(L,I),I=1,N)
001023 61 FORMAT (10X,*DRAG COEFF*,2X,10E9.2)
001023 WRITE (6,203) (XRE(L,I),I=1,N)
001040 203 FORMAT (10X,*RE*,10X,10E9.2)
001040 WRITE (6,58) (DPC(L,I),I=1,N)
001055 58 FORMAT (10X,*DELTA-PM*,4X,10E9.2)
001055 WRITE (6,60) (OPQIF(L,I),I=1,N)
001072 60 FORMAT (10X,*DPM-DPL*,5X,10E9.2)
001072 WRITE (6,84) (VPR(L,I),I=1,N)
001107 84 FORMAT (10X,*V.V/K*,7X,10E9.2)
001107 WRITE (6,85) (XLG(L,I),I=1,N)
001124 85 FORMAT (10X,*DPM-DPL/K*,3X,10E9.2)
001124 WRITE (6,56) (THT(L,I),I=1,N)
001141 56 FORMAT (10X,*MAN, THETA*,2X,10E9.2)
001141 WRITE (6,57) (CRX(L,I),I=1,N)
001156 57 FORMAT (10X,*(ZR1+ZR2)/2*,1X,10E9.2)
001156 WRITE (6,350) (DPZ(L,I),I=1,N)
001173 350 FORMAT (10X,*PR1*,9X,10E9.2)
001173 WRITE (6,201) (BLDL(L,I),I=1,N)
001210 201 FORMAT (10X,*DPL-BLASIUS*,1X,10E9.2)
001210 WRITE (6,403)
001214 403 FORMAT (H0,40X,*K=D.(SIG-RO)/RO*)
001214 50 CONTINUE

```

C
C

```

001217 STOP
001221 END

```

```

UNUSED COMPILER SPACE
016700

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SUBROUTINE INTERP(V,LX,DH,DH1,CLR)
C
000010 REAL NU
000010 COMMON/111/RE(100),DPT(100),D,NU(40),L,RO,NPTS
C
000010 DL=4.0
000011 D=0.16343
000012 IF (LX.LE.26) GO TO 50
000015 DL=5.0
000016 D=0.1615
000020 50 CLR=V*D/NU(LX)
000022 IF (CLR.LE.2500.0) GO TO 130
C
000025 DO 100 I=1,NPTS
000026 IF (CLR.LE.RE(I)) GO TO 110
000031 100 CONTINUE
C
000033 WRITE (6,120) LX
000040 120 FORMAT (10X,*DATA NOT IN RANGE*,5X,*SET NUMBER*,5X,I2//)
000040 DH=0.00
000044 GO TO 500
C
000044 110 I=I-1
000046 CF=(DPT(I)-DPT(I+1))*((CLR-RE(I))/(RE(I+1)-RE(I)))+DPT(I+1)
000055 DH=(CF*DL*RO*V*V)/(D*2.0*32.17)
000063 CF1=0.316/(CLR)**0.25
000067 DH1=(CF1*DL*RO*V*V)/(D*2.0*32.17)
000076 GO TO 500
000076 130 DH=(32.0*DL*RO*V*V)/(32.17*D*CLR)
000104 DH1=DH
C
000105 500 RETURN
000106 END

```

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JNUSED COMPILER SPACE
023200

```


SET 1 1.875 STEEL SINGLE SPHERE

SPHERE DIAMETER 1.87500

SPHERE DENSITY LB PER FT..3 499.51000

D OVER D RATIO .95607
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 7.00497
 SIGMA-RO/SIGMA .87508

MANOMETER READING (CM)
 8.08 65.30
 8.05 65.38
 8.00 65.10
 I
 I
 I
 I
 I
 I

ZERO 1
 1.43
 1.86
 1.93
 I
 I
 I
 I
 I
 I

ZERO 2
 1.86
 1.93
 1.62
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	7.14E-01	7.14E-01	4.59E-01	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	5.10E-01	5.10E-01	2.11E-01	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	9.21E+01	9.21E+01	2.23E+02	0.	0.	0.	0.	0.	0.	0.
RE	7.58E+03	7.58E+03	4.88E+03	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	4.05E+01	4.04E+01	4.03E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	4.02E+01	4.01E+01	4.02E+01	0.	0.	0.	0.	0.	0.	0.
V.V/K	4.45E-01	4.45E-01	1.84E-01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	3.51E+01	3.50E+01	3.51E+01	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.02E-01	6.02E-01	6.02E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.64E+00	1.89E+00	1.77E+00	0.	0.	0.	0.	0.	0.	0.
PR1	2.51E+03	2.50E+03	5.43E+03	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	4.10E-01	4.10E-01	1.89E-01	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 2 1.749 STEEL SINGLE SPHERE

SPHERE DIAMETER 1.74900

SPHERE DENSITY LB PER FT..3 503.50000

D OVER D RATIO .89182
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO 7.06891
 SIGMA-RO/SIGMA .87607

MANOMETER READING (CM)
 13.70 56.80

ZERO 1
 .96

ZERO 2
 .96

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	6.69E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SC	4.48E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	9.86E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
RE	6.68E+03	0.	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	3.10E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	3.07E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	3.88E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	2.66E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	9.60E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
PR1	2.26E+03	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	3.72E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG-RO) / RO$

SET 3 1.625 STEEL UP TO 2 IN LINE

SPHERE DIAMETER 1.62500

SPHERE DENSITY LB PER FT..3 506.80000

D OVER D RATIO .82859
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 7.12179
 SIGMA-RO/SIGMA .87687

MANOMETER READING (CM)

18.31 56.37
 29.55 36.60

ZERO 1

.87
 .10

ZERO 2

1.52
 .10

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.35E+01	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	2.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	1.50E+00	2.35E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.25E+00	5.51E+00	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	1.84E+01	7.51E+00	0.	0.	0.	0.	0.	0.	0.	0.
RE	1.59E+04	2.49E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	2.70E+01	5.67E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	2.59E+01	5.41E+01	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.93E+00	4.73E+00	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	2.22E+01	4.65E+01	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.05E-01	3.17E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.20E+00	1.00E-01	0.	0.	0.	0.	0.	0.	0.	0.
PR1	5.03E+02	2.41E+02	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.50E+00	3.29E+00	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SET 4 1.497 STEEL UP TO 5 IN LINE

SPHERE DIAMETER 1.49700

SPHERE DENSITY LB PER FT..3 513.50000

D OVER D RATIO .76332
 VISCOSITY 1.716E-05
 (SIGMA-RO)/RO 7.22917
 SIGMA-RO/SIGMA .87848

MANOMETER READING (CM)

17.70 55.65
 30.15 36.00
 30.20 35.90
 30.10 36.00
 28.80 37.35
 28.80 37.35
 27.34 38.80
 27.38 38.78
 25.90 40.25
 25.90 41.90

ZERO 1

1.70
 .10
 .10
 .10
 .10
 .07
 .08
 .07
 .06
 .08

ZERO 2

1.40
 .10
 .10
 .10
 .10
 .10
 .10
 .08
 .06
 .03

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01
SPHERE NO	1.00E+00	2.00E+00	2.00E+00	2.00E+00	3.00E+00	3.00E+00	4.00E+00	4.00E+00	5.00E+00	5.00E+00
(V-AV)	3.20E+00	3.62E+00	3.92E+00	3.62E+00	3.67E+00	3.57E+00	3.95E+00	3.95E+00	4.38E+00	4.38E+00
(V-AV)-SQ	1.02E+01	1.31E+01	1.24E+01	1.31E+01	1.35E+01	1.27E+01	1.56E+01	1.56E+01	1.92E+01	1.92E+01
DRAG COEFF	3.78E+00	2.95E+00	3.12E+00	2.95E+00	2.87E+00	3.03E+00	2.48E+00	2.48E+00	2.01E+00	2.01E+00
RE	3.05E+04	3.45E+04	3.35E+04	3.45E+04	3.50E+04	3.40E+04	3.77E+04	3.77E+04	4.18E+04	4.18E+04
DELTA-PM	2.65E+01	4.66E+01	4.54E+01	4.70E+01	6.85E+01	6.86E+01	9.22E+01	9.18E+01	1.16E+02	1.29E+02
DPM-DPL	2.20E+01	4.09E+01	4.00E+01	4.13E+01	6.26E+01	6.30E+01	8.55E+01	8.52E+01	1.08E+02	1.21E+02
V.V/K	8.67E+00	1.11E+01	1.05E+01	1.11E+01	1.14E+01	1.08E+01	1.32E+01	1.32E+01	1.63E+01	1.63E+01
DPM-DPL/K	1.86E+01	3.46E+01	3.38E+01	3.49E+01	5.30E+01	5.34E+01	7.24E+01	7.21E+01	9.10E+01	1.02E+02
MAN. THETA	6.02E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01	3.16E-01
(ZR1+ZR2)/2	1.55E+00	1.00E-01	1.00E-01	1.00E-01	1.00E-01	8.50E-02	9.00E-02	7.50E-02	6.00E-02	5.50E-02
PR1	1.15E+02	8.85E+01	9.10E+01	8.94E+01	8.94E+01	9.45E+01	8.08E+01	8.05E+01	6.83E+01	7.68E+01
DPL-BLASIUS	5.82E+00	7.22E+00	6.87E+00	7.22E+00	7.39E+00	7.04E+00	8.41E+00	8.41E+00	1.01E+01	1.01E+01

K=D.(SIG-RO)/RO

SET 5 1.497 STEEL A CONTINUATION OF SET 4

SPHERE DIAMETER 1.49700

SPHERE DENSITY LB PER FT..3 513.50000

D OVER D RATIO .76332
 VISCOSITY 1.716E-05
 (SIGMA-RO)/RO 7.22917
 SIGMA-RO/SIGMA .87848

MANOMETER READING (CM)

21.55 44.65
 21.50 44.55
 21.95 44.14
 I
 I
 I
 I
 I
 I
 I

ZERO 1

.05
 .09
 .11
 I
 I
 I
 I
 I
 I

ZERO 2

.05
 .05
 .09
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.35E+01	1.35E+01	1.35E+01	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	6.00E+00	6.00E+00	6.00E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.14E+00	4.14E+00	4.07E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.72E+01	1.72E+01	1.65E+01	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	2.25E+00	2.25E+00	2.34E+00	0.	0.	0.	0.	0.	0.	0.
RE	3.95E+04	3.95E+04	3.87E+04	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.87E+02	1.86E+02	1.79E+02	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.80E+02	1.79E+02	1.72E+02	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.45E+01	1.45E+01	1.40E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.52E+02	1.51E+02	1.46E+02	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.16E-01	3.16E-01	3.16E-01	0.	0.	0.	0.	0.	0.	0.
(ZP1+ZR2)/2	5.00E-02	7.00E-02	1.00E-01	0.	0.	0.	0.	0.	0.	0.
PR1	1.05E+02	1.05E+02	1.04E+02	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	9.14E+00	9.14E+00	8.84E+00	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SET 6 1.375 STEEL SINGLE SPHERES

SPHERE DIAMETER 1.37500

SPHERE DENSITY LB PER FT..3 520.50000

D OVER D RATIO .70112
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 7.34135
 SIGMA-RO/SIGMA .88012

MANOMETER READING (CM)

19.78 54.00
 19.50 54.00
 19.30 53.95
 I
 I
 I
 I
 I
 I

ZERO 1

1.83
 1.39
 2.08
 I
 I
 I
 I
 I
 I

ZERO 2

1.39
 2.08
 2.10
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	3.93E+00	3.93E+00	3.93E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.54E+01	1.54E+01	1.54E+01	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	2.34E+00	2.34E+00	2.34E+00	0.	0.	0.	0.	0.	0.	0.
RE	4.17E+04	4.17E+04	4.17E+04	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	2.38E+01	2.39E+01	2.37E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.71E+01	1.72E+01	1.70E+01	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.29E+01	1.29E+01	1.29E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.42E+01	1.43E+01	1.42E+01	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.02E-01	6.02E-01	6.02E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.61E+00	1.74E+00	2.09E+00	0.	0.	0.	0.	0.	0.	0.
PR1	6.84E+01	6.89E+01	6.83E+01	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	8.11E+00	8.11E+00	8.11E+00	0.	0.	0.	0.	0.	0.	0.

$K = D. (SIG-RO) / RO$

SET 7 1.250 STEEL SINGLE SPHERE

SPHERE DIAMETER 1.25000

SPHERE DENSITY LB PER FT..3 535.80000

D OVER D RATIO .63738
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 7.58654
 SIGMA-RO/SIGMA .88354

MANOMETER READING (CM)

20.95 52.33
 20.98 52.33

I
I
I
I
I
I
I

ZERO 1

1.79
1.13

I
I
I
I
I
I
I

ZERO 2

1.13
1.23

I
I
I
I
I
I
I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.38E+00	4.41E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.92E+01	1.95E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	1.76E+00	1.74E+00	0.	0.	0.	0.	0.	0.	0.	0.
RE	4.65E+04	4.69E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	2.19E+01	2.20E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.37E+01	1.38E+01	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.55E+01	1.57E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.11E+01	1.11E+01	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.03E-01	6.03E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.46E+00	1.18E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	4.82E+01	4.78E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	9.81E+00	9.93E+00	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SET 8 1.00 STEEL SINGLE SPHERES

SPHERE DIAMETER 1.00000

SPHERE DENSITY LB PER FT..3 513.50000

D OVER D RATIO .50990
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 7.22917
 SIGMA-RO/SIGMA .87848

MANOMETER READING (CM)

23.60 49.50
 23.50 49.60

ZERO 1

1.62
 1.16

ZERO 2

1.20
 1.77

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.93E+00	4.92E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.44E+01	2.42E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	1.06E+00	1.07E+00	0.	0.	0.	0.	0.	0.	0.	0.
RE	5.24E+04	5.22E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.76E+01	1.77E+01	0.	0.	0.	0.	0.	0.	0.	0.
OPM-DPL	7.35E+00	7.53E+00	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.06E+01	2.05E+01	0.	0.	0.	0.	0.	0.	0.	0.
OPM-DPL/K	6.22E+00	6.37E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	5.92E-01	5.92E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.41E+00	1.47E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	2.28E+01	2.36E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.21E+01	1.20E+01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 9 7/8 STEEL SINGLE SPHERES

SPHERE DIAMETER .87500

SPHERE DENSITY LB PER FT..3 482.50000

D OVER D RATIO .44616
 VISCOSITY 1.584E-05
 (SIGMA-RO)/RO 6.73237
 SIGMA-RO/SIGMA .87067

MANOMETER READING (CM)

25.85 47.60
 25.85 47.75

ZERO 1

1.62
 1.31

ZERO 2

1.30
 1.63

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.89E+00	4.88E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.39E+01	2.38E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	8.81E-01	8.85E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	5.04E+04	5.03E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.50E+01	1.51E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	4.98E+00	5.13E+00	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.17E+01	2.16E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	4.53E+00	4.66E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.46E+00	1.47E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	1.48E+01	1.55E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.20E+01	1.19E+01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 10 3/4 STEEL SINGLE SPHERES

SPHERE DIAMETER .75000

SPHERE DENSITY LB PER FT..3 482.00000

D OVER D RATIO .38243
 VISCOSITY 1.584E-05
 (SIGMA-RO)/RO 6.72436
 SIGMA-RO/SIGMA .87054

MANOMETER READING (CM)

26.93 46.37
 27.05 46.48

ZERO 1

1.27
 1.19

ZERO 2

1.19
 1.59

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.81E+00	4.81E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.32E+01	2.32E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	7.78E-01	7.78E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	4.97E+04	4.97E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.34E+01	1.33E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	3.76E+00	3.64E+00	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.11E+01	2.11E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	3.43E+00	3.31E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.23E+00	1.39E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	1.08E+01	1.01E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.16E+01	1.16E+01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SPHERE DIAMETER .62500

SPHERE DENSITY LB PER FT..3 482.30000

D OVER D RATIO .31869
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 6.72917
 SIGMA-RO/SIGMA .87062

MANOMETER READING (CM)

27.85 45.40
 27.90 45.45

ZERO 1

1.27
 1.23

ZERO 2

1.23
 1.88

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.72E+00	4.72E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.22E+01	2.22E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	6.76E-01	6.76E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	5.01E+04	5.01E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.20E+01	1.18E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	2.74E+00	2.51E+00	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.02E+01	2.02E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	2.49E+00	2.29E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.25E+00	1.56E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	6.96E+00	5.41E+00	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.12E+01	1.12E+01	0.	0.	0.	0.	0.	0.	0.	0.

$K=D.(SIG-RO)/RO$

SPHERE DIAMETER .50000

SPHERE DENSITY LB PER FT..3 484.00000

D OVER D RATIO .25495
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 6.75641
 SIGMA-RO/SIGMA .87107

MANOMETER READING (CM)

29.00 44.28
 29.15 44.15
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ZERO 1

1.45
 1.25
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ZERO 2

1.25
 1.44
 I
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.43E+00	4.38E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.96E+01	1.92E+01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	6.15E-01	6.29E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	4.71E+04	4.65E+04	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.03E+01	1.01E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.95E+00	1.94E+00	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.78E+01	1.74E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.76E+00	1.76E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.35E+00	1.35E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	3.58E+00	3.51E+00	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.00E+01	9.81E+00	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SPHERE DIAMETER .37500

SPHERE DENSITY LB PER FT..3 485.00000

D OVER D RATIO .19121
 VISCOSITY 1.539E-05
 (SIGMA-RO)/RO 6.77244
 SIGMA-RO/SIGMA .87134

MANOMETER READING (CM)
 33.00 42.70

ZERC 1
 1.19

ZERO 2
 1.38

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.11E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.69E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	5.37E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
RE	7.37E+04	0.	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	6.20E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	-8.91E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.53E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	-8.05E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	6.09E-01	0.	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.28E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-3.65E+01	0.	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	8.78E+00	0.	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 14 1.740 PLASTIC UP TO 5 IN LINE FREE FLOATING

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 73.69000

D OVER D RATIO .88723
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .18093
 SIGMA-RO/SIGMA .15321

MANOMETER READING (CM)

32.97 40.00
 32.79 40.17
 31.02 41.98
 27.40 45.71
 24.40 48.70
 24.97 48.17
 23.50 49.60
 21.00 52.08
 I I
 I I

ZERO 1

6.43
 6.67
 8.90
 10.63
 9.62
 10.50
 11.10
 10.62
 I I
 I I

ZERO 2

6.67
 7.08
 9.48
 10.70
 10.50
 11.00
 10.62
 12.30
 I I
 I I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	0.	0.
SPHERE NO	1.00E+00	1.00E+00	2.00E+00	3.00E+00	4.00E+00	4.00E+00	4.00E+00	5.00E+00	0.	0.
(V-AV)	1.17E-01	1.20E-01	1.26E-01	1.53E-01	1.59E-01	1.42E-01	1.52E-01	1.53E-01	0.	0.
(V-AV)-SQ	1.38E-02	1.44E-02	1.59E-02	2.34E-02	2.54E-02	2.00E-02	2.30E-02	2.34E-02	0.	0.
DRAG COEFF	8.18E+01	7.83E+01	7.06E+01	4.81E+01	4.43E+01	5.62E+01	4.89E+01	4.81E+01	0.	0.
RE	1.17E+03	1.20E+03	1.26E+03	1.53E+03	1.59E+03	1.41E+03	1.52E+03	1.53E+03	0.	0.
DELTA-PM	7.08E-02	7.45E-02	2.54E-01	1.10E+00	2.04E+00	1.79E+00	2.19E+00	2.81E+00	0.	0.
DPM-DPL	5.30E-02	5.62E-02	2.35E-01	1.07E+00	2.02E+00	1.76E+00	2.16E+00	2.79E+00	0.	0.
V.V/K	4.65E-01	4.86E-01	5.80E-01	7.92E-01	8.59E-01	6.78E-01	7.79E-01	7.92E-01	0.	0.
DPM-DPL/K	1.79E+00	1.90E+00	7.93E+00	3.63E+01	6.82E+01	5.96E+01	7.31E+01	9.44E+01	0.	0.
MAN. THETA	1.22E-01	1.22E-01	1.18E-01	1.18E-01	1.18E-01	1.18E-01	1.18E-01	1.18E-01	0.	0.
(ZR1+ZR2)/2	6.55E+00	6.87E+00	9.19E+00	1.07E+01	1.01E+01	1.07E+01	1.09E+01	1.15E+01	0.	0.
PR1	8.28E+01	8.61E+01	1.69E+02	4.34E+01	5.75E+02	5.66E+02	6.47E+02	6.62E+02	0.	0.
DPL-BLASIUS	1.79E-02	1.82E-02	1.92E-02	2.33E-02	2.43E-02	2.15E-02	2.31E-02	2.33E-02	0.	0.

K=D.(SIG-RO)/RO

SET 15 1.475 PLASTIC UP TO 4 IN LINE FREE FLOATING

SPHERE DIAMETER 1.47500

SPHERE DENSITY LB PER FT..3 73.32000

D OVER D RATIO .75211
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .17500
 SIGMA-RO/SIGMA .14894

MANOMETER	READING (CM)	ZERO 1	ZERO 2
32.89	40.02	6.86	4.60
32.91	40.01	4.60	5.76
34.64	36.25	.65	1.08
33.71	36.73	.91	1.10
33.92	37.09	.68	1.17
33.90	37.12	1.17	1.30
33.00	38.00	.84	1.18
33.04	38.00	1.09	3.60
33.12	37.90	.49	1.15
I	I	I	I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	0.
SPHERE NO	1.00E+00	1.00E+00	1.00E+00	2.00E+00	2.00E+00	2.00E+00	4.00E+00	4.00E+00	4.00E+00	0.
(V-AV)	2.61E-01	2.49E-01	2.74E-01	2.96E-01	4.07E-01	4.04E-01	4.20E-01	4.21E-01	3.19E-01	0.
(V-AV)-SQ	6.83E-02	6.18E-02	7.52E-02	8.75E-02	1.66E-01	1.63E-01	1.76E-01	1.77E-01	1.02E-01	0.
DRAG COEFF	1.35E+01	1.49E+01	1.23E+01	1.05E+01	5.58E+00	5.65E+00	5.24E+00	5.21E+00	9.08E+00	0.
RE	2.61E+03	2.48E+03	2.74E+03	2.95E+03	4.06E+03	4.04E+03	4.19E+03	4.20E+03	3.18E+03	0.
DELTA-PM	2.01E-01	2.75E-01	2.84E-01	7.69E-01	8.62E-01	7.62E-01	1.52E+00	9.98E-01	1.51E+00	0.
DPM-DPL	1.61E-01	2.37E-01	2.41E-01	7.23E-01	7.87E-01	6.88E-01	1.44E+00	9.18E-01	1.46E+00	0.
V.V/K	2.39E+00	2.16E+00	2.63E+00	3.06E+00	5.79E+00	5.71E+00	6.15E+00	6.19E+00	3.55E+00	0.
DPM-DPL/K	5.62E+00	8.30E+00	8.41E+00	2.53E+01	2.75E+01	2.40E+01	5.05E+01	3.21E+01	5.10E+01	0.
MAN. THETA	1.18E-01	1.18E-01	3.16E-01	3.16E-01	3.17E-01	3.17E-01	3.16E-01	3.16E-01	3.16E-01	0.
(ZR1+ZR2)/2	5.73E+00	5.18E+00	8.65E+00	1.00E+00	9.25E+00	1.24E+00	1.01E+00	2.35E+00	8.20E+00	0.
PR1	5.95E+01	2.05E+02	8.72E+01	1.25E+02	7.49E+01	6.53E+01	6.84E+01	4.21E+01	1.14E+02	0.
DPL-BLASIUS	7.17E-02	3.78E-02	7.79E-02	8.91E-02	1.55E-01	1.54E-01	1.64E-01	1.65E-01	1.01E-01	0.

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 73.69000

D OVER D RATIO .88723
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .18093
 SIGMA-RO/SIGMA .15321

MANOMETER READING (CM)	ZERO 1	ZERO 2
32.97	40.00	6.43
32.79	40.17	6.67
33.72	37.62	1.60
33.60	37.77	1.61
33.68	37.71	1.65
33.68	37.72	1.60
32.29	38.98	1.83
32.20	39.08	1.87
32.32	39.00	1.38
31.50	39.62	1.26

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	1.00E+00	1.00E+00	2.00E+00	2.00E+00	2.00E+00	2.00E+00	3.00E+00	3.00E+00	3.00E+00	4.00E+00
(V-AV)	1.17E-01	1.20E-01	1.22E-01	1.17E-01	1.20E-01	1.13E-01	1.19E-01	1.19E-01	1.19E-01	1.21E-01
(V-AV)-SQ	1.38E-02	1.44E-02	1.50E-02	1.38E-02	1.44E-02	1.29E-02	1.41E-02	1.41E-02	1.41E-02	1.47E-02
DRAG COEFF	8.18E+01	7.83E+01	7.51E+01	8.18E+01	7.83E+01	8.74E+01	8.00E+01	8.00E+01	8.00E+01	7.67E+01
RE	1.14E+03	1.16E+03	1.18E+03	1.14E+03	1.16E+03	1.10E+03	1.15E+03	1.15E+03	1.15E+03	1.17E+03
DELTA-PM	7.08E-02	7.45E-02	8.73E-01	9.75E-01	9.23E-01	9.25E-01	1.86E+00	2.51E+00	1.98E+00	2.60E+00
DPM-DPL	5.24E-02	5.57E-02	8.54E-01	9.56E-01	9.04E-01	9.07E-01	1.84E+00	2.49E+00	1.97E+00	2.58E+00
V.V/K	4.65E-01	4.86E-01	5.07E-01	4.65E-01	4.86E-01	4.36E-01	4.76E-01	4.76E-01	4.76E-01	4.96E-01
DPM-DPL/K	1.77E+00	1.88E+00	2.89E+01	3.23E+01	3.06E+01	3.07E+01	6.22E+01	8.43E+01	6.65E+01	8.73E+01
MAN. THETA	1.22E-01	1.22E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	6.55E+00	6.87E+00	1.63E+00	1.63E+00	1.63E+00	1.63E+00	1.85E+00	3.35E-01	1.51E+00	1.35E+00
PR1	7.95E+01	8.26E+01	6.14E+02	7.17E+02	6.64E+02	7.03E+02	9.09E+02	1.23E+03	9.72E+02	9.37E+02
DPL-BLASIUS	1.84E-02	1.88E-02	1.92E-02	1.84E-02	1.88E-02	1.78E-02	1.86E-02	1.86E-02	1.86E-02	1.90E-02

K=D.(SIG-RO)/RO

SET 17 1.740 PLASTIC A CONTINLATION OF SET 16

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 73.69000

D OVER D RATIO .88723
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .18093
 SIGMA-RO/SIGMA .15321

MANOMETER READING (CM)	ZERO 1	ZERO 2
31.86	39.39	1.34
31.70	39.48	1.20
31.77	39.43	1.30
30.79	40.60	1.41
30.98	40.40	1.45
30.98	40.49	1.28
29.32	42.06	.64
29.35	42.07	1.79
29.40	42.00	1.82
I	I	I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	4.00E+00	4.00E+00	4.00E+00	5.00E+00	5.00E+00	5.00E+00	6.00E+00	6.00E+00	6.00E+00	6.00E+00
(V-AV)	1.19E-01	1.20E-01	1.20E-01	1.17E-01	1.19E-01	1.17E-01	1.17E-01	1.19E-01	1.17E-01	1.17E-01
(V-AV)-SQ	1.41E-02	1.44E-02	1.44E-02	1.38E-02	1.41E-02	1.38E-02	1.38E-02	1.41E-02	1.38E-02	1.38E-02
DRAG COEFF	8.00E+01	7.83E+01	7.83E+01	8.18E+01	8.00E+01	8.18E+01	8.18E+01	8.00E+01	8.18E+01	8.18E+01
RE	1.15E+03	1.16E+03	1.16E+03	1.14E+03	1.15E+03	1.14E+03	1.14E+03	1.15E+03	1.14E+03	1.14E+03
DELTA-PM	2.41E+00	2.50E+00	2.43E+00	3.22E+00	3.00E+00	3.10E+00	4.42E+00	4.19E+00	4.14E+00	4.12E+00
DPM-DPL	2.39E+00	2.48E+00	2.41E+00	3.20E+00	2.98E+00	3.08E+00	4.40E+00	4.17E+00	4.12E+00	4.12E+00
V.V/K	4.76E-01	4.86E-01	4.86E-01	4.65E-01	4.76E-01	4.65E-01	4.65E-01	4.76E-01	4.65E-01	4.65E-01
DPM-DPL/K	8.08E+01	8.39E+01	8.17E+01	1.08E+02	1.01E+02	1.04E+02	1.49E+02	1.41E+02	1.39E+02	1.39E+02
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	1.32E+00	1.27E+00	1.32E+00	1.43E+00	1.61E+00	1.44E+00	1.21E+00	1.80E+00	1.83E+00	1.83E+00
PR1	8.86E+02	9.10E+02	8.86E+02	9.59E+02	8.84E+02	9.24E+02	1.10E+03	1.03E+03	1.03E+03	1.03E+03
DPL-BLASIUS	1.86E-02	1.88E-02	1.88E-02	1.84E-02	1.86E-02	1.84E-02	1.84E-02	1.86E-02	1.84E-02	1.84E-02

$K=D. (SIG-RO)/RO$

SET 18 1.475 PLASTIC UP TO 5 IN LINE AT TWO DIAMETERS APART

SPHERE DIAMETER 1.47500

SPHERE DENSITY LB PER FT..3 73.32000

D OVER D RATIO .75211
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .17500
 SIGMA-RO/SIGMA .14894

MANOMETER	READING (CM)	ZERO 1	ZERO 2
32.91	40.91	.60	5.76
34.15	36.91	1.38	1.63
33.50	37.59	1.51	1.77
33.00	37.20	1.77	1.79
32.60	38.32	1.74	1.92
32.68	38.26	1.68	1.91
32.62	38.33	1.76	1.84
32.39	38.89	1.35	1.81
32.17	39.00	1.80	1.89
32.29	38.94	1.40	1.83

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	1.00E+00	2.00E+00	3.00E+00	3.00E+00	4.00E+00	4.00E+00	4.00E+00	5.00E+00	5.00E+00	5.00E+00
(V-AV)	2.49E-01	2.68E-01	2.72E-01	2.75E-01	2.70E-01	2.86E-01	2.91E-01	2.93E-01	3.05E-01	2.87E-01
(V-AV)-SQ	6.18E-02	7.17E-02	7.38E-02	7.59E-02	7.31E-02	8.16E-02	8.45E-02	8.60E-02	9.29E-02	8.23E-02
DRAG COEFF	1.49E+01	1.29E+01	1.25E+01	1.22E+01	1.26E+01	1.13E+01	1.09E+01	1.07E+01	9.93E+00	1.12E+01
RE	2.41E+03	2.59E+03	2.63E+03	2.67E+03	2.62E+03	2.76E+03	2.81E+03	2.84E+03	2.95E+03	2.78E+03
DELTA-PM	5.62E-01	4.84E-01	9.06E-01	9.33E-01	1.50E+00	1.46E+00	1.51E+00	1.90E+00	1.92E+00	1.93E+00
DPM-DPL	5.23E-01	4.40E-01	8.63E-01	8.88E-01	1.46E+00	1.41E+00	1.46E+00	1.85E+00	1.87E+00	1.89E+00
V.V/K	2.16E+00	2.51E+00	2.58E+00	2.65E+00	2.56E+00	2.85E+00	2.96E+00	3.01E+00	3.25E+00	2.88E+00
DPM-DPL/K	1.83E+01	1.54E+01	3.02E+01	3.11E+01	5.41E+01	4.94E+01	5.10E+01	6.46E+01	6.55E+01	6.59E+01
MAN. THETA	1.18E-01	3.19E-01	3.19E-01	3.19E-01	3.19E-01	3.19E-01	3.19E-01	3.19E-01	3.19E-01	3.17E-01
(ZR1+ZR2)/2	3.18E+00	1.50E+00	1.64E+00	1.78E+00	1.83E+00	1.79E+00	1.80E+00	1.58E+00	1.84E+00	1.62E+00
PR1	4.37E+02	8.92E+01	1.17E+02	1.18E+02	1.52E+02	1.34E+02	1.34E+02	1.34E+02	1.27E+02	1.42E+02
DPL-BLASIUS	3.90E-02	7.54E-02	7.73E-02	7.92E-02	7.66E-02	8.44E-02	8.71E-02	8.84E-02	9.45E-02	8.51E-02

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.47500

SPHERE DENSITY LB PER FT..3 73.32000

D OVER D RATIO .75211
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .17500
 SIGMA-RO/SIGMA .14894

MANOMETER READING (CM)

31.28
 31.28
 31.30

39.80
 39.85
 39.85

ZERO 1

1.71
 1.92
 1.88

ZERO 2

1.92
 1.92
 1.95

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	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	6.00E+00	6.00E+00	6.00E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	2.91E-01	3.01E-01	3.05E-01	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	8.45E-02	9.06E-02	9.29E-02	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	1.09E+01	1.02E+01	9.93E+00	0.	0.	0.	0.	0.	0.	0.
RE	2.81E+03	2.91E+03	2.95E+03	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	2.57E+00	2.55E+00	2.55E+00	0.	0.	0.	0.	0.	0.	0.
OPM-DPL	2.53E+00	2.50E+00	2.50E+00	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.96E+00	3.17E+00	3.25E+00	0.	0.	0.	0.	0.	0.	0.
OPM-DPL/K	8.83E+01	8.75E+01	8.73E+01	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.82E+00	1.92E+00	1.91E+00	0.	0.	0.	0.	0.	0.	0.
PR1	1.56E+02	1.45E+02	1.42E+02	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	8.71E-02	9.25E-02	9.45E-02	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SET 20 1.236 PLASTIC SINGLE SPHERES

SPHERE DIAMETER 1.23600

SPHERE DENSITY LB PER FT..3 72.26000

D OVER D PATIO .63024
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .15801
 SIGMA-RO/SIGMA .13645

MANOMETER READING (CM)

32.64	42.60
32.64	43.30
I	I
I	I
I	I
I	I
I	I
I	I
I	I

ZERO 1

6.91
6.78
I
I
I
I
I
I
I

ZERO 2

6.78
6.32
I
I
I
I
I
I
I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	5.15E-01	5.10E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	2.65E-01	2.60E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	2.63E+00	2.68E+00	0.	0.	0.	0.	0.	0.	0.	0.
RE	5.14E+03	5.09E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	4.47E-01	5.89E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	2.94E-01	4.28E-01	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.03E+01	1.01E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.14E+01	1.66E+01	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	1.18E-01	1.18E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	6.85E+00	6.55E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	3.60E+01	6.12E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	2.35E-01	2.31E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 21 0.981 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .98100

SPHERE DENSITY LB PER FT..3 62.78000

D OVER D RATIO .50021
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .00609
 SIGMA-RO/SIGMA .00605

MANOMETER READING (CM)

32.50	40.34
32.39	40.40
I	I
I	I
I	I
I	I
I	I
I	I

ZERO 1
 6.82
 6.14
 I
 I
 I
 I
 I
 I
 I

ZERO 2
 6.09
 6.40
 I
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	7.65E-01	7.65E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	5.85E-01	5.85E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	3.65E-02	3.65E-02	0.	0.	0.	0.	0.	0.	0.	0.
RE	7.64E+03	7.64E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.99E-01	2.49E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	-1.63E-01	-1.12E-01	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	5.88E+02	5.88E+02	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	-1.63E+02	-1.12E+02	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	1.18E-01	1.18E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	6.46E+00	6.27E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-2.72E+01	-2.19E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	4.70E-01	4.70E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SFT 22 0.969 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .96900

SPHERE DENSITY LB PER FT..3 73.92000

D OVER D RATIO .49410
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .18462
 SIGMA-RO/SIGMA .15584

MANOMETER READING (CM)
 34.55 36.34
 34.66 36.28
 I I
 I I
 I I
 I I
 I I
 I I

ZERO 1
 .27
 .70
 I I
 I I
 I I
 I I
 I I

ZERO 2
 .69
 .57
 I I
 I I
 I I
 I I
 I I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	7.97E-01	7.82E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	6.35E-01	6.11E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	1.01E+00	1.05E+00	0.	0.	0.	0.	0.	0.	0.	0.
RE	7.96E+03	7.80E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	5.08E-01	3.82E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.24E-01	1.29E-03	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.11E+01	2.03E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	4.12E+00	4.27E-02	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.21E-01	3.21E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	4.80E-01	6.35E-01	0.	0.	0.	0.	0.	0.	0.	0.
PR1	1.35E+00	-9.73E+00	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	5.04E-01	4.88E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 23 0.879 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .87900

SPHERE DENSITY LB PER FT..3 70.33000

D OVER D RATIO .44820
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .12708
 SIGMA-RO/SIGMA .11275

MANOMETER READING (CM)
 32.47 40.35
 32.39 40.40
 I I I I I I I I
 I I I I I I I I
 I I I I I I I I
 I I I I I I I I
 I I I I I I I I

ZERO 1
 6.64
 6.40
 I I I I I I I I
 I I I I I I I I

ZERO 2
 6.40
 6.51
 I I I I I I I I
 I I I I I I I I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	6.76E-01	6.76E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	4.57E-01	4.57E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	8.74E-01	8.74E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	6.75E+03	6.75E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.95E-01	2.23E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	-1.06E-01	-7.79E-02	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.20E+01	2.20E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	-5.10E+00	-3.75E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	1.18E-01	1.18E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	6.52E+00	6.45E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-2.54E+01	-2.14E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	3.78E-01	3.78E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D. (SIG-RO) / RO$

SET 24 0.742 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .74200

SPHERE DENSITY LB PER FT..3 72.63000

D OVER D RATIO .37835
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .16394
 SIGMA-RO/SIGMA .14085

MANOMETER READING (CM)
 34.70 36.19
 34.68 36.20
 I I
 I I
 I I
 I I
 I I
 I I

ZERO 1
 .63
 .60
 I I
 I I
 I I
 I I
 I I

ZERO 2
 .60
 .60
 I I
 I I
 I I
 I I
 I I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	7.33E-01	7.18E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SC	5.38E-01	5.15E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	8.09E-01	8.44E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	7.32E+03	7.17E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	3.39E-01	3.57E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	2.98E-04	2.14E-02	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	2.01E+01	1.92E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.11E-02	8.00E-01	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.21E-01	3.21E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	6.15E-01	6.00E-01	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-1.33E+01	-8.76E+00	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	4.36E-01	4.20E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

SET 25 0.616 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .61600

SPHERE DENSITY LB PER FT..3 72.82000

D OVER D RATIO .31410
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .16699
 SIGMA-RO/SIGMA .14309

MANOMETER READING (CM)

32.85	39.87
32.42	40.24
I	I
I	I
I	I
I	I
I	I
I	I

ZERO 1

5.68
6.20
I
I
I
I
I
I

ZERO 2

5.95
6.24
I
I
I
I
I
I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	6.44E-01	6.73E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	4.15E-01	4.53E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	8.87E-01	8.11E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	6.43E+03	6.72E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	1.73E-01	2.29E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	-1.05E-01	-6.86E-02	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.52E+01	1.66E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	-3.85E+00	-2.51E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	1.18E-01	1.18E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	5.81E+00	6.22E+00	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-3.82E+01	-2.93E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	3.47E-01	3.76E-01	0.	0.	0.	0.	0.	0.	0.	0.

$K = D. (SIG-RO) / RO$

SET 26 0.608 PLASTIC SINGLE SPHERES

SPHERE DIAMETER .60800

SPHERE DENSITY LB PER FT..3 71.33000

D OVER D RATIO .31002
 VISCOSITY 1.637E-05
 (SIGMA-RO)/RO .14311
 SIGMA-RO/SIGMA .12519

MANOMETER READING (CM)

34.88	36.12
34.89	36.13
I	I
I	I
I	I
I	I
I	I
I	I
I	I

ZERO 1
 .63
 .61
 I
 I
 I
 I
 I
 I
 I

ZERO 2
 .61
 .60
 I
 I
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.00E+00	1.00E+00	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)	6.57E-01	6.57E-01	0.	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	4.31E-01	4.31E-01	0.	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	7.21E-01	7.21E-01	0.	0.	0.	0.	0.	0.	0.	0.
RE	6.56E+03	6.56E+03	0.	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	2.40E-01	2.46E-01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	-5.06E-02	-4.48E-02	0.	0.	0.	0.	0.	0.	0.	0.
V.V/K	1.84E+01	1.84E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	-2.16E+00	-1.91E+00	0.	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.21E-01	3.21E-01	0.	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	6.20E-01	6.05E-01	0.	0.	0.	0.	0.	0.	0.	0.
PR1	-2.51E+01	-2.39E+01	0.	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	3.60E-01	3.60E-01	0.	0.	0.	0.	0.	0.	0.	0.

K=D.(SIG-RO)/RO

SET 27 1.740 PLASTIC UP TO 9 IN LINE D APART

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 78.79000

D OVER D RATIO .89783
 VISCOSITY 1.743E-05
 (SIGMA-RO)/RO .26266
 SIGMA-RO/SIGMA .20802

MANOMETER READING (CM)	ZERO 1	ZERO 2
34.42	36.53	.65
34.33	36.60	1.78
34.30	36.68	1.96
34.78	36.46	1.92
34.60	36.56	.79
34.57	36.62	1.65
34.55	36.68	1.73
33.75	37.43	1.78
33.50	37.65	1.79
33.55	37.64	2.14
		2.13
		2.21

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHEPE NO	1.00E+00	1.00E+00	1.00E+00	1.00E+00	1.00E+00	1.00E+00	1.00E+00	2.00E+00	2.00E+00	2.00E+00
(V-AV)	6.92E-02	6.92E-02	6.92E-02	9.40E-02	9.92E-02	9.92E-02	9.92E-02	9.79E-02	1.33E-01	1.33E-01
(V-AV)-SQ	4.79E-03	4.79E-03	4.79E-03	8.84E-03	9.85E-03	9.85E-03	9.85E-03	9.59E-03	1.77E-02	1.77E-02
DRAG COEFF	3.41E+02	3.41E+02	3.41E+02	1.85E+02	1.66E+02	1.66E+02	1.66E+02	1.70E+02	9.21E+01	9.21E+01
RE	6.41E+02	6.41E+02	6.41E+02	8.71E+02	9.19E+02	9.19E+02	9.07E+02	1.23E+03	1.23E+03	1.23E+03
DELTA-PM	3.42E-01	1.53E-01	1.68E-01	1.77E-01	1.13E-01	1.09E-01	1.08E+00	6.58E-01	7.73E-01	7.50E-01
DPM-DPL	3.27E-01	1.38E-01	1.54E-01	1.57E-01	9.26E-02	8.88E-02	1.06E+00	6.31E-01	7.46E-01	7.22E-01
V.V/K	1.13E-01	1.13E-01	1.13E-01	2.08E-01	2.32E-01	2.32E-01	2.26E-01	4.18E-01	4.18E-01	4.26E-01
DPM-DPL/K	7.72E+00	3.26E+00	3.62E+00	3.70E+00	2.13E+00	2.09E+00	2.50E+01	1.49E+01	1.76E+01	1.70E+01
MAN. THETA	3.16E-01	3.16E-01	3.16E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	1.21E+00	1.87E+00	1.94E+00	1.22E+00	1.67E+00	1.76E+00	6.90E-01	1.97E+00	2.14E+00	2.13E+00
PR1	7.87E+02	3.33E+02	3.70E+02	2.79E+02	1.56E+02	1.50E+02	1.80E+03	3.94E+02	4.66E+02	4.47E+02
DPL-BLASIUS	1.44E-02	1.44E-02	1.44E-02	1.95E-02	2.06E-02	2.06E-02	2.03E-02	2.76E-02	2.76E-02	2.79E-02

K=D.(SIG-RO)/RO

SET 28 A CONTINUATION OF 27

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 78.79000

D OVER D RATIO .89783
 VISCOSITY 1.743E-05
 (SIGMA-RO)/RO .26266
 SIGMA-RO/SIGMA .20802

MANOMETER	READING (CM)	ZERO 1	ZERO 2
33.68	37.58	1.92	2.14
32.80	38.58	2.09	2.29
33.37	38.00	2.29	2.30
32.51	38.80	2.12	2.30
32.60	38.75	2.30	2.27
31.51	40.43	1.90	2.11
31.30	40.50	2.11	2.06
31.38	40.45	1.84	1.90
30.70	41.00	1.90	2.02
31.50	40.33	2.00	2.09

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	2.00E+00	3.00E+00	3.00E+00	3.00E+00	3.00E+00	4.00E+00	4.00E+00	4.00E+00	4.00E+00	4.00E+00
(V-AV)	1.32E-01	1.59E-01	1.58E-01	1.59E-01	1.59E-01	1.78E-01	1.79E-01	1.70E-01	1.70E-01	1.71E-01
(V-AV)-SQ	1.74E-02	2.54E-02	2.50E-02	2.54E-02	2.54E-02	3.15E-02	3.20E-02	2.88E-02	2.88E-02	2.93E-02
DRAG COEFF	9.39E+01	6.44E+01	6.54E+01	6.44E+01	6.44E+01	5.18E+01	5.10E+01	5.67E+01	5.67E+01	5.58E+01
RE	1.22E+03	1.48E+03	1.46E+03	1.48E+03	1.48E+03	1.65E+03	1.66E+03	1.57E+03	1.57E+03	1.58E+03
DELTA-PH	7.18E-01	1.38E+00	8.96E-01	1.57E+00	1.48E+00	2.65E+00	2.73E+00	2.76E+00	3.20E+00	2.60E+00
DPM-DPL	6.90E-01	1.34E+00	8.63E-01	1.53E+00	1.49E+00	2.62E+00	2.69E+00	2.73E+00	3.17E+00	2.57E+00
V.V/K	4.10E-01	5.98E-01	5.89E-01	5.98E-01	5.98E-01	7.44E-01	7.54E-01	6.79E-01	6.79E-01	6.90E-01
DPM-DPL/K	1.63E+01	3.17E+01	2.04E+01	3.61E+01	3.42E+01	6.17E+01	6.35E+01	6.43E+01	7.46E+01	6.06E+01
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	2.03E+00	2.19E+00	2.29E+00	2.21E+00	2.28E+00	2.00E+00	2.08E+00	1.87E+00	1.96E+00	2.04E+00
PR1	4.36E+02	4.69E+02	3.04E+02	5.34E+02	5.05E+02	6.13E+02	6.27E+02	6.69E+02	7.76E+02	6.25E+02
DPL-BLASIUS	2.74E-02	3.31E-02	3.28E-02	3.31E-02	3.31E-02	3.68E-02	3.71E-02	3.52E-02	3.52E-02	3.55E-02

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 78.79000

D OVER D RATIO .89783
 VISCOSITY 1.716E-05
 (SIGMA-RO)/RO .26266
 SIGMA-RO/SIGMA .20802

MANOMETER READING (CM)	ZERO 1	ZERO 2
29.39	42.20	1.79
29.55	42.05	2.12
29.60	42.06	2.22
27.31	44.10	1.82
27.53	43.85	2.21
27.38	43.95	2.21
27.55	43.88	2.13
25.57	45.80	1.18
25.30	46.00	1.03
25.70	45.60	1.10

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	5.00E+00	5.00E+00	5.00E+00	6.00E+00	6.00E+00	6.00E+00	6.00E+00	7.00E+00	7.00E+00	7.00E+00
(V-AV)	1.96E-01	1.96E-01	1.96E-01	2.00E-01	2.00E-01	1.97E-01	1.98E-01	1.80E-01	2.13E-01	2.12E-01
(V-AV)-SQ	3.84E-02	3.84E-02	3.84E-02	3.99E-02	3.99E-02	3.89E-02	3.94E-02	3.25E-02	4.53E-02	4.48E-02
DRAG COEFF	4.26E+01	4.26E+01	4.26E+01	4.09E+01	4.09E+01	4.20E+01	4.15E+01	5.03E+01	3.61E+01	3.65E+01
RE	1.84E+03	1.84E+03	1.84E+03	1.88E+03	1.88E+03	1.86E+03	1.87E+03	1.70E+03	2.00E+03	1.99E+03
DELTA-PM	4.15E+00	3.96E+00	3.92E+00	5.67E+00	5.67E+00	5.49E+00	5.42E+00	7.36E+00	7.54E+00	7.23E+00
DPM-DPL	4.11E+00	3.92E+00	3.88E+00	5.63E+00	5.63E+00	5.45E+00	5.38E+00	7.32E+00	7.49E+00	7.19E+00
V.V/K	9.04E-01	9.04E-01	9.04E-01	9.41E-01	9.41E-01	9.17E-01	9.29E-01	7.66E-01	1.07E+00	1.05E+00
DPM-DPL/K	9.69E+01	9.25E+01	9.16E+01	1.33E+02	1.33E+02	1.29E+02	1.27E+02	1.73E+02	1.77E+02	1.70E+02
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	2.00E+00	2.17E+00	2.24E+00	2.01E+00	2.01E+00	2.26E+00	2.22E+00	1.09E+00	1.06E+00	1.05E+00
PR1	7.10E+02	6.78E+02	6.71E+02	7.94E+02	7.94E+02	7.79E+02	7.64E+02	9.82E+02	8.50E+02	8.21E+02
DPL-BLASIUS	4.00E-02	4.00E-02	4.00E-02	4.08E-02	4.08E-02	4.02E-02	4.05E-02	3.68E-02	4.34E-02	4.32E-02

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.74000

SPHERE DENSITY LB PER FT..3 78.79000

D OVER D PATIO .89783
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .26266
 SIGMA-RO/SIGMA .20802

MANOMETER READING (CM)
 26.25 45.45
 24.48 46.74
 24.50 46.80
 22.55 48.68
 22.55 48.64
 I I
 I I
 I I
 I I
 I I

ZERO 1
 1.09
 .68
 .70
 .83
 .77
 I
 I
 I
 I
 I

ZERO 2
 1.06
 .89
 1.04
 .77
 .77
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.
SPHERE NO	7.00E+00	8.00E+00	8.00E+00	9.00E+00	9.00E+00	0.	0.	0.	0.	0.
(V-AV)	1.82E-01	2.12E-01	2.13E-01	2.23E-01	2.23E-01	0.	0.	0.	0.	0.
(V-AV)-SQ	3.29E-02	4.48E-02	4.53E-02	4.99E-02	4.99E-02	0.	0.	0.	0.	0.
DRAG COEFF	4.96E+01	3.65E+01	3.61E+01	3.28E+01	3.28E+01	0.	0.	0.	0.	0.
RE	1.74E+03	2.02E+03	2.04E+03	2.14E+03	2.14E+03	0.	0.	0.	0.	0.
DELTA-PM	6.96E+00	8.24E+00	8.22E+00	9.72E+00	9.72E+00	0.	0.	0.	0.	0.
DPM-DPL	6.92E+00	8.20E+00	8.18E+00	9.68E+00	9.67E+00	0.	0.	0.	0.	0.
V.V/K	7.77E-01	1.05E+00	1.07E+00	1.18E+00	1.18E+00	0.	0.	0.	0.	0.
DPM-DPL/K	1.63E+02	1.93E+02	1.93E+02	2.28E+02	2.28E+02	0.	0.	0.	0.	0.
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.07E+00	7.85E-01	8.70E-01	8.00E-01	7.70E-01	0.	0.	0.	0.	0.
PR1	9.36E+02	8.33E+02	8.26E+02	8.27E+02	8.27E+02	0.	0.	0.	0.	0.
DPL-BLASIUS	3.65E-02	4.25E-02	4.28E-02	4.49E-02	4.49E-02	0.	0.	0.	0.	0.

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SET 31 1.478 PLASTIC UP TO 10 IN LINE D APART

SPHERE DIAMETER 1.47800

SPHERE DENSITY LB PER FT..3 77.43000

D OVER D RATIO .76264
 VISCOSITY 1.715E-05
 (SIGMA-RO)/RO .24087
 SIGMA-RO/SIGMA .19411

MANOMETER READING (CM)

35.35 36.50
 35.39 36.54
 35.38 36.48
 34.30 36.96
 33.80 37.48
 33.50 37.78
 33.48 37.75
 33.50 37.70
 32.15 39.40
 32.00 39.59

ZERO 1

.90
 .89
 .98
 .48
 1.49
 1.10
 1.90
 1.82
 2.13
 2.04

ZERO 2

.90
 .98
 .98
 1.50
 1.90
 1.90
 1.82
 2.09
 2.04
 2.00

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	1.00E+00	1.00E+00	1.00E+00	2.00E+00	2.00E+00	3.00E+00	3.00E+00	3.00E+00	4.00E+00	4.00E+00
(V-AV)	2.26E-01	2.17E-01	2.22E-01	4.36E-01	3.94E-01	4.81E-01	4.44E-01	4.51E-01	5.69E-01	5.93E-01
(V-AV)-SQ	5.10E-02	4.70E-02	4.93E-02	1.90E-01	1.56E-01	2.31E-01	1.97E-01	2.03E-01	3.24E-01	3.51E-01
DRAG COEFF	2.49E+01	2.71E+01	2.58E+01	6.69E+00	8.18E+00	5.51E+00	6.46E+00	6.27E+00	3.93E+00	3.62E+00
RE	2.13E+03	2.04E+03	2.09E+03	4.11E+03	3.71E+03	4.52E+03	4.18E+03	4.24E+03	5.36E+03	5.58E+03
DELTA-PM	9.60E-02	8.25E-02	4.61E-02	6.41E-01	7.62E-01	1.07E+00	9.25E-01	8.62E-01	1.98E+00	2.14E+00
DPM-DPL	4.98E-02	3.83E-02	7.42E-04	5.32E-01	6.69E-01	9.30E-01	8.12E-01	7.45E-01	1.69E+00	1.82E+00
V.V/K	1.31E+00	1.21E+00	1.27E+00	4.89E+00	4.00E+00	5.94E+00	5.07E+00	5.22E+00	8.33E+00	9.04E+00
DPM-DPL/K	1.28E+00	9.84E-01	1.91E-02	1.37E+01	1.72E+01	2.39E+01	2.09E+01	1.92E+01	4.34E+01	4.68E+01
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	9.00E-01	9.35E-01	9.80E-01	9.90E-01	1.69E+00	1.50E+00	1.86E+00	1.96E+00	2.08E+00	2.02E+00
PR1	4.49E+01	3.61E+01	1.66E+00	3.84E+01	6.23E+01	4.15E+01	4.13E+01	3.63E+01	4.68E+01	4.71E+01
DPL-BLASIUS	4.61E-02	4.42E-02	4.53E-02	2.25E-01	1.89E-01	2.67E-01	2.33E-01	2.39E-01	3.59E-01	3.86E-01

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.47800

SPHERE DENSITY LB PER FT..3 77.43000

D OVER D RATIO .76264
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .24087
 SIGMA-RO/SIGMA .19411

MANOMETER READING (CM)	ZERO 1	ZERO 2
32.00	39.50	1.62
30.98	40.50	2.05
31.20	40.35	2.20
31.00	40.49	2.14
30.96	40.50	2.02
29.78	41.48	2.04
29.78	41.47	2.18
29.77	41.44	2.16
28.78	42.57	2.23
28.65	42.50	2.10
		1.80
		1.95

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	4.00E+00	5.00E+00	5.00E+00	5.00E+00	5.00E+00	6.00E+00	6.00E+00	6.00E+00	7.00E+00	7.00E+00
(V-AV)	6.10E-01	6.54E-01	6.67E-01	6.70E-01	6.81E-01	7.12E-01	6.84E-01	6.78E-01	7.09E-01	7.23E-01
(V-AV)-SQ	3.72E-01	4.28E-01	4.45E-01	4.49E-01	4.87E-01	5.06E-01	4.68E-01	4.59E-01	5.03E-01	5.23E-01
DRAG COEFF	3.42E+00	2.97E+00	2.86E+00	2.84E+00	2.91E+00	2.51E+00	2.72E+00	2.77E+00	2.53E+00	2.43E+00
RE	5.83E+03	6.26E+03	6.38E+03	6.41E+03	6.88E+03	6.81E+03	6.54E+03	6.48E+03	6.78E+03	6.92E+03
DELTA-PM	2.16E+00	2.84E+00	2.68E+00	2.84E+00	2.88E+00	3.73E+00	3.65E+00	3.64E+00	4.53E+00	4.60E+00
DPM-DPL	1.83E+00	2.46E+00	2.30E+00	2.46E+00	2.51E+00	3.31E+00	3.25E+00	3.25E+00	4.10E+00	4.17E+00
V.V/K	9.56E+00	1.10E+01	1.14E+01	1.15E+01	1.12E+01	1.30E+01	1.20E+01	1.18E+01	1.29E+01	1.35E+01
DPM-DPL/K	4.71E+01	6.33E+01	5.92E+01	6.33E+01	6.46E+01	8.50E+01	8.37E+01	8.34E+01	1.06E+02	1.07E+02
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	1.87E+00	2.13E+00	2.17E+00	2.08E+00	2.03E+00	1.98E+00	2.17E+00	2.20E+00	2.08E+00	1.87E+00
PR1	4.52E+01	4.33E+01	3.89E+01	4.14E+01	4.32E+01	4.20E+01	4.43E+01	4.49E+01	4.51E+01	4.42E+01
DPL-BLASIUS	4.04E-01	4.57E-01	4.73E-01	4.76E-01	4.65E-01	5.29E-01	4.94E-01	4.86E-01	5.26E-01	5.44E-01

$K = D \cdot (\text{SIG} - \text{RO}) / \text{RO}$

SPHERE DIAMETER 1.47800

SPHERE DENSITY LB PER FT..3 77.43000

D OVER D RATIO .76264
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .24087
 SIGMA-RO/SIGMA .19411

MANOMETER READING (CM)

29.49 41.69
 28.65 42.50
 27.54 43.60
 27.55 43.60
 26.14 44.57
 26.57 44.60
 25.49 45.85
 25.30 45.90
 I I
 I I

ZERO 1

2.20
 1.80
 1.85
 1.83
 1.81
 1.80
 .95
 .96
 I
 I

ZERO 2

2.30
 1.95
 1.83
 1.88
 1.80
 1.80
 1.18
 2.14
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	0.	0.
SPHERE NO	6.00E+00	7.00E+00	8.00E+00	8.00E+00	9.00E+00	9.00E+00	1.00E+01	1.00E+01	0.	0.
(V-AV)	6.92E-01	7.12E-01	7.52E-01	7.40E-01	7.12E-01	7.31E-01	7.31E-01	7.39E-01	0.	0.
(V-AV)-SQ	4.79E-01	5.06E-01	5.66E-01	5.48E-01	5.06E-01	5.35E-01	5.35E-01	5.46E-01	0.	0.
DRAG COEFF	2.66E+00	2.51E+00	2.25E+00	2.32E+00	2.51E+00	2.38E+00	2.38E+00	2.33E+00	0.	0.
RE	6.62E+03	6.81E+03	7.19E+03	7.08E+03	6.81E+03	6.99E+03	6.99E+03	7.07E+03	0.	0.
DELTA-PM	3.82E+00	4.60E+00	5.46E+00	5.45E+00	6.38E+00	6.26E+00	7.41E+00	7.31E+00	0.	0.
DPM-DPL	3.42E+00	4.17E+00	5.01E+00	5.00E+00	5.99E+00	5.82E+00	6.97E+00	6.87E+00	0.	0.
V.V/K	1.23E+01	1.30E+01	1.45E+01	1.41E+01	1.30E+01	1.37E+01	1.37E+01	1.40E+01	0.	0.
DPM-DPL/K	8.80E+01	1.07E+02	1.29E+02	1.29E+02	1.53E+02	1.50E+02	1.79E+02	1.76E+02	0.	0.
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	0.	0.
(ZR1+ZR2)/2	2.25E+00	1.87E+00	1.84E+00	1.85E+00	1.80E+00	1.80E+00	1.86E+00	1.55E+00	0.	0.
PR1	4.55E+01	4.56E+01	4.34E+01	4.47E+01	5.09E+01	4.73E+01	5.11E+01	4.94E+01	0.	0.
DPL-BLASIUS	5.04E-01	5.29E-01	5.83E-01	5.67E-01	5.29E-01	5.55E-01	5.55E-01	5.65E-01	0.	0.

K=D.(SIG-RO)/RO

SET 34 1.235 PLASTIC UP TO 12 IN LINE D APART

SPHERE DIAMETER 1.23500

SPHERE DENSITY LB PER FT..3 80.15000

D OVER D RATIO .63725
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .28446
 SIGMA-RO/SIGMA .22146

MANOMETER	READING (CM)	ZERO 1	ZERO 2
35.36	36.21	.39	.39
35.30	36.30	.40	.40
35.26	36.31	.40	.40
34.60	37.22	1.88	1.88
34.80	38.00	.30	.87
34.80	38.04	.85	.96
33.78	38.07	.96	1.00
32.20	39.11	-.12	.98
33.40	38.38	.98	1.00
33.40	38.35	1.00	1.02

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	1.00E+00	1.00E+00	1.00E+00	2.00E+00	3.00E+00	3.00E+00	3.00E+00	4.00E+00	4.00E+00	4.00E+00
(V-AV)	4.51E-01	4.57E-01	4.60E-01	5.50E-01	8.42E-01	8.49E-01	8.55E-01	1.04E+00	1.02E+00	1.02E+00
(V-AV)-SQ	2.03E-01	2.09E-01	2.11E-01	3.02E-01	7.09E-01	7.20E-01	7.32E-01	1.09E+00	1.04E+00	1.04E+00
DRAG COEFF	6.19E+00	6.01E+00	5.94E+00	4.15E+00	1.77E+00	1.74E+00	1.72E+00	1.16E+00	1.21E+00	1.21E+00
RE	4.31E+03	4.37E+03	4.40E+03	5.26E+03	8.06E+03	8.12E+03	8.18E+03	9.97E+03	9.75E+03	9.75E+03
DELTA-PM	1.77E-01	2.30E-01	2.49E-01	2.84E-01	1.00E+00	8.96E-01	1.27E+00	2.49E+00	1.53E+00	1.51E+00
DPM-DPL	6.03E-02	1.10E-01	1.28E-01	2.03E-02	4.59E-01	3.42E-01	7.06E-01	1.70E+00	7.83E-01	7.63E-01
V.V/K	4.42E+00	4.55E+00	4.60E+00	6.58E+00	1.54E+01	1.57E+01	1.59E+01	2.36E+01	2.26E+01	2.26E+01
DPM-DPL/K	1.31E+00	2.39E+00	2.78E+00	4.41E-01	1.00E+01	7.45E+00	1.54E+01	3.70E+01	1.70E+01	1.66E+01
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	3.90E-01	4.00E-01	4.00E-01	1.88E+00	5.85E-01	9.05E-01	9.80E-01	4.30E-01	9.90E-01	1.01E+00
PR1	-1.15E+01	-1.68E+00	1.65E+00	-2.80E+00	7.66E+00	4.96E+00	1.30E+01	1.81E+01	7.58E+00	7.35E+00
DPL-BLASIUS	2.38E-01	2.44E-01	2.46E-01	3.37E-01	7.10E-01	7.20E-01	7.30E-01	1.03E+00	9.93E-01	9.93E-01

K=D.(SIG-RO)/RO

SPHERE DIAMETER 1.23500

SPHERE DENSITY LB PER FT..3 80.15000

D OVER D RATIO .63725
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .28446
 SIGMA-RO/SIGMA .22146

MANOMETER READING (CM)

31.64 39.82
 31.64 39.80
 31.64 39.80
 30.80 40.65
 30.75 45.64
 36.62 40.80
 29.93 41.50
 29.92 41.50
 30.08 41.40
 29.85 42.00

ZERO 1

1.41
 1.41
 1.44
 1.49
 1.52
 1.57
 1.31
 1.00
 1.52
 1.56

ZERO 2

1.44
 1.44
 1.46
 1.52
 1.52
 1.60
 1.45
 1.52
 1.50
 1.70

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
SPHERE NO	5.00E+00	5.00E+00	5.00E+00	6.00E+00	6.00E+00	6.00E+00	7.00E+00	7.00E+00	7.00E+00	8.00E+00
(V-AV)	1.13E+00	1.14E+00	1.13E+00	1.21E+00	1.20E+00	1.19E+00	1.23E+00	1.21E+00	1.22E+00	1.27E+00
(V-AV)-SQ	1.27E+00	1.31E+00	1.28E+00	1.46E+00	1.45E+00	1.43E+00	1.52E+00	1.46E+00	1.50E+00	1.60E+00
DRAG COEFF	9.86E-01	9.62E-01	9.84E-01	8.59E-01	8.68E-01	8.80E-01	8.28E-01	8.61E-01	8.37E-01	7.83E-01
RE	1.08E+04	1.09E+04	1.08E+04	1.16E+04	1.15E+04	1.14E+04	1.18E+04	1.16E+04	1.17E+04	1.21E+04
DELTA-PH	2.59E+00	2.58E+00	2.58E+00	3.20E+00	5.52E+00	9.96E-01	3.91E+00	3.96E+00	3.77E+00	4.04E+00
DPM-DPL	1.69E+00	1.65E+00	1.67E+00	2.19E+00	4.51E+00	6.26E-03	2.89E+00	2.95E+00	2.76E+00	2.95E+00
V.V/K	2.77E+01	2.84E+01	2.78E+01	3.18E+01	3.15E+01	3.11E+01	3.30E+01	3.18E+01	3.27E+01	3.49E+01
DPM-DPL/K	3.67E+01	3.59E+01	3.63E+01	4.76E+01	9.82E+01	1.36E-01	6.29E+01	6.42E+01	6.00E+01	6.42E+01
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	1.43E+00	1.43E+00	1.45E+00	1.50E+00	1.52E+00	1.58E+00	1.38E+00	1.26E+00	1.51E+00	1.63E+00
PR1	1.25E+01	1.20E+01	1.24E+01	1.23E+01	2.66E+01	9.42E-01	1.37E+01	1.46E+01	1.32E+01	1.18E+01
DPL-BLASIUS	1.19E+00	1.21E+00	1.19E+00	1.34E+00	1.33E+00	1.31E+00	1.38E+00	1.34E+00	1.37E+00	1.45E+00

$K = D \cdot (SIG - RO) / RO$

SPHERE DIAMETER 1.23500

SPHERE DENSITY LB PER FT..3 80.15000

D OVER D RATIO .63725
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .28446
 SIGMA-RO/SIGMA .22146

MANOMETER READING (CM)	ZERO 1	ZERO 2
29.85	42.00	1.70
29.70	42.00	1.70
28.29	43.05	1.69
28.28	43.01	1.84
28.30	43.02	1.36
28.55	42.94	1.45
27.90	43.43	1.44
27.80	43.50	1.51
27.90	43.40	1.30
27.40	43.90	1.19
		1.30
		1.10
		1.23

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00	1.599E+00
SPHERE NO	8.000E+00	8.000E+00	9.000E+00	9.000E+00	9.000E+00	9.000E+00	1.000E+01	1.000E+01	1.000E+01	1.000E+01
(V-AV)	1.27E+00	1.25E+00	1.23E+00	1.25E+00	1.27E+00	1.25E+00	1.24E+00	1.21E+00	1.22E+00	1.22E+00
(V-AV)-SQ	1.60E+00	1.57E+00	1.52E+00	1.56E+00	1.60E+00	1.57E+00	1.54E+00	1.46E+00	1.48E+00	1.50E+00
DRAG COEFF	7.83E-01	8.01E-01	8.28E-01	8.06E-01	7.83E-01	7.99E-01	8.18E-01	8.59E-01	8.48E-01	8.37E-01
RE	1.21E+04	1.20E+04	1.18E+04	1.19E+04	1.21E+04	1.20E+04	1.19E+04	1.16E+04	1.16E+04	1.17E+04
DELTA-PM	4.01E+00	4.07E+00	5.10E+00	5.11E+00	5.09E+00	4.96E+00	5.50E+00	5.57E+00	5.47E+00	5.89E+00
DPM-DPL	2.92E+00	3.01E+00	4.08E+00	4.06E+00	4.00E+00	3.89E+00	4.46E+00	4.55E+00	4.48E+00	4.83E+00
V.V/K	3.49E+01	3.41E+01	3.30E+01	3.39E+01	3.49E+01	3.42E+01	3.34E+01	3.18E+01	3.22E+01	3.27E+01
DPM-DPL/K	6.36E+01	6.55E+01	8.88E+01	8.84E+01	8.72E+01	8.47E+01	9.72E+01	9.90E+01	9.75E+01	1.06E+02
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01	3.17E-01
(ZR1+ZR2)/2	1.70E+00	1.69E+00	1.48E+00	1.41E+00	1.45E+00	1.48E+00	1.20E+00	1.20E+00	1.25E+00	1.16E+00
PR1	1.17E+01	1.23E+01	1.55E+01	1.51E+01	1.46E+01	1.44E+01	1.53E+01	1.64E+01	1.58E+01	1.56E+01
DPL-BLASIUS	1.45E+00	1.42E+00	1.38E+00	1.41E+00	1.45E+00	1.42E+00	1.40E+00	1.34E+00	1.35E+00	1.37E+00

K=D. (SIG-RO) / RO

SPHERE DIAMETER 1.23500

SPHERE DENSITY LB PER FT..3 80.15000

D OVER D RATIO .63725
 VISCOSITY 1.689E-05
 (SIGMA-RO)/RO .28446
 SIGMA-RO/SIGMA .22146

MANOMETER READING (CM)
 27.50 43.83
 26.65 44.63
 26.65 44.63
 I I
 I I
 I I
 I I
 I I

ZERO 1
 1.23
 .90
 1.01
 I
 I
 I
 I
 I

ZERO 2
 1.22
 1.01
 1.13
 I
 I
 I
 I
 I

	1	2	3	4	5	6	7	8	9	10
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
SPHERE NO	1.10E+01	1.20E+01	1.20E+01	0.	0.	0.	0.	0.	0.	0.
(V-AV)	1.22E+00	1.23E+00	1.24E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)-SQ	1.48E+00	1.52E+00	1.54E+00	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	8.45E-01	8.28E-01	8.18E-01	0.	0.	0.	0.	0.	0.	0.
RE	1.17E+04	1.18E+04	1.19E+04	0.	0.	0.	0.	0.	0.	0.
DELTA-PM	5.80E+00	6.53E+00	6.49E+00	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	4.80E+00	5.51E+00	5.46E+00	0.	0.	0.	0.	0.	0.	0.
V.V/K	3.23E+01	3.30E+01	3.34E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.05E+02	1.20E+02	1.19E+02	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	3.17E-01	3.17E-01	3.17E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	1.23E+00	9.55E-01	1.07E+00	0.	0.	0.	0.	0.	0.	0.
PR1	1.55E+01	1.61E+01	1.58E+01	0.	0.	0.	0.	0.	0.	0.
DPL-BLASIUS	1.36E+00	1.38E+00	1.40E+00	0.	0.	0.	0.	0.	0.	0.

$K = D \cdot (SIG - RO) / RO$

PROGRAM TST (INPUT,OUTPUT,TAPE5=INPUT,TAPE6=OUTPUT)

REAL NU
INTEGER SETS

C

DIMENSION ZA(40,10),ZRO1(40,10),ZRO2(40,10),V(40,10),
1 THT(40,10),CPDIF(40,10),VSCAV(40,10),GM(40,10),A(40,10,2),DPL(
2 40,10),DPM(40,10),FCT(40,10),CRX(40,10),CD(40,10),DPC(40,10),
3 VPR(40,10),XLG(40,10),LJCT(40),XRE(40,10),DS(40,10),SIG(40,10),
4 DDPT(5,100),RRE(5,100),DOVD(40,10),BUO(40,10),BUO1(40,10)
5 ,ID(100),IX(100),IY(100)

C

COMMON/111/RE(5,100),DPT(5,100),D,NU(40),RO,NPTS(6)

COMMON/222/LINE(40,7)

COMMON/333/ISUB(5)

C

DATA INPUT (READ)

C

C

C

READ (5,1) SETS,N

DO 75 L=1,SETS

DO 75 I=1,N

SIG(L,I)=0.0

DS(L,I)=0.0

DOVC(L,I)=0.0

BUO(L,I)=0.0

V(L,I)=0.0

GM(L,I)=0.0

THT(L,I)=0.0

75 CONTINUE

DO 10 L=1,SETS

DO 11 I=1,N

DO 12 K=1,2

READ(5,2) (ZA(K,J),J=1,2)

IF (ZA(1,1).EQ.0.0) GO TO 13

12 CONTINUE

ZRO1(L,I)=ZA(1,2)-ZA(1,1)

ZRO2(L,I)=ZA(2,2)-ZA(2,1)

READ(5,2) (A(L,I,J),J=1,2)

READ(5,3) V(L,I)

READ(5,4) DS(L,I),THT(L,I),GM(L,I),SIG(L,I)

11 CONTINUE

13 READ(5,5) NU(L)

READ(5,6) (LINE(L,J),J=1,7)

6 FORMAT (7A10)

10 CONTINUE

1 FORMAT (2I2)

2 FORMAT (2F6.2)

3 FORMAT (F6.2)

4 FORMAT (4F10.5)

5 FORMAT (E10.4)

D=0.1615

RO=62.4

GC=0.99707

GT=0.99999

DL=5.0

DO 200 I=1,N

C

C READ DIGITIZER DATA

C

```

000213 200 LJCT(I)=I
000215 K=1
000217 NN=500
000220 340 DO 300 I=1,NN
000222 IF (NN.EQ.1) GO TO 310
000224 READ (5,305) ID(I),IX(I),IY(I)
000235 305 FORMAT (3I10)
000237 IF (IX(I).EQ.0) GO TO 320
000244 RRE(K,I)=FLOAT(IX(I))/100.0
000252 DDPT(K,I)=FLOAT(IY(I))/100.0
000254 300 CONTINUE
000256 320 K=K+1
000260 ISUB(K-1)=I-1
000262 IF (K.GE.5) GO TO 330
000263 GO TO 340
000264 330 NN=1
000265 GO TO 340
000301 310 READ(5,42) XPL,YPL,XACT,YACT
000301 42 FORMAT (4F20.2)

```

C
C
C

CONVERT DIGITIZER DATA TO ACTUAL VALUES

```

000301 SFX1=XPL/(ALOG(XACT)-ALOG(1000.0))
000310 SFY1=YPL/(ALOG(YACT)-ALOG(0.001))
000316 DO 43 I=1,4
000317 WRITE (6,70)
000322 70 FORMAT (60X,*RE*,20X,*CF*//)
000322 KK=ISUB(I)
000324 DO 43 J=1,KK
000326 RE(I,J)=EXP((RRE(I,J)/SFX1)+ALOG(1000.0))
000342 DPT(I,J)=EXP((DDPT(I,J)/SFY1)+ALOG(0.001))
000355 WRITE (6,46) RE(I,J),DPT(I,J)
000367 46 FORMAT (45X,2E20.5)
000367 43 CONTINUE

```

C
C
C
C

INITIALIZE PROGRAM PRELIMINARY CALCULATIONS

```

000374 DO 20 L=1,SETS
000375 DO 20 I=1,N
000376 CS(L,I)=DS(L,I)/12.0
000402 FCT(L,I)=0.0
000405 CRX(L,I)=0.0
000410 CD(L,I)=0.0
000413 DPDIF(L,I)=0.0
000415 DPC(L,I)=0.0
000420 VSQAV(L,I)=0.0
000422 DPL(L,I)=0.0
000425 DPM(L,I)=0.0
000427 VPR(L,I)=0.0
000432 XLG(L,I)=0.0
000434 XRE(L,I)=0.0
000437 C IF (V(L,I).EQ.0.0) GO TO 20
000441 FCT(L,I)=((GM(L,I)-GC)/GT)*THT(L,I)/30.48
000452 V(L,I)=V(L,I)*(0.1605*4.0)/(3.14159*D*D*60.0)

```



```

000462  C 20 CONTINUE
C
C CORRECT FOR THERMAL NON ZERO
C
000467 DO 21 L=1,SETS
000471 DO 21 I=1,N
000472 IF (V(L,I).EQ.0.0) GO TO 21
000475 CRX(L,I)=(ZRO1(L,I)+ZRO2(L,I))/2.0
000504 21 CONTINUE

C
C CALCULATE PRESSURE DROP ACROSS CAPSULE ETC
C
000511 DO 30 L=1,SETS
000513 DO 31 I=1,N
C
000514 IF (V(L,I).EQ.0.0) GO TO 31
000517 DOVD(L,I)=DS(L,I)/D
000524 BUO(L,I)=(SIG(L,I)-RO)/RO
000530 BUO1(L,I)=(SIG(L,I)-RO)/SIG(L,I)
000533 DPC(L,I)=((A(L,I,2)-A(L,I,1))-CRX(L,I))*RO*FCT(L,I)
000542 VSQAV(L,I)=V(L,I)*V(L,I)
000544 CALL INTERP (V(L,I),L,DPM(L,I),XRE(L,I))
000550 DPDIF(L,I)=DPC(L,I)-DPM(L,I)
000557 CD(L,I)=(4.0/3.0)*(DS(L,I)*32.17/VSQAV(L,I))*((SIG(L,I)-RO)/RO)
000573 VPR(L,I)=VSQAV(L,I)/(BUO(L,I)*D)
000600 XLG(L,I)=DPDIF(L,I)/(BUO(L,I)*D)
000603 31 CONTINUE
000606 30 CONTINUE

C
C
C OUTPUT PORTION OF PROGRAM
C
000610 DO 50 L=1,SETS
000612 DS(L,I)=DS(L,I)*12.0
000616 WRITE (6,51) (LINE(L,J),J=1,7)
000632 51 FORMAT (H1,20X,7A10)
C
000632 WRITE (6,65) NU(L)
000640 65 FORMAT (H0,10X,*VISCOSITY (FT..2)/SEC*,5X,10E10.3//)
000640 WRITE (6,400)
000644 400 FORMAT (H0,20X,*MANOMETER READING (CM)*,10X,*ZERO 1*,10X,*ZERO 2*)
000644 DO 401 I=1,N
000646 WRITE (6,402) (A(L,I,J),J=1,2),ZRO1(L,I),ZRO2(L,I)
000671 402 FORMAT (25X,F5.2,5X,F5.2,13X,F5.2,11X,F5.2)
000671 401 CONTINUE
000674 WRITE (6,201) (LJCT(I),I=1,N)
000706 201 FORMAT (H0,17X,10I9)
000706 WRITE (6,62) (DOVD(L,I),I=1,N)
000723 62 FORMAT (10X,*D/D*,9X,10E9.2)
000723 WRITE (6,63) (BUO(L,I),I=1,N)
000740 63 FORMAT (10X,*SIGMA-RO/RO*,1X,10E9.2)
000740 WRITE (6,54) (V(L,I),I=1,N)
000755 54 FORMAT (10X,* (V-AV)*,6X,10E9.2)
000755 WRITE (6,59) (VSQAV(L,I),I=1,N)
000772 59 FORMAT (10X,* (V-AV)..2*,3X,10E9.2)
000772 WRITE (6,61) (CD(L,I),I=1,N)
001007 61 FORMAT (10X,*DRAG COEFF*,2X,10E9.2)

```



```
001007 WRITE (6,203) (XRF(L,I),I=1,N)
001024 203 FORMAT (10X,*RE*,10X,10E9.2)
001024 WRITE (6,58) (DPC(L,I),I=1,N)
001041 58 FORMAT (10X,*DPM*,9X,10E9.2)
001041 WRITE (6,60) (DPDIF(L,I),I=1,N)
001056 60 FORMAT (10X,*DPM-DPL*,5X,10E9.2)
001056 WRITE (6,84) (VPR(L,I),I=1,N)
001073 84 FORMAT (10X,* (V-AV) . . 2/K*,1X,10E9.2)
001073 WRITE (6,85) (XLG(L,I),I=1,N)
001110 85 FORMAT (10X,*DPM-DPL/K*,3X,10E9.2)
001110 WRITE (6,53) (GM(L,I),I=1,N)
001125 53 FORMAT (10X,*MAN. GM*,5X,10E9.2)
001125 WRITE (6,56) (THT(L,I),I=1,N)
001142 56 FORMAT (10X,*MAN. THETA*,2X,10E9.2)
001142 WRITE (6,57) (CRX(L,I),I=1,N)
001157 57 FORMAT (10X,* (ZR1+ZR2)/2*,1X,10E9.2)
001157 WRITE (6,403)
001163 403 FORMAT (H0,40X,*K=D. (SIG-RO)/RO*)
001163 50 CONTINUE
```

C
C

```
001166 STOP
001170 END
```

```
UNUSED COMPILER SPACE
017100
```

SUBROUTINE INTERP (V,L,DH,CLR)

```

C
000007 REAL NU
000007 COMMON/111/RE(5,100),DPT(5,100),D,NU(40),RO,NPTS(6)
000007 COMMON/333/ISUB(5)
C
000007 IF (L.GE.10) GO TO 200
000011 DL=5.0
000013 D=0.1615
000014 50 CLR=V*D/NU(L)
000017 IF (CLR.LE.2500.0) GO TO 130
000021 IF (CLR.LT.9400.0) K=1
000024 IF (CLR.LT.9400.0) GO TO 230
C
000026 IF (L-5) 210,210,220
000030 210 K=3
000031 GO TO 230
000032 220 K=4
000033 230 J=ISUB(K)
000035 CO 100 I=1,J
000037 IF (CLR.LE.RE(K,I)) GO TO 110
000043 100 CONTINUE
C
000045 WRITE (6,120) L
000053 120 FORMAT (10X,*DATA NOT IN RANGE*,5X,*SET NUMBER*,5X,I2//)
000053 DH=0.00
000056 GO TO 500
C
000057 110 I=I-1
000061 CF=(DPT(K,I)-DPT(K,I+1))*((CLR-RE(K,I))/(RE(K,I+1)-RE(K,I)))+DPT(K
I,I+1)
000075 DH=(CF*DL*RO*V*V)/(D*2.0*32.17)
000103 GO TO 500
000104 130 DH=(32.0*DL*RO*V*V)/(32.17*D*CLR)
000113 GO TO 500
C
000113 200 WRITE (6,300)
000117 300 FORMAT (2X,*CF DATA EXCEEDED*//)
000117 500 RETURN
000120 END
UNUSED COMPILER SPACE
023000

```

DATA SET 1 SINGLE STEEL SPHERES IN 25 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)	ZERO 1	ZERO 2
17.91	52.66	1.29
18.63	51.80	1.21
18.49	51.98	1.10
21.03	49.28	.02
21.05	49.33	-.14
23.35	46.93	-.27
23.42	46.92	-.34
27.59	42.56	.10
27.52	42.61	-.22
24.58	45.10	.27

	1	2	3	4	5	6	7	8	9	10
D/D	7.74E-01	7.74E-01	7.74E-01	7.09E-01	7.09E-01	6.45E-01	6.45E-01	5.16E-01	5.16E-01	3.87E-01
SIGMA-RO/RO	7.23E+00	7.23E+00	7.23E+00	7.34E+00	7.34E+00	7.59E+00	7.59E+00	7.23E+00	7.23E+00	6.72E+00
(V-AV)	2.79E+00	3.06E+00	3.06E+00	3.98E+00	3.98E+00	4.60E+00	4.59E+00	4.77E+00	4.71E+00	4.60E+00
(V-AV)..2	7.81E+00	9.35E+00	9.35E+00	1.59E+01	1.59E+01	2.11E+01	2.11E+01	2.28E+01	2.22E+01	2.12E+01
DRAG COEFF	4.96E+00	4.14E+00	4.14E+00	2.27E+00	2.33E+00	1.60E+00	1.61E+00	1.13E+00	1.17E+00	8.52E-01
RE	2.59E+04	2.83E+04	2.83E+04	3.69E+04	3.63E+04	4.25E+04	4.25E+04	4.42E+04	4.35E+04	4.26E+04
DPM	2.35E+01	2.25E+01	2.28E+01	1.97E+01	2.01E+01	1.69E+01	1.69E+01	1.07E+01	1.09E+01	6.87E+00
DPM-DPL	2.14E+01	2.01E+01	2.04E+01	1.62E+01	1.68E+01	1.29E+01	1.28E+01	6.53E+00	6.58E+00	2.81E+00
(V-AV)..2/K	6.69E+00	8.01E+00	8.01E+00	1.34E+01	1.30E+01	1.73E+01	1.72E+01	1.95E+01	1.90E+01	1.93E+01
DPM-DPL/K	1.83E+01	1.72E+01	1.74E+01	1.37E+01	1.41E+01	1.05E+01	1.05E+01	5.59E+00	5.63E+00	2.99E+00
MAN. CM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
MAN. THETA	5.76E-01	5.76E-01	5.76E-01	5.81E-01	5.81E-01	5.81E-01	5.81E-01	5.82E-01	5.82E-01	2.77E-01
(ZR1+ZR2)/2	1.30E+00	1.25E+00	1.16E+00	5.05E-01	6.00E-02	2.95E-01	3.05E-01	8.50E-02	2.45E-01	1.35E-01

K=D.(SIG-RO)/RO

DATA SET 2 SINGLE STEEL SPHERES IN 25 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)

26.40 43.25
27.80 41.50
29.42 40.12

ZERO 1

.90
.82
3.28

ZERO 2

-.11
-.60
-.24

I
I
I
I
I

I
I
I
I
I

I
I
I
I
I

I
I
I
I
I

	1	2	3	4	5	6	7	8	9	10
D/D	3.22E-01	2.58E-01	1.93E-01	0.	0.	0.	0.	0.	0.	0.
SIGMA-RO/RO	6.73E+00	6.76E+00	6.77E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.45E+00	4.33E+00	3.87E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)..2	1.98E+01	1.88E+01	1.50E+01	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	7.60E-01	6.43E-01	6.06E-01	0.	0.	0.	0.	0.	0.	0.
RE	4.12E+04	4.01E+04	3.58E+04	0.	0.	0.	0.	0.	0.	0.
DPM	5.55E+00	4.69E+00	3.17E+00	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	1.62E+00	8.47E-01	3.55E-02	0.	0.	0.	0.	0.	0.	0.
(V-AV)..2/K	1.82E+01	1.72E+01	1.37E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.49E+00	7.76E-01	3.25E-02	0.	0.	0.	0.	0.	0.	0.
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	2.77E-01	2.84E-01	2.84E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	3.95E-01	1.10E-01	1.52E+00	0.	0.	0.	0.	0.	0.	0.

K=D.(SIG-RO)/RO

DATA SET 4 25 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)

ZERO 1

ZERO 2

29.50	40.70	1.80
29.78	40.42	1.85
30.04	40.16	.16
28.81	41.39	1.10
28.29	41.91	1.70
27.17	43.03	.96
27.30	42.90	.60
26.59	43.61	1.31
25.81	44.39	.98
25.38	44.82	1.42

1.08
1.11
.10
.66
1.02
.57
.36
.78
.58
.86

	1	2	3	4	5	6	7	8	9	10
D/D	1.93E-01	1.93E-01	1.93E-01	2.58E-01	2.58E-01	3.22E-01	3.22E-01	3.22E-01	3.87E-01	3.87E-01
SIGMA-RO/RO	7.67E+01	7.67E+01	7.67E+01	6.76E+00	6.76E+00	6.73E+00	6.73E+00	6.73E+00	6.72E+00	6.72E+00
(V-AV)	3.94E+00	3.87E+00	3.75E+00	4.11E+00	4.09E+00	4.53E+00	4.38E+00	4.59E+00	4.65E+00	4.78E+00
(V-AV)..2	1.55E+01	1.50E+01	1.41E+01	1.69E+01	1.62E+01	2.05E+01	1.92E+01	2.11E+01	2.16E+01	2.29E+01
DRAG COEFF	6.63E+00	6.85E+00	7.30E+00	7.14E+00	6.82E+00	7.34E+00	7.85E+00	7.13E+00	8.35E+00	7.88E+00
RF	3.65E+04	3.59E+04	3.48E+04	3.81E+04	4.06E+04	4.19E+04	4.05E+04	4.25E+04	4.30E+04	4.43E+04
DPM	3.37E+00	3.16E+00	3.45E+00	4.04E+00	4.23E+00	5.21E+00	5.22E+00	5.52E+00	6.15E+00	6.32E+00
DPM-DPL	1.32E-02	5.09E-02	2.81E-01	5.04E-01	4.52E-01	1.11E+00	1.45E+00	1.47E+00	1.97E+00	2.11E+00
(V-AV)..2/K	1.25E+00	1.21E+00	1.14E+00	1.55E+00	1.56E+00	1.88E+00	1.76E+00	1.94E+00	1.99E+00	2.11E+00
DPM-DPL/K	1.07E-03	4.10E-03	2.27E-02	4.62E-01	4.14E-01	1.02E+00	1.34E+00	1.35E+00	1.81E+00	1.94E+00
MAN. CM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01
(ZR1+ZR2)/2	1.44E+00	1.48E+00	1.30E-01	8.80E-01	1.06E+00	7.65E-01	4.80E-01	1.05E+00	7.80E-01	1.14E+00

K=D.(SIG-RO)/RO

DATA SET 5 25 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)

ZERO 1

ZERO 2

21.34 48.86
19.47 50.73
18.41 51.79
12.12 58.08
12.24 57.96
9.79 60.41
33.65 36.55
33.72 36.48
33.78 36.42
33.61 36.59

1.52
1.64
1.66
1.92
1.62
1.10
0.02
0.04
0.03
0.02
-1.85

	1	2	3	4	5	6	7	8	9	10
D/D	5.16E-01	5.16E-01	5.16E-01	6.45E-01	6.45E-01	6.45E-01	7.09E-01	7.09E-01	7.09E-01	7.72E-01
SIGMA-RO/RO	7.23E+00	7.23E+00	7.23E+00	7.59E+00	7.59E+00	7.59E+00	7.34E+00	7.34E+00	7.34E+00	7.23E+00
(V-AV)	4.65E+00	4.61E+00	4.75E+00	4.51E+00	4.50E+00	4.46E+00	4.06E+00	4.16E+00	3.73E+00	2.34E+00
(V-AV)..2	2.16E+01	2.13E+01	2.25E+01	2.04E+01	1.99E+01	1.99E+01	1.65E+01	1.73E+01	1.39E+01	5.46E+00
DRAG COEFF	1.19E+00	1.21E+00	1.15E+00	1.66E+00	1.79E+00	1.71E+00	2.19E+00	2.09E+00	2.60E+00	7.08E+00
RE	4.31E+04	4.27E+04	4.39E+04	4.18E+04	4.04E+04	4.13E+04	3.76E+04	3.85E+04	3.45E+04	2.16E+04
DPM	9.08E+00	1.03E+01	1.11E+01	1.56E+01	1.52E+01	1.72E+01	2.10E+01	1.99E+01	1.91E+01	2.87E+01
DPM-DPL	4.89E+00	6.24E+00	6.65E+00	1.15E+01	1.34E+01	1.32E+01	1.76E+01	1.63E+01	1.60E+01	2.70E+01
(V-AV)..2/K	1.85E+01	1.82E+01	1.93E+01	1.68E+01	1.55E+01	1.62E+01	1.39E+01	1.46E+01	1.17E+01	4.68E+00
DPM-DPL/K	4.19E+00	5.35E+00	5.70E+00	9.42E+00	9.00E+00	1.08E+01	1.49E+01	1.37E+01	1.35E+01	2.31E+01
MAN. CM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.35E+01	1.35E+01	1.35E+01	1.35E+01
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01
(ZR1+ZR2)/2	1.22E+00	1.31E+00	1.33E+00	7.40E-01	1.20E+00	8.80E-01	2.00E-02	3.00E-02	2.50E-02	9.50E-01

$K=D.(SIG-RO)/RO$

DATA SET 6 POLYMER 25 WPPM

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)		ZERO 1	ZERO 2
33.53	36.67	.11	.06
33.50	36.70	.02	.02
33.27	36.93	.09	.06
33.21	36.99	.06	.04
33.23	36.97	.04	.02
33.06	37.14	.10	.06
32.97	37.23	.04	.02
32.35	37.85	.03	.02
I	I	I	I

	1	2	3	4	5	6	7	8	9	10
D/D	7.72E-01	7.72E-01	8.38E-01	8.38E-01	8.38E-01	9.02E-01	9.02E-01	9.67E-01	0.	0.
SIGMA-RO/RO	7.23E+00	7.23E+00	7.12E+00	7.12E+00	7.12E+00	7.07E+00	7.07E+00	7.00E+00	0.	0.
(V-AV)	2.93E+00	3.18E+00	1.61E+00	2.01E+00	1.48E+00	5.54E-01	9.58E-01	7.16E-01	0.	0.
(V-AV)..2	8.58E+00	1.01E+01	2.61E+00	4.04E+00	2.09E+00	3.07E-01	9.19E-01	5.12E-01	0.	0.
DRAG COEFF	4.51E+00	3.83E+00	1.59E+01	1.02E+01	1.98E+01	1.44E+02	4.81E+01	9.17E+01	0.	0.
RE	2.71E+04	2.94E+04	1.49E+04	1.86E+04	1.34E+04	5.13E+03	8.88E+03	6.63E+03	0.	0.
DPM	2.23E+01	2.32E+01	2.62E+01	2.72E+01	2.71E+01	2.92E+01	3.09E+01	3.99E+01	0.	0.
DPM-DPL	2.00E+01	2.07E+01	2.50E+01	2.58E+01	2.60E+01	2.89E+01	3.02E+01	3.95E+01	0.	0.
(V-AV)..2/K	7.35E+00	8.66E+00	2.26E+00	3.51E+00	1.82E+00	2.69E-01	8.05E-01	4.53E-01	0.	0.
DPM-DPL/K	1.71E+01	1.77E+01	2.18E+01	2.24E+01	2.26E+01	2.53E+01	2.64E+01	3.49E+01	0.	0.
MAN. CM	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	0.	0.
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	0.	0.
(ZR1+ZR2)/2	8.50E-02	2.00E-02	7.50E-02	5.00E-02	3.00E-02	8.00E-02	3.00E-02	2.50E-02	0.	0.

K=D. (SIG-RO)/RO

DATA SET 3 SINGLE STEEL SPHERES IN 50 WFFM POLYMER

VISCOSITY (FT.²)/SEC 1.744E-05

MANOMETER READING (CM)

26.55 42.98
29.00 40.45
29.50 40.02

ZERO 1

-.11
.99
.94

ZERO 2

-.18
-.40
3.28

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	1	2	3	4	5	6	7	8	9	10
D/D	3.22E-01	2.58E-01	1.93E-01	0.	0.	0.	0.	0.	0.	0.
SIGMA-RO/RO	6.73E+00	6.76E+00	6.77E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV)	4.50E+00	4.11E+00	4.04E+00	0.	0.	0.	0.	0.	0.	0.
(V-AV) ²	2.03E+01	1.69E+01	1.63E+01	0.	0.	0.	0.	0.	0.	0.
DRAG COEFF	7.41E-01	7.16E-01	5.58E-01	0.	0.	0.	0.	0.	0.	0.
RE	4.17E+04	3.80E+04	3.74E+04	0.	0.	0.	0.	0.	0.	0.
DPM	5.59E+00	3.85E+00	2.90E+00	0.	0.	0.	0.	0.	0.	0.
DPM-DPL	2.06E+00	3.58E+01	-1.62E-01	0.	0.	0.	0.	0.	0.	0.
(V-AV) ² /K	1.87E+01	1.54E+01	1.49E+01	0.	0.	0.	0.	0.	0.	0.
DPM-DPL/K	1.89E+00	7.87E-01	-1.49E-01	0.	0.	0.	0.	0.	0.	0.
MAN. GM	1.59E+00	1.59E+00	1.59E+00	0.	0.	0.	0.	0.	0.	0.
MAN. THETA	2.77E-01	2.84E-01	2.84E-01	0.	0.	0.	0.	0.	0.	0.
(ZR1+ZR2)/2	-1.45E-01	2.95E-01	2.11E+00	0.	0.	0.	0.	0.	0.	0.

$K = D. (SIG-RO) / RO$

DATA SET 7 50 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)

30.84 39.36
 30.76 39.44
 31.00 39.20
 29.91 40.29
 30.22 39.98
 28.84 41.36
 28.59 41.61
 28.37 41.83
 27.52 42.68
 27.16 43.04

ZERO 1

.68
 1.28
 1.62
 .23
 .71
 1.22
 .28
 .38
 1.54
 1.20

ZERO 2

.41
 .77
 .97
 .14
 .41
 .72
 .16
 .22
 .92
 .72

	1	2	3	4	5	6	7	8	9	10
D/D	1.93E-01	1.93E-01	1.93E-01	2.58E-01	2.58E-01	2.58E-01	3.22E-01	3.22E-01	3.22E-01	3.87E-01
SIGMA-RO/RO	6.77E+00	6.77E+00	6.77E+00	6.76E+00	6.76E+00	6.76E+00	6.73E+00	6.73E+00	6.73E+00	6.72E+00
(V-AV)	3.69E+00	3.44E+00	3.65E+00	4.24E+00	4.04E+00	3.85E+00	4.20E+00	4.28E+00	4.31E+00	4.70E+00
(V-AV)..2	1.36E+01	1.18E+01	1.33E+01	1.80E+01	1.63E+01	1.48E+01	1.77E+01	1.83E+01	1.86E+01	2.21E+01
DRAG COEFF	6.67E-01	7.69E-01	6.81E-01	6.72E-01	7.39E-01	8.15E-01	8.50E-01	8.20E-01	8.10E-01	8.15E-01
RE	3.42E+04	3.18E+04	3.38E+04	3.93E+04	3.74E+04	3.56E+04	3.89E+04	3.97E+04	3.99E+04	4.35E+04
DPM	2.75E+00	2.64E+00	2.38E+00	3.52E+00	3.18E+00	3.99E+00	4.42E+00	4.54E+00	4.81E+00	5.15E+00
DPM-DPL	1.45E-01	1.83E-01	1.51E-01	2.65E-01	9.44E-02	1.29E+00	1.23E+00	1.45E+00	1.67E+00	1.55E+00
(V-AV)..2/K	1.25E+01	1.08E+01	1.22E+01	1.65E+01	1.50E+01	1.36E+01	1.63E+01	1.69E+01	1.71E+01	2.04E+01
DPM-DPL/K	1.33E-01	1.68E-01	1.38E-01	2.42E-01	8.65E-02	1.18E+00	1.14E+00	1.34E+00	1.53E+00	1.43E+00
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01
(ZR1+ZR2)/2	5.45E-01	1.03E+00	1.29E+00	1.85E-01	5.60E-01	9.70E-01	2.20E-01	3.00E-01	1.23E+00	9.60E-01

$K = D \cdot (SIG-RO) / RO$

DATA SET 8 50 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

	MANOMETER READING (CM)		ZERC 1	ZERO 2						
	24.79	45.41	1.44	.86						
	26.52	43.68	.60	.36						
	21.79	48.41	26.62	18.32						
	21.49	48.71	1.36	.82						
	20.58	49.62	.22	.14						
	12.46	57.74	.14	.08						
	13.62	56.58	.98	.58						
	11.26	58.94	1.10	.66						
	33.94	36.26	.02	.02						
	33.81	36.39	.10	.06						
	1	2	3	4	5	6	7	8	9	10
D/D	3.87E-01	3.87E-01	5.16E-01	5.16E-01	5.16E-01	6.45E-01	6.45E-01	6.45E-01	7.09E-01	7.09E-01
SIGMA-RO/RO	6.72E+00	6.72E+00	7.23E+00	7.23E+00	7.23E+00	7.59E+00	7.59E+00	7.59E+00	7.34E+00	7.34E+00
(V-AV)	4.43E+00	4.51E+00	4.69E+00	4.50E+00	4.63E+00	4.54E+00	4.26E+00	4.23E+00	3.83E+00	4.01E+00
(V-AV)..2	1.96E+01	2.03E+01	2.20E+01	2.03E+01	2.19E+01	2.06E+01	1.81E+01	1.79E+01	1.47E+01	1.61E+01
DRAG COEFF	9.19E-01	8.87E-01	1.17E+00	1.27E+00	1.13E+00	1.65E+00	1.87E+00	1.89E+00	2.46E+00	2.24E+00
RF	4.10E+04	4.18E+04	4.34E+04	4.17E+04	4.33E+04	4.20E+04	3.94E+04	3.92E+04	3.55E+04	3.71E+04
DPM	6.72E+00	6.76E+00	1.43E+00	9.02E+00	9.97E+00	1.56E+01	1.46E+01	1.62E+01	1.68E+01	1.82E+01
DPM-DPL	3.34E+00	2.22E+00	2.15E+00	5.49E+00	6.41E+00	1.20E+01	1.13E+01	1.29E+01	1.41E+01	1.52E+01
(V-AV)..2/K	1.81E+01	1.87E+01	1.88E+01	1.74E+01	1.83E+01	1.68E+01	1.48E+01	1.46E+01	1.24E+01	1.36E+01
DPM-DPL/K	3.08E+00	2.04E+00	1.84E+00	4.71E+00	5.49E+00	9.79E+00	9.20E+00	1.05E+01	1.19E+01	1.28E+01
MAN. GM	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.59E+00	1.35E+01	1.35E+01
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01
(ZR1+ZR2)/2	1.15E+00	4.80E-01	2.25E+01	1.09E+00	1.80E-01	1.10E-01	7.80E-01	8.80E-01	2.00E-02	8.00E-02

K=D.(SIG-RO)/RO

DATA SET 9 50 WPPM POLYMER

VISCOSITY (FT..2)/SEC 1.744E-05

MANOMETER READING (CM)

33.64 36.56
 33.54 36.66
 33.37 36.83
 33.39 36.81
 33.36 36.85
 32.98 37.22
 32.41 37.79

ZERO 1

0.00
 .12
 .10
 .04
 3.48
 .02
 .12

ZERO 2

0.00
 .08
 .06
 .02
 3.76
 .01
 .08

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	1	2	3	4	5	6	7	8	9	10
D/D	7.72E-01	7.72E-01	8.38E-01	8.38E-01	8.38E-01	9.02E-01	9.67E-01	0.	0.	0.
SIGMA-RO/RO	7.23E+00	7.23E+00	7.12E+00	7.12E+00	7.12E+00	7.07E+00	7.00E+00	0.	0.	0.
(V-AV)	2.79E+00	3.01E+00	1.79E+00	1.55E+00	1.11E+00	8.15E-01	4.52E-01	0.	0.	0.
(V-AV)..2	7.77E+00	9.08E+00	3.22E+00	2.40E+00	1.22E+00	6.64E-01	2.04E-01	0.	0.	0.
DRAG COEFF	4.98E+00	4.26E+00	1.28E+01	1.72E+01	3.38E+01	6.66E+01	2.30E+02	0.	0.	0.
RE	2.58E+04	2.79E+04	1.66E+04	1.43E+04	1.02E+04	7.55E+03	4.18E+03	0.	0.	0.
DPM	2.13E+01	2.20E+01	2.47E+01	2.47E+01	-9.69E-01	3.08E+01	3.85E+01	0.	0.	0.
DPM-DPL	1.95E+01	2.00E+01	2.35E+01	2.37E+01	-1.77E+00	3.03E+01	3.84E+01	0.	0.	0.
(V-AV)..2/K	6.65E+00	7.78E+00	2.80E+00	2.09E+00	1.06E+00	5.82E-01	1.80E-01	0.	0.	0.
DPM-DPL/K	1.67E+01	1.71E+01	2.05E+01	2.06E+01	-1.55E+00	2.65E+01	3.40E+01	0.	0.	0.
MAN. GM	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	1.35E+01	0.	0.	0.
MAN. THETA	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	2.84E-01	0.	0.	0.
(ZR1+ZR2)/2	0.	1.00E-01	8.00E-02	3.00E-02	3.82E+00	1.50E-02	1.00E-01	0.	0.	0.

$K=D. (SIG-RO) / RO$